

# Estimated sensitivity for auxiliary degrees of freedom of KAGRA interferometer

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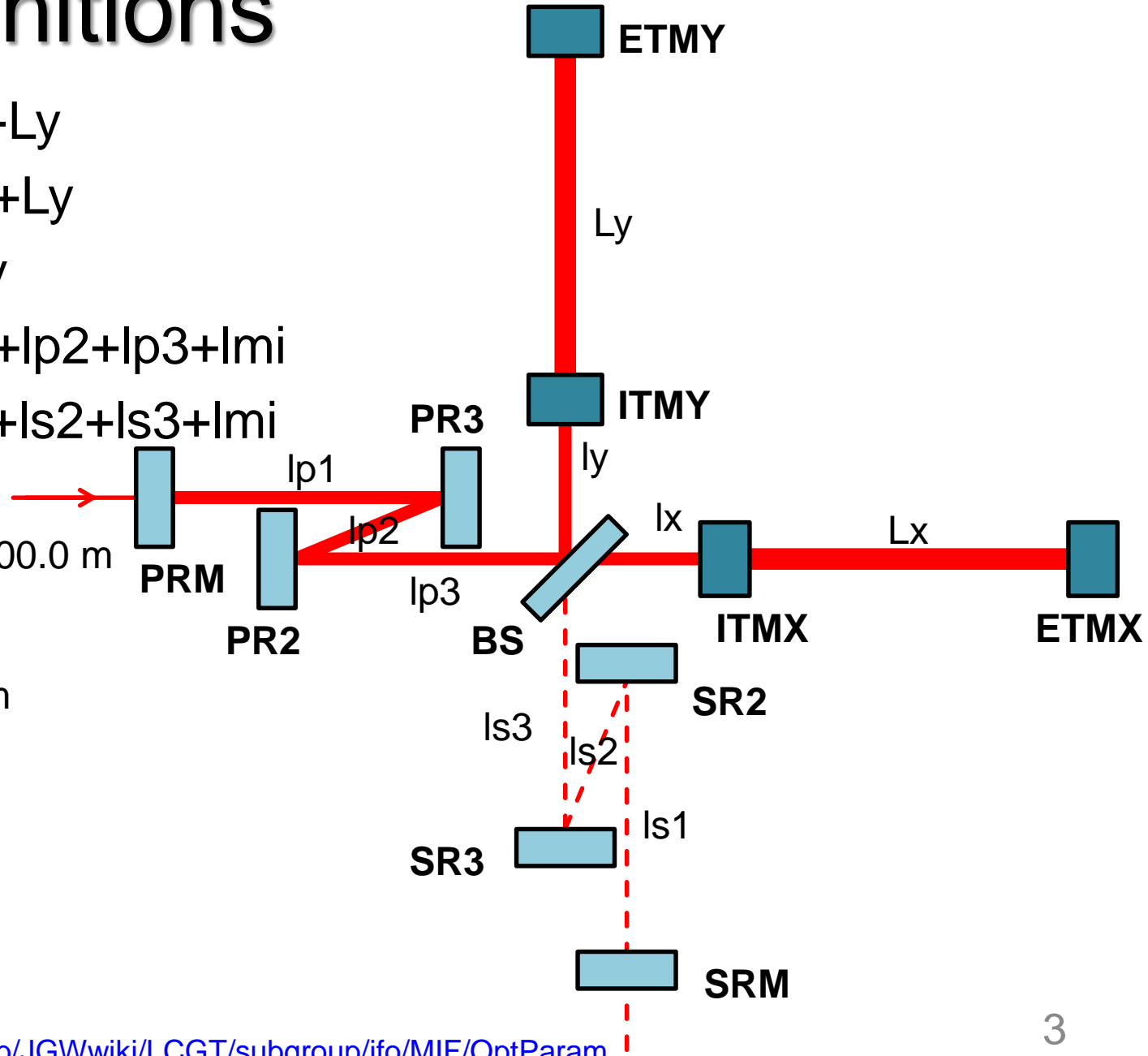
# Scope

- Estimate the displacement sensitivity for CARM, MICH, PRCL, SRCL
  - useful for the noise budget of auxiliary DoFs
- Based on the latest estimated sensitivity code ([JGW-T1707038](#))
- Seismic noise
  - fitted function from suspension model
- Suspension thermal noise
  - analytical calculation
- Mirror thermal noise
  - analytical calculation (we have to guess coating thickness)
- Quantum noise
  - analytical calculation for DARM, fitting of Optickle result for auxiliary DoFs

# Definitions

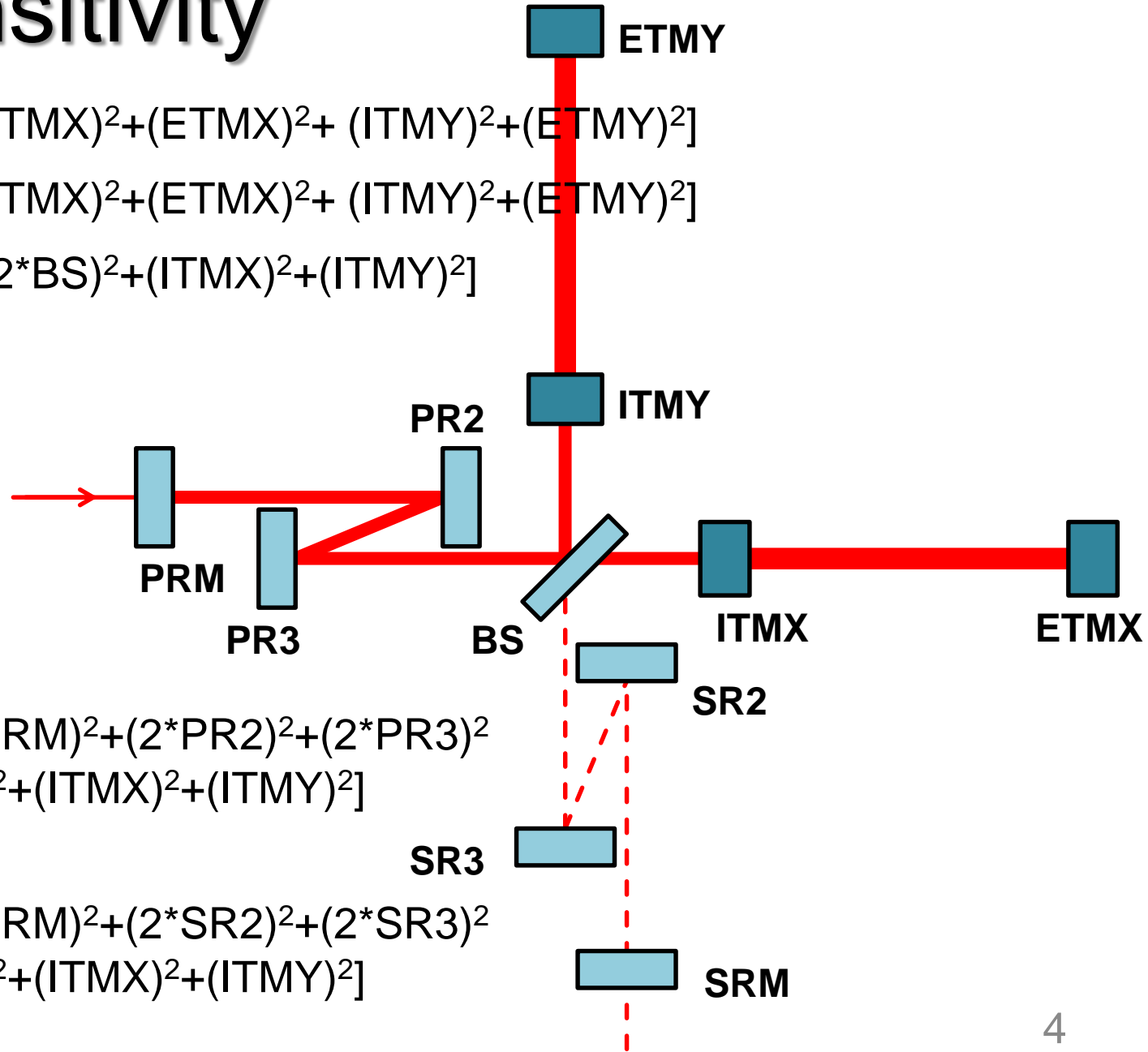
- DARM:  $L_x - L_y$
- CARM:  $L_x + L_y$
- MICH:  $l_x - l_y$
- PRCL:  $l_{p1} + l_{p2} + l_{p3} + l_{mi}$
- SRCL:  $l_{s1} + l_{s2} + l_{s3} + l_{mi}$

$L_x = L_y = L_{arm} = 3000.0 \text{ m}$   
 $L_x = 26.6649 \text{ m}$   
 $l_y = 23.3351 \text{ m}$   
 $l_{mi} = (l_x + l_y) / 2 = 25 \text{ m}$   
 $l_{p1} = 14.7615 \text{ m}$   
 $l_{p2} = 11.0661 \text{ m}$   
 $l_{p3} = 15.7638 \text{ m}$   
 $l_{s1} = 14.7412 \text{ m}$   
 $l_{s2} = 11.1115 \text{ m}$   
 $l_{s3} = 15.7386 \text{ m}$



# Sensitivity

- DARM:  $\sqrt{[(ITMX)^2+(ETMX)^2+ (ITMY)^2+(ETMY)^2]}$
- CARM:  $\sqrt{[(ITMX)^2+(ETMX)^2+ (ITMY)^2+(ETMY)^2]}$
- MICH:  $\sqrt{[(\sqrt{2} \cdot BS)^2+(ITMX)^2+(ITMY)^2]}$

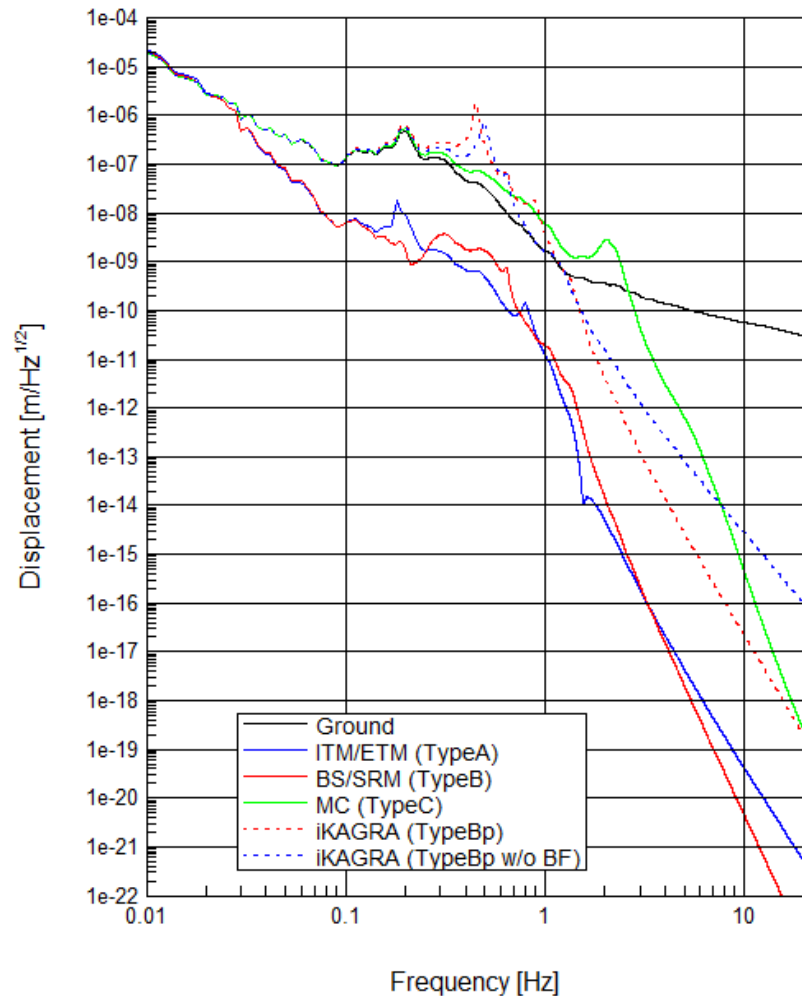


- PRCL:  $\sqrt{[(PRM)^2+(2 \cdot PR2)^2+(2 \cdot PR3)^2 +(\sqrt{2}/2 \cdot BS)^2+(ITMX)^2+(ITMY)^2]}$
- SRCL:  $\sqrt{[(SRM)^2+(2 \cdot SR2)^2+(2 \cdot SR3)^2 +(\sqrt{2}/2 \cdot BS)^2+(ITMX)^2+(ITMY)^2]}$

# Seismic noise

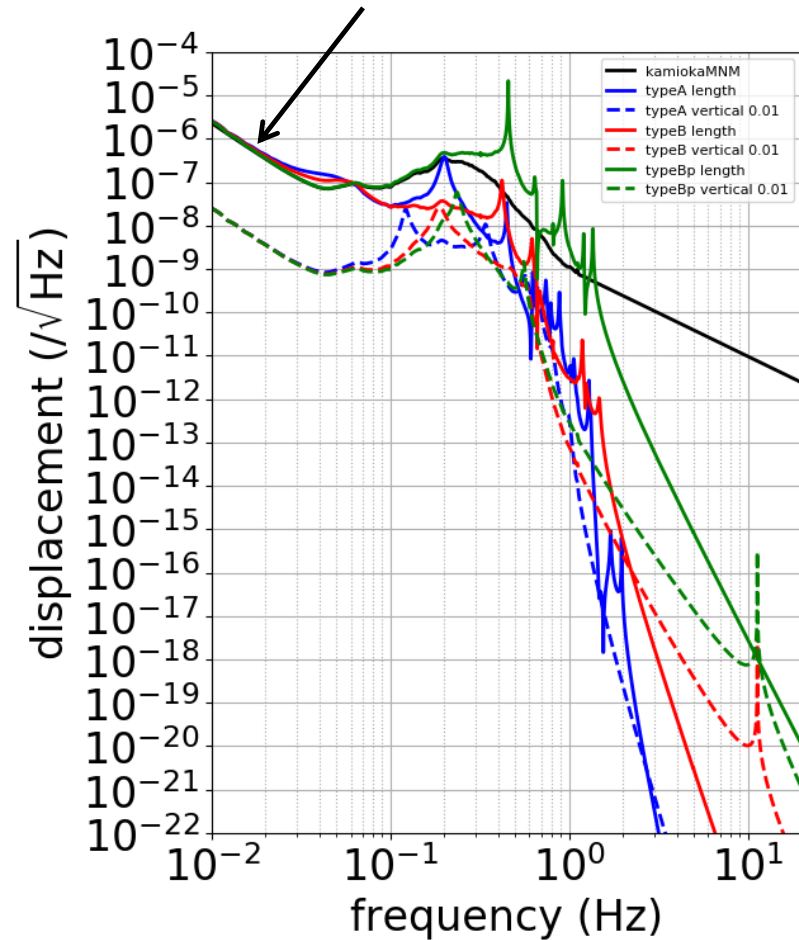
# Models

- There exists several models



TypeA-C rev3.png  
 from R. Takahashi  
 (used for K. Somiya's fitting)

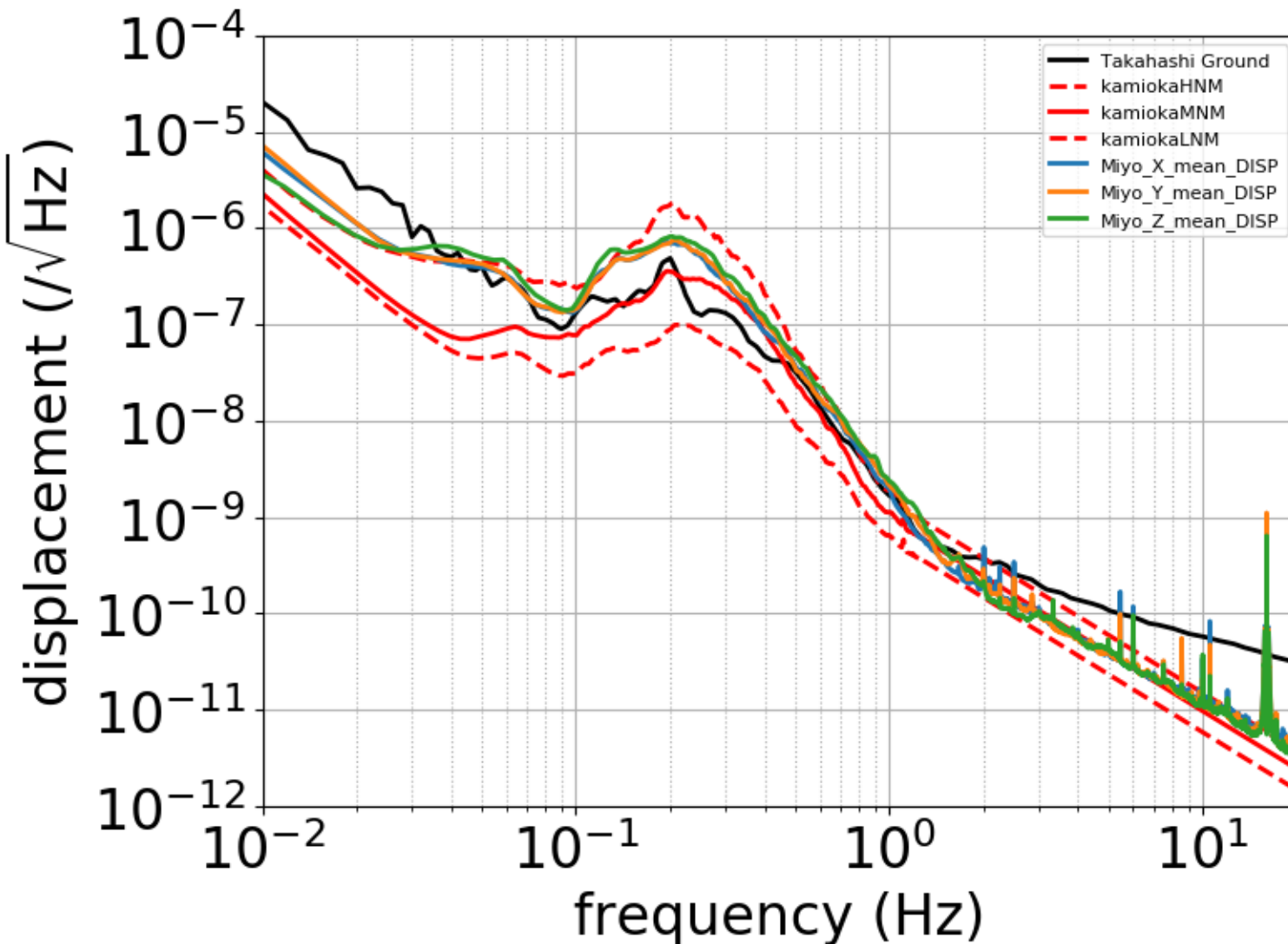
Medium Noise Model  
 from [JGW-T1402971](https://www.j-gw.org/wiki/JGW-T1402971)



Model from T. Sekiguchi  
 (used for actuator modeling in  
[JGW-P1707051](https://www.j-gw.org/wiki/JGW-P1707051))

# Seismic Noise Spectra

- Let's just use [JGW-T1402971](#) MNM for simplicity

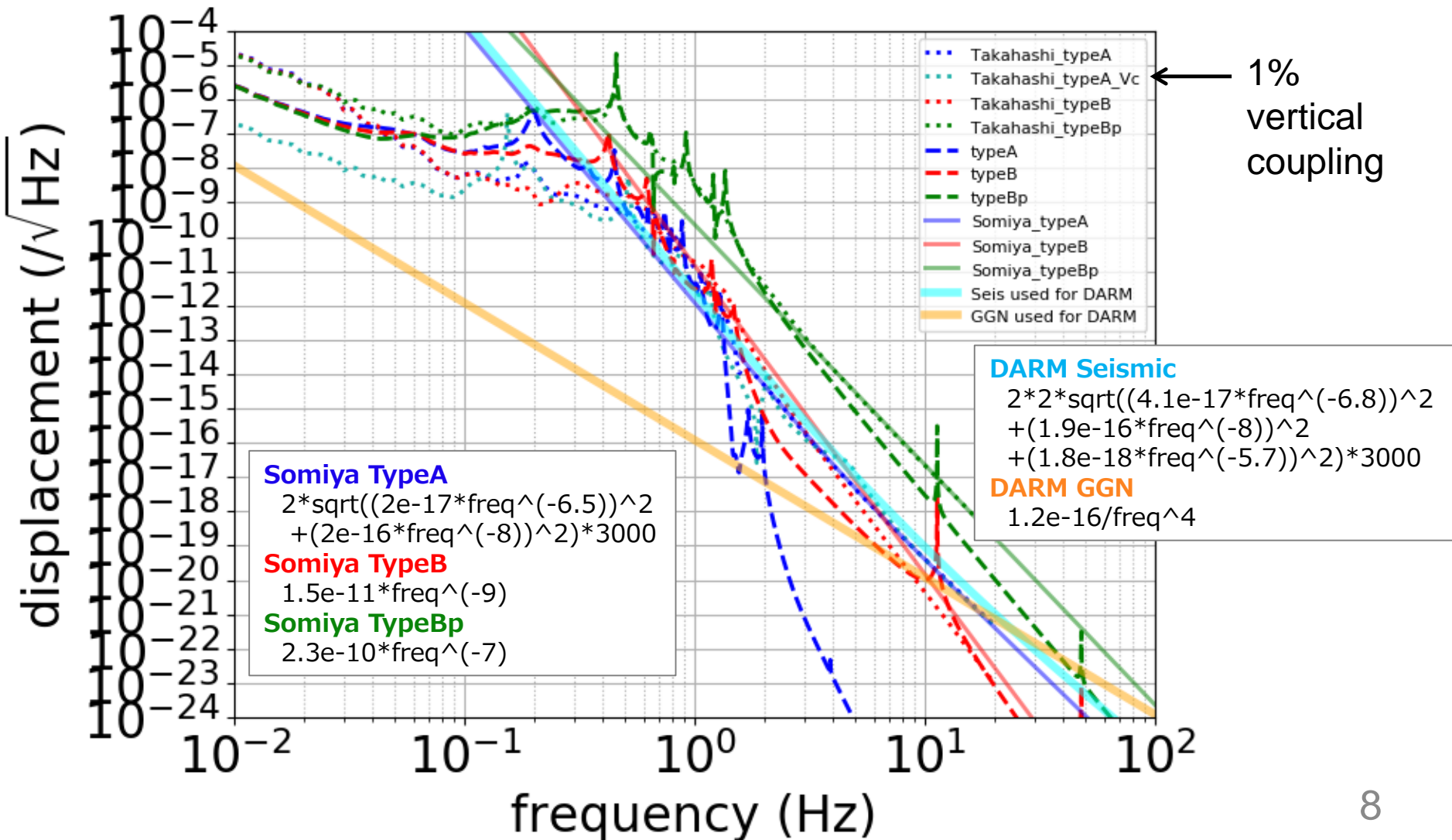


By Sekiguchi  
[JGW-T1402971](#)

By Miyo  
[JGW-T1910436](#)

# Comparison Between Models

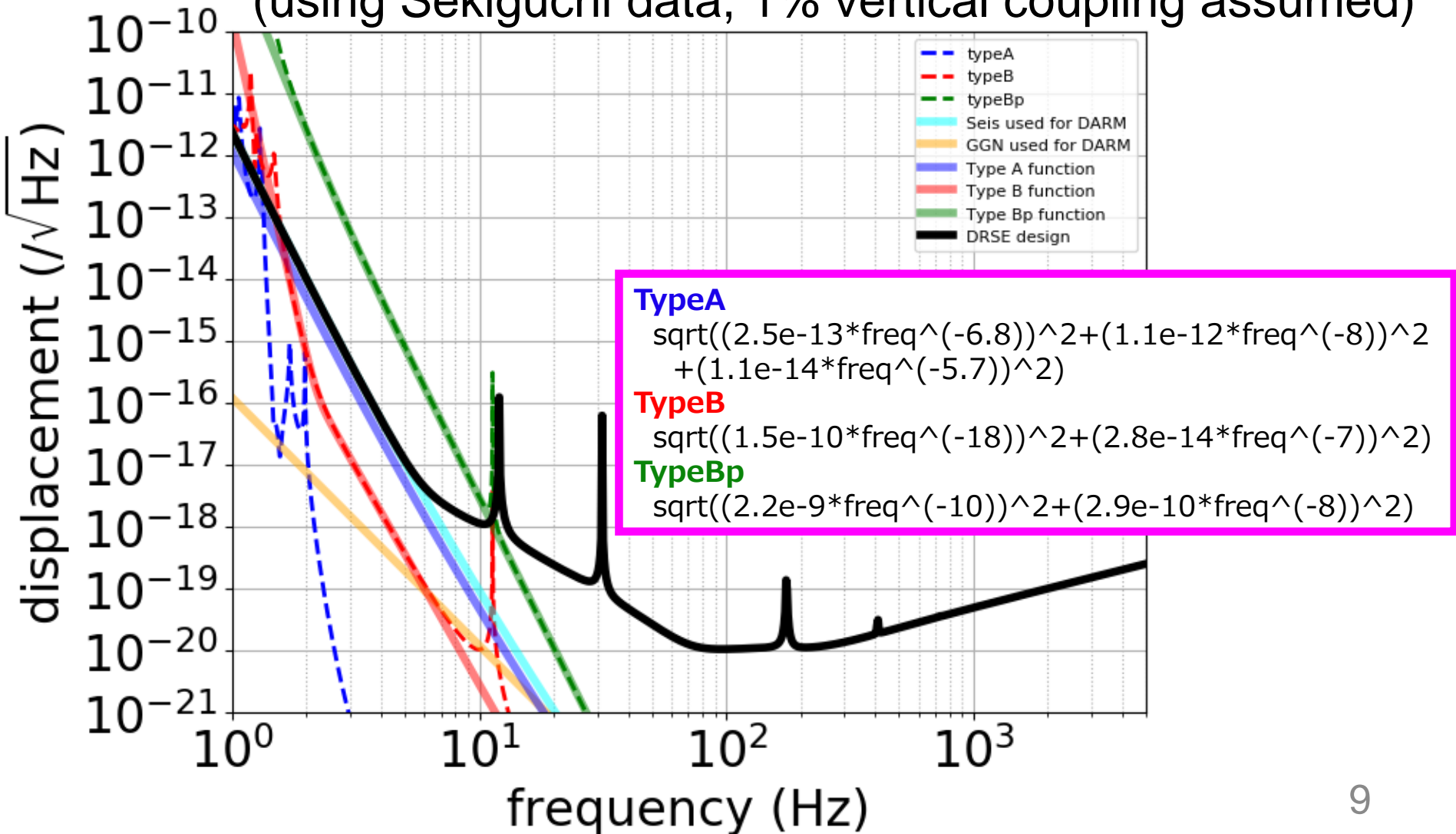
- Fitting function by Somiya based on Takahashi model





# New Seismic Function

- Function for one optic that work above ~3 Hz  
(using Sekiguchi data, 1% vertical coupling assumed)



# Suspension thermal noise

# Type-A Payload Configuration

[CQG 34, 225001 \(2017\)](#)

## IM suspension

4 CuBe wires  
16 K  
26.1 cm long, 0.6 mm dia.  
loss angle  $5e-6$

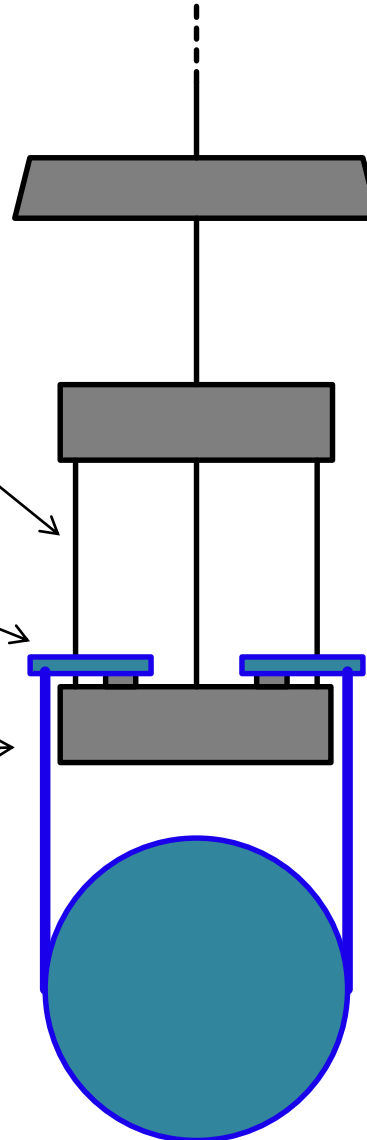
## Blade springs

4 Sapphire  
55 g each  
16 K  
loss angle  $7e-7$

## TM suspension

4 Sapphire fibers  
19 K (average of 16 K and 22 K)  
35 cm long, 1.6 mm dia.  
loss angle  $2e-7$

Vertical to horizontal coupling 1/200



**Platform**

**Marionette**

16 K

**Intermediate mass**

16 K

20.5 kg

**Test mass**

22 K

22.8 kg

# Type-B/Bp Payload Configuration

[CQG 34, 225001 \(2017\)](#)

Type-B info from Fabian

Type-B maraging rod [JGW-D1605614](#)

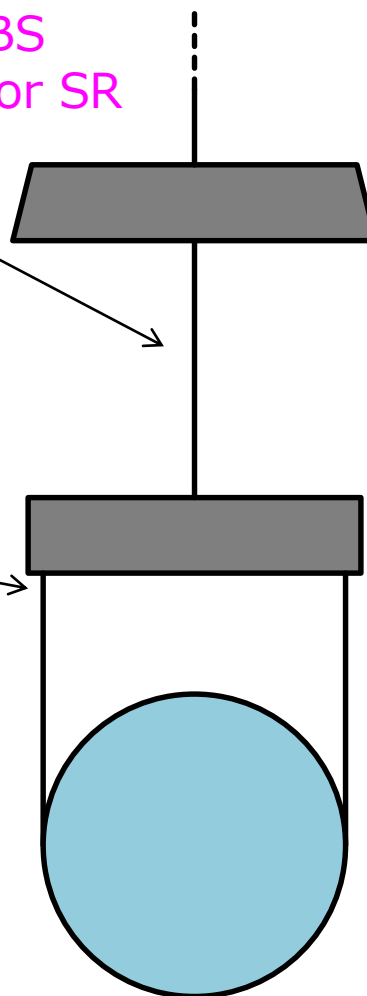
## IM suspension

1 maraging steel rod  
62.5 cm long, 3.6 m dia. body for BS  
59.85 cm long, 2.5 mm dia. body for SR  
(neck 2.65 cm long, 2 mm dia.)  
loss angle ??

## TM suspension

4 piano wire  
55.1 cm long, 0.3 mm dia. for BS  
58.7 cm long, 0.2 mm dia. For SRs  
??? for PRs  
loss angle ??

Vertical to horizontal coupling 1/200



**Bottom filter**

**Intermediate mass**

36.5 kg for BS,  
15.6 kg for others

**Test mass**

18.9 kg for BS,  
10.8 kg for others

# Mirror thermal noise

# Mirror and Coating Parameters

- Coating: silica/tantala (loss angle:  $3e-4$  /  $5e-4$ )

	ITM/ETM	BS	SRM/2/3	PRM/2/3
Material	Sapphire	Fused silica	Fused silica	Fused silica
Diameter	22 cm	37 cm	25 cm	25 cm
Thickness	15 cm	8 cm	10 cm	10 cm
Mass	22.8 kg	18.9 kg	10.8 kg	10.8 kg
Temperature	22 K	290 K	290 K	290 K
Substrate loss angle	$1e-8$	$1/(6.5e-12/\text{thickness}+7.6e-12*f^{0.77})$ <a href="#">Physics Letters A 352, 3 (2006)</a>		
Coating layers	22 / 40	<b>4</b>	<b>4 / 18 / 18</b>	<b>4 / 18 / 18</b>
Beam radius	3.5 cm	3.62 cm	0.43 / 0.43 / 3.67 cm	0.46 / 0.46 / 3.66 cm

Number of coating layers for fused silica mirrors are derived from calculation using reflectivity. Coating thermal noise of Type-B/Bp suspensions are not very important since quantum noises for auxiliary DOFs are quite high.

BS thermal noise is tricky ([LIGO-T0900209](#)) but not considered carefully here.

[JGW-T1707038](#)

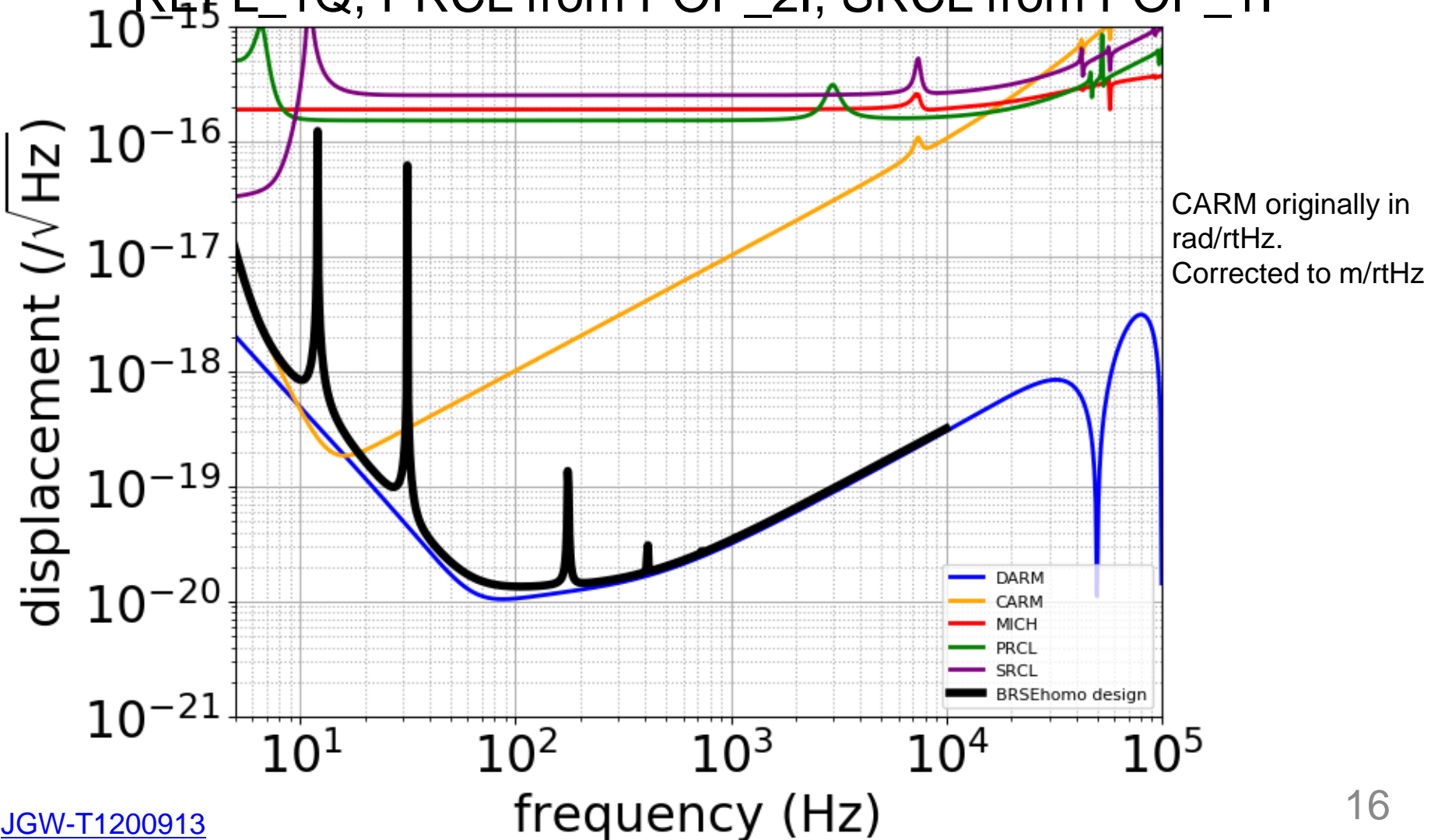
[Classical and Quantum Gravity 34, 225001 \(2017\)](#)

<http://gwwiki.icrr.u-tokyo.ac.jp/JGWwiki/LCGT/subgroup/ifo/MIF/OptParam>

# Quantum noise

# Optickle Simulation (BRSE Aso)

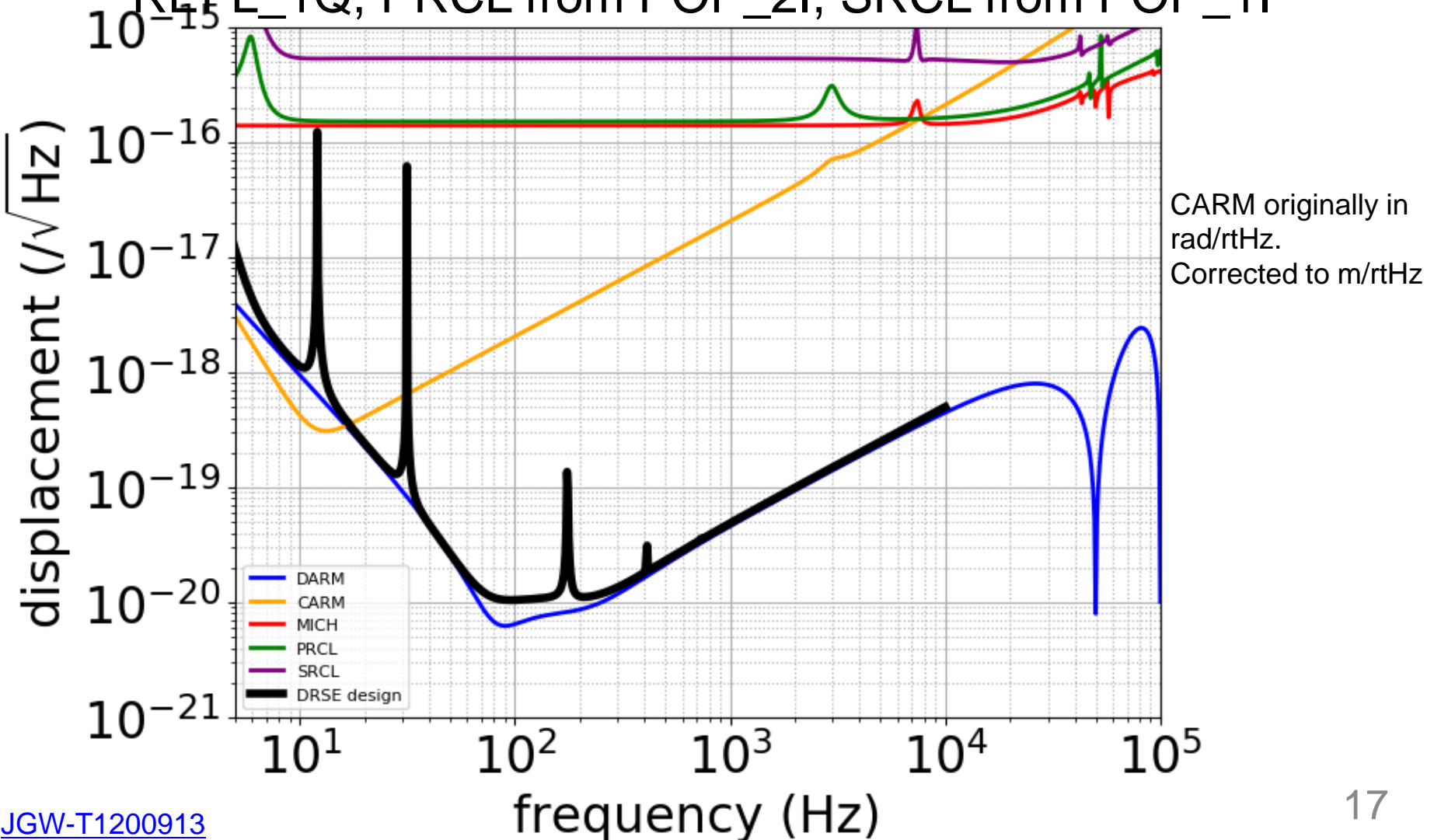
- DARM from AS\_DC, CARM from REFL\_1I, MICH from REFL\_1Q, PRCL from POP\_2I, SRCL from POP\_1I





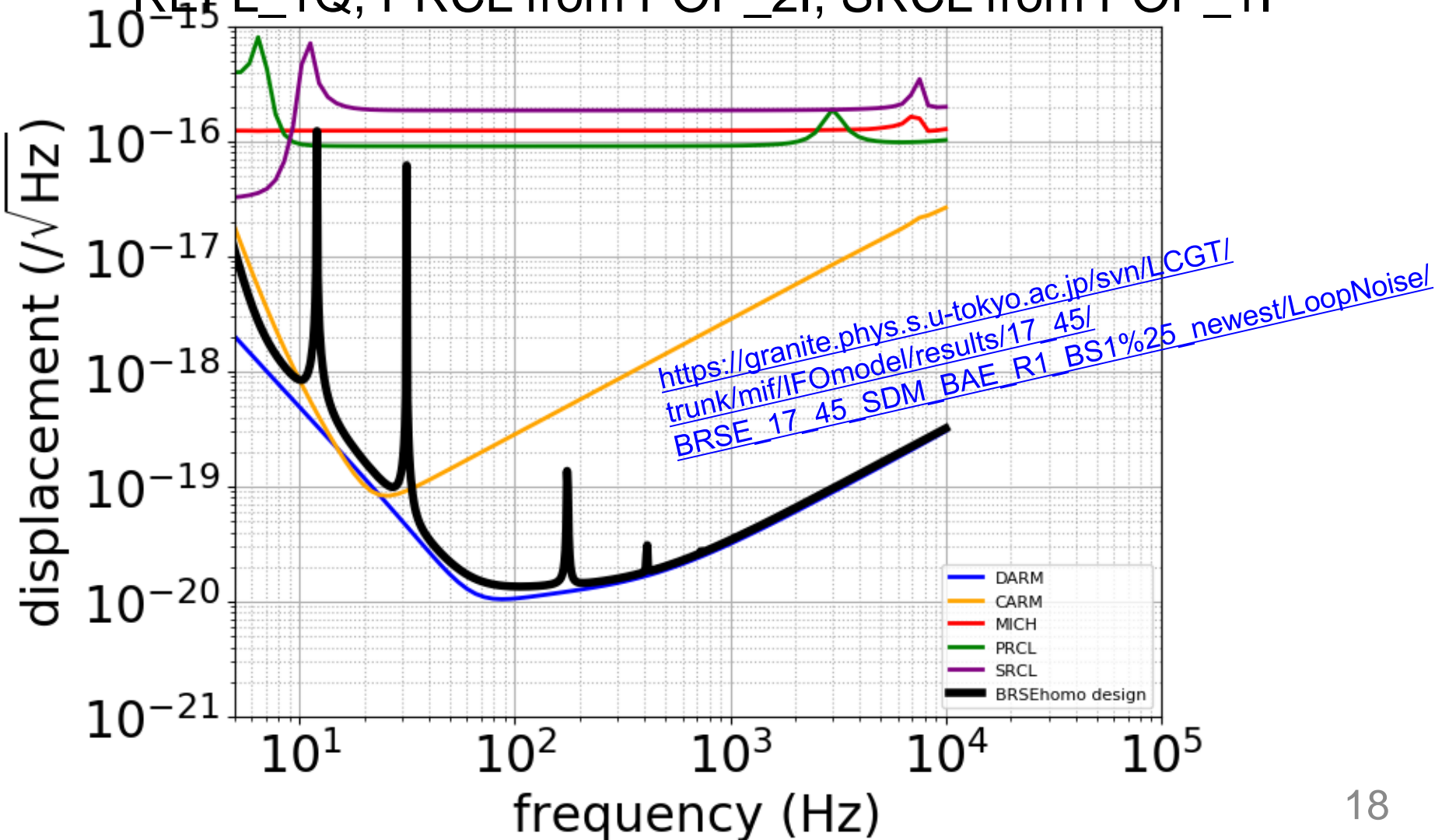
# Optickle Simulation (DRSE Aso)

- DARM from AS\_DC, CARM from REFL\_2I, MICH from REFL\_1Q, PRCL from POP\_2I, SRCL from POP\_1I



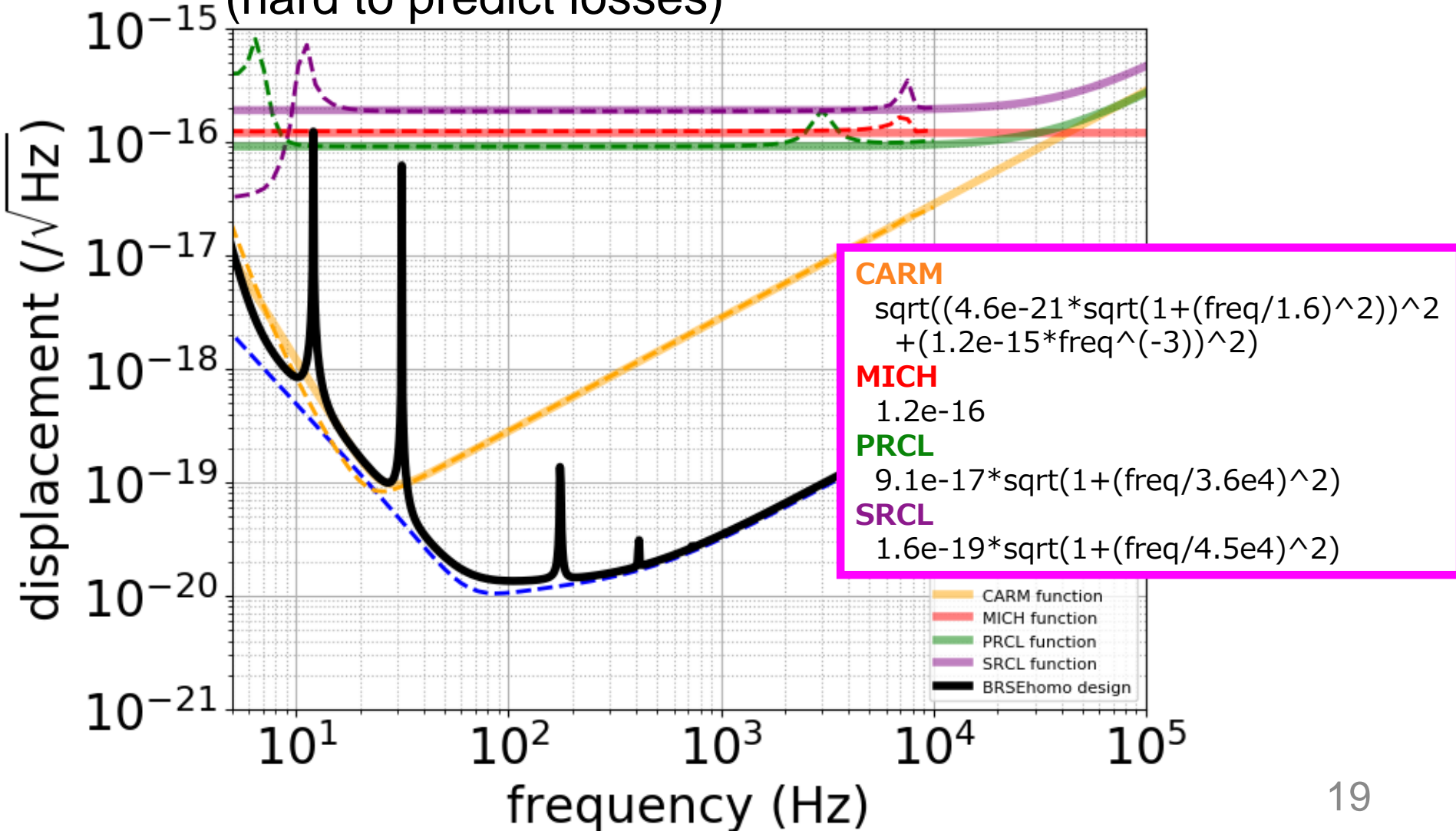
# Optickle Simulation (BRSE Enomoto)

- DARM from AS\_DC, CARM from REFL\_1I, MICH from REFL\_1Q, PRCL from POP\_2I, SRCL from POP\_1I



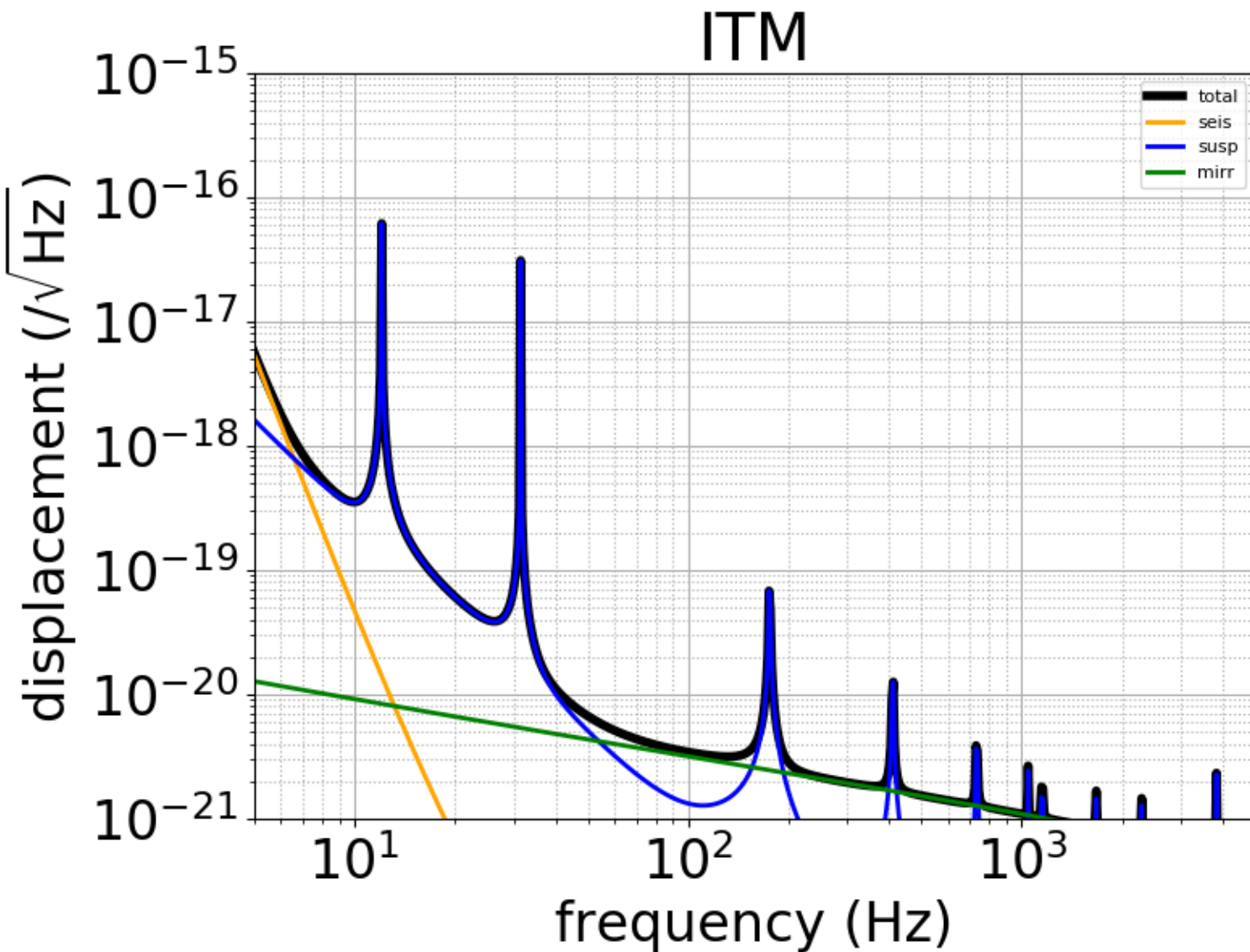
# Quantum Function

- Use fitted function instead of doing analytical calculation (hard to predict losses)

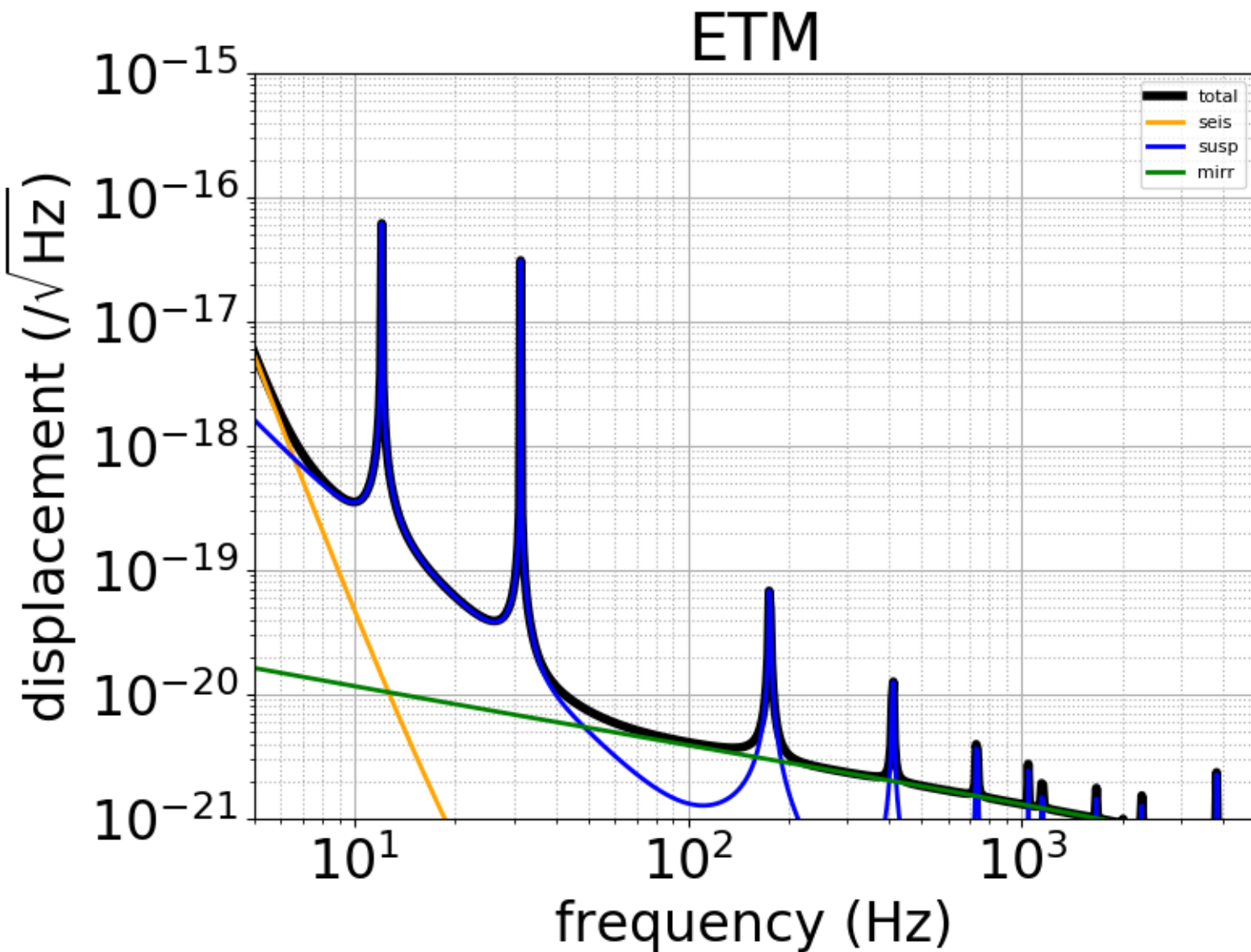


# Displacement sensitivity

# Displacement Noise: ITM



# Displacement Noise: ETM



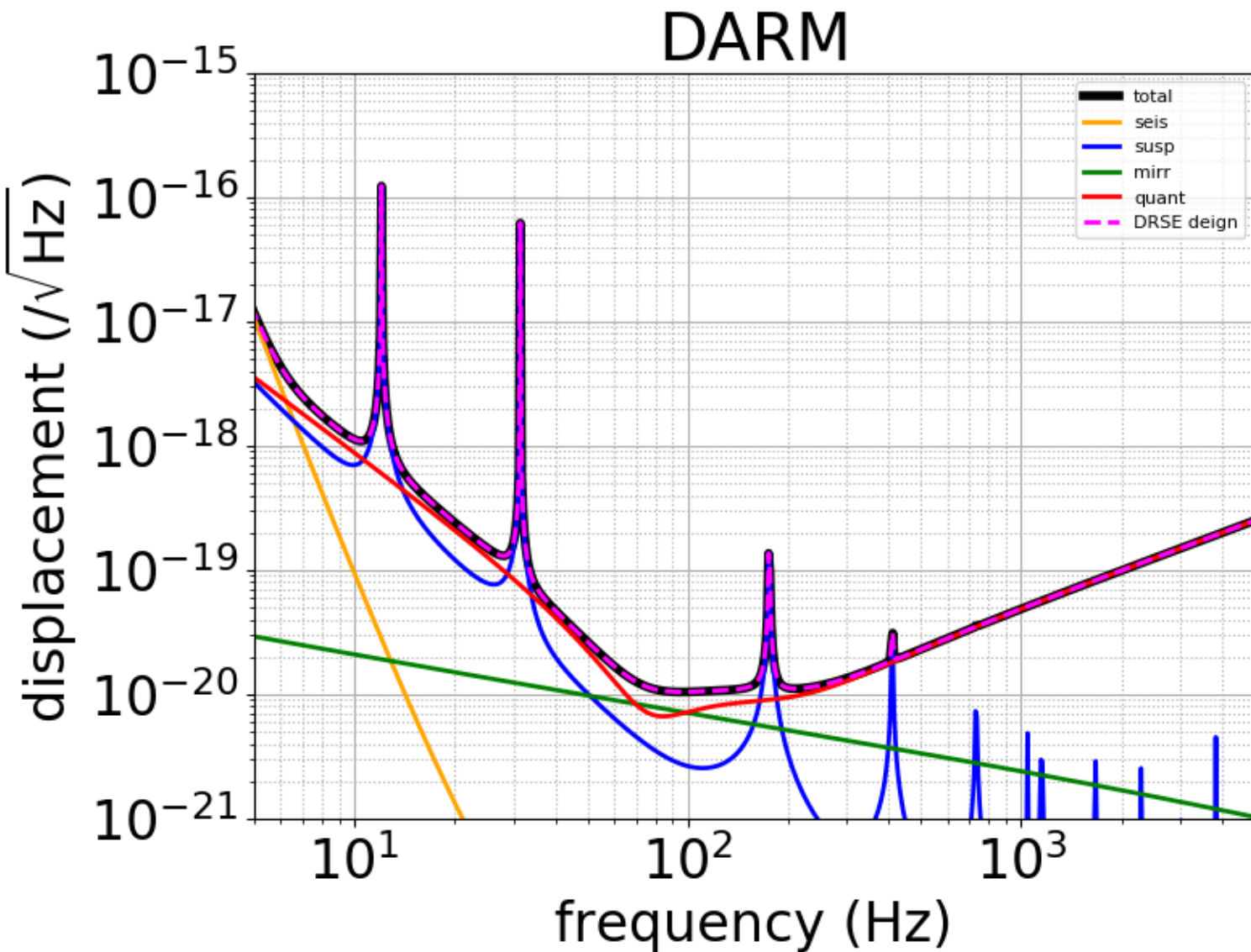
# Displacement Noise: BS

# Displacement Noise: SRM

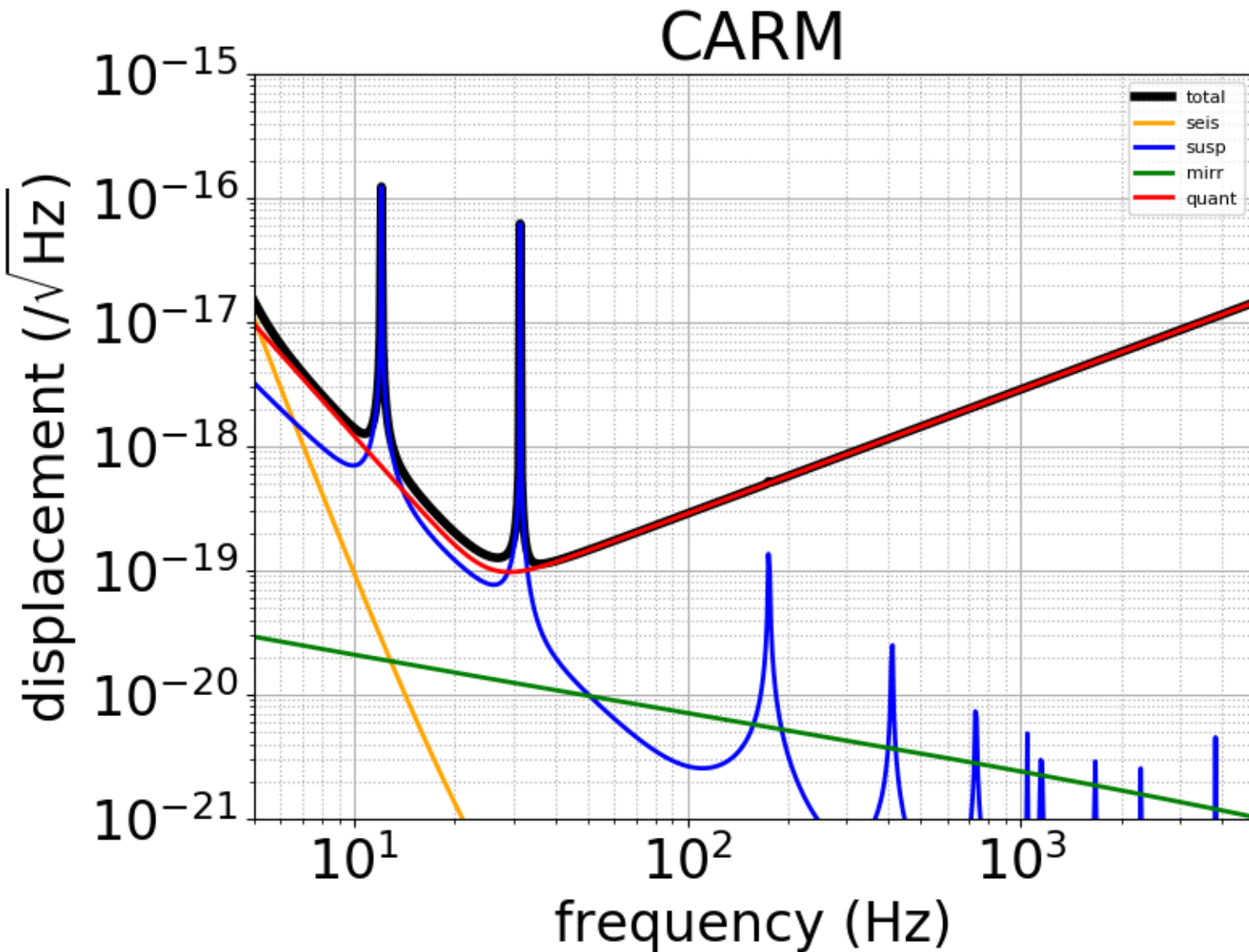


# Displacement Noise: PRM

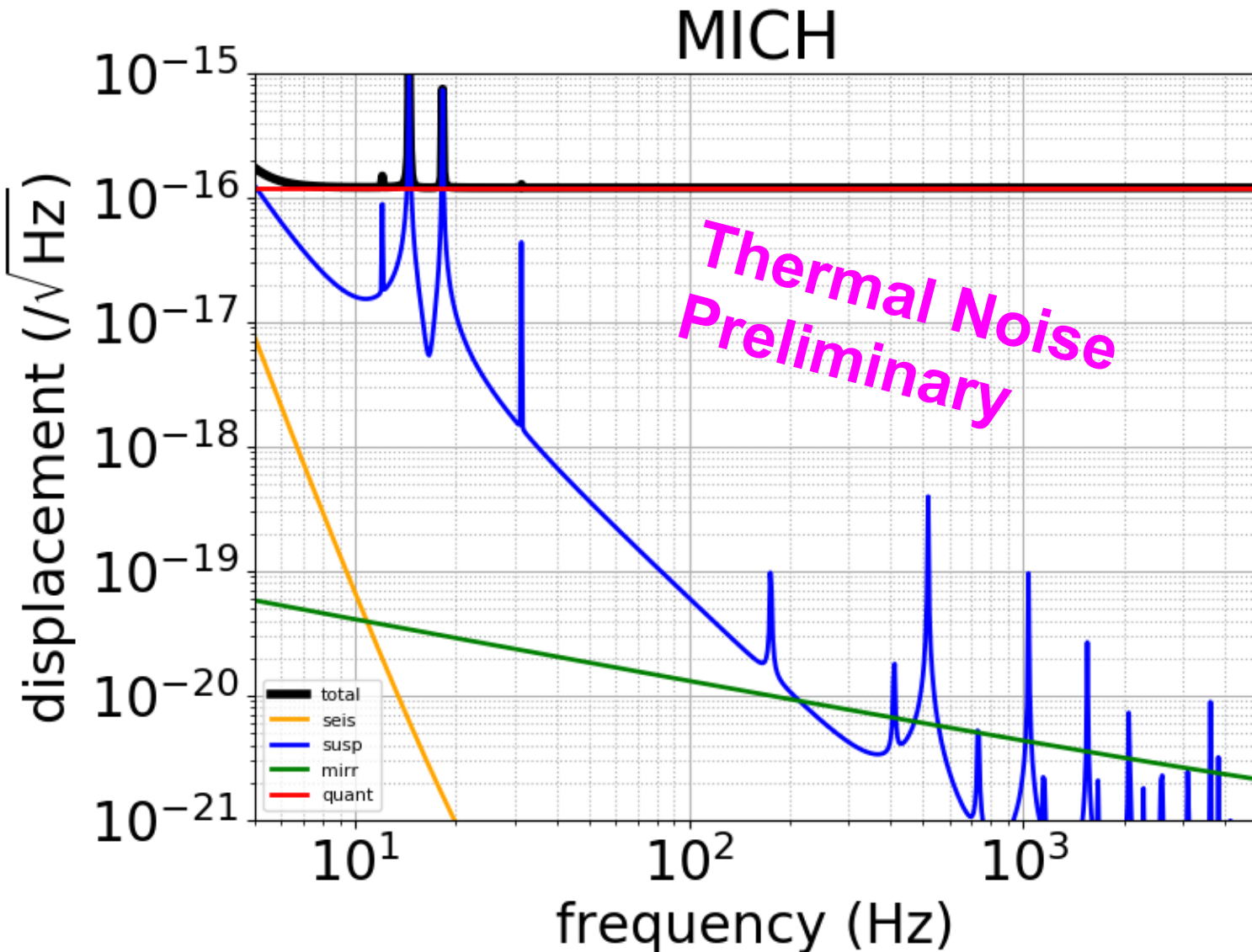
# Displacement Sensitivity: DARM



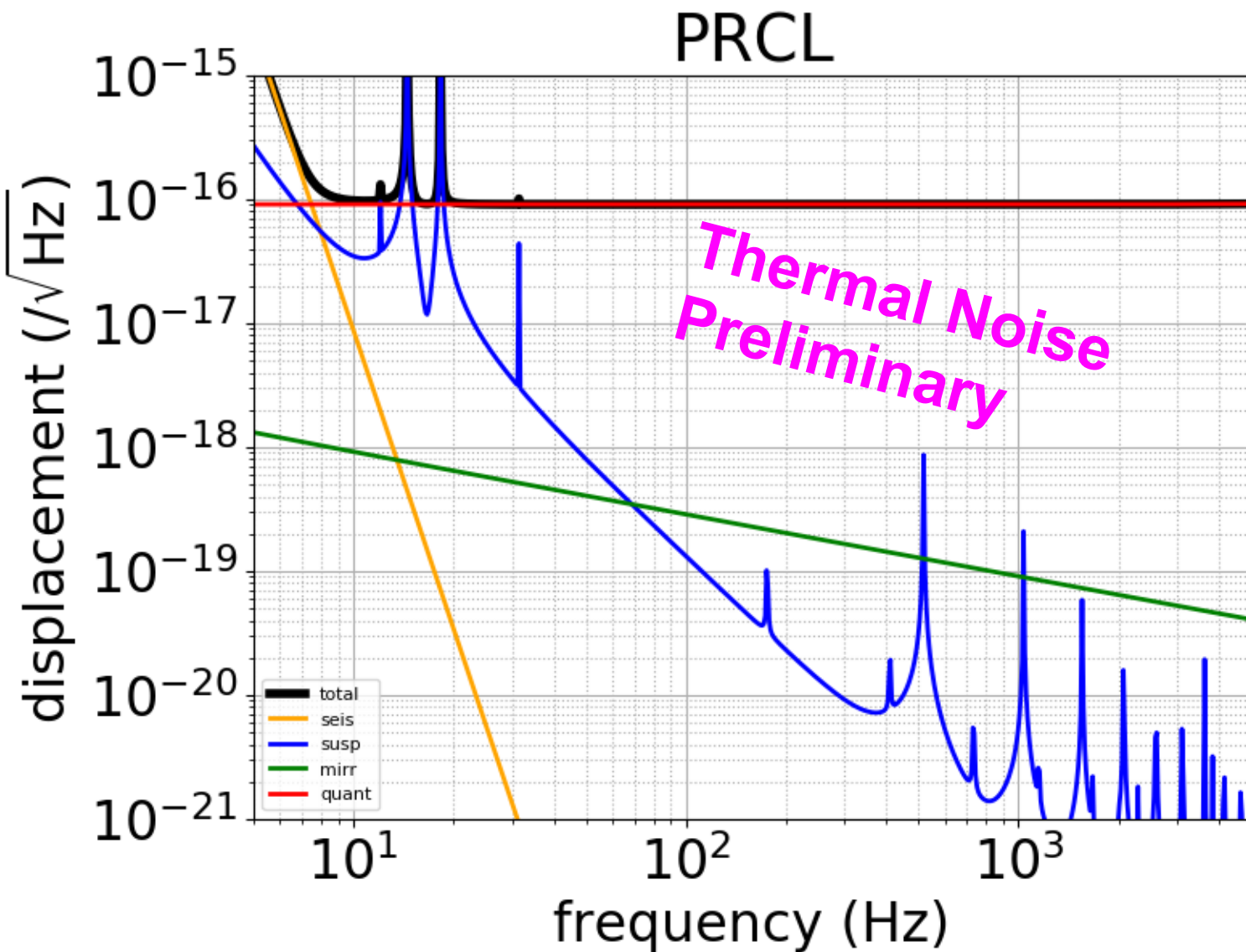
# Displacement Sensitivity: CARM



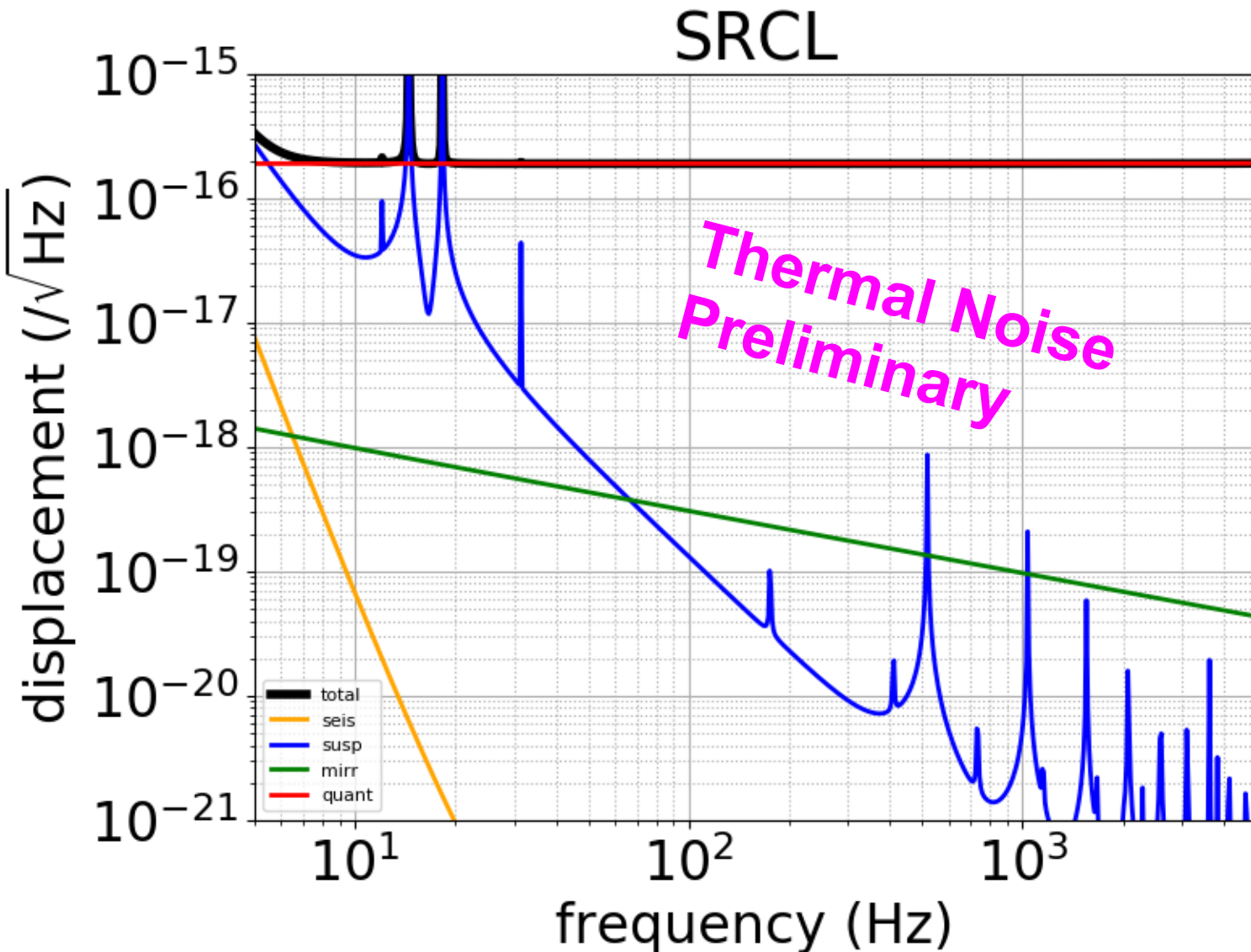
# Displacement Sensitivity: MICH



# Displacement Sensitivity: PRCL



# Displacement Sensitivity: SRCL



# Displacement Sensitivity Summary

