



Advanced Virgo suspensions control

Lucia Trozzo



東京大学
THE UNIVERSITY OF TOKYO

OUTLINE

- **Advanced Virgo**
- **Seismic noise and mechanical attenuators of the seismic vibrations: The Superattenuator.**
 - **Suspension control**
 - **Blending technique**
 - Above 100 mHz
 - Below 100 mHz
 - GIPC Control
 - **Suspension control Noise**

Virgo detector



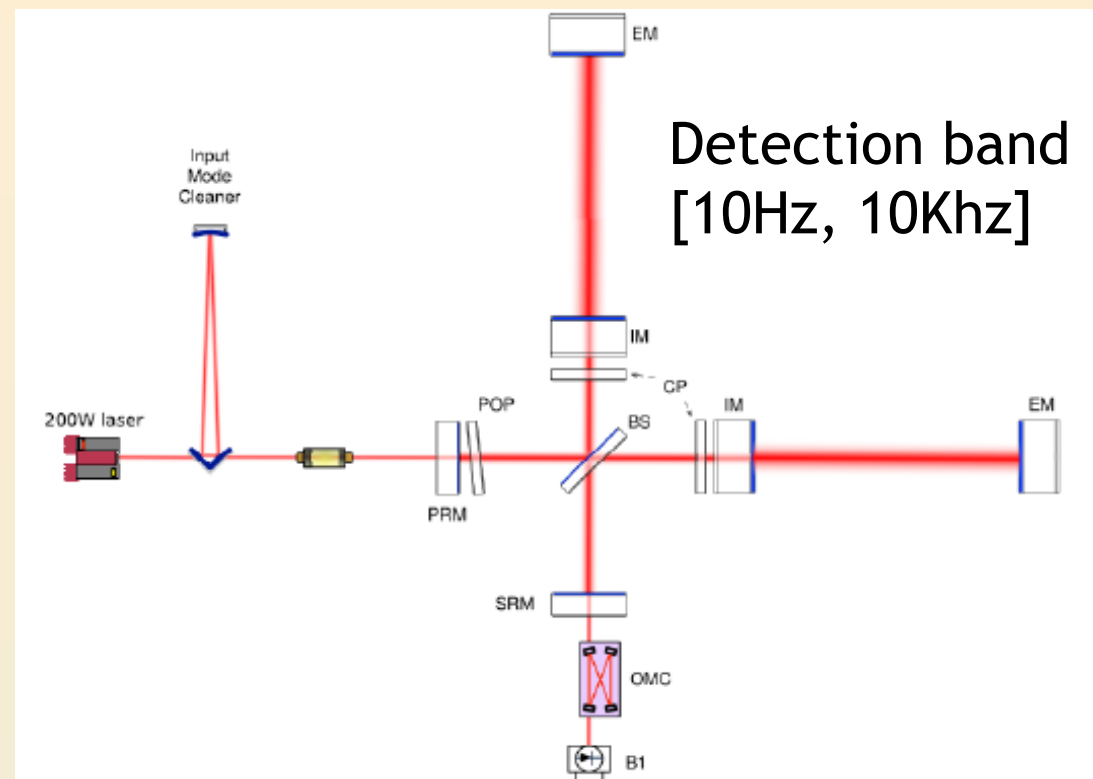
❖ **Virgo is a ground based GWs detector located in Cascina (Pisa, Tuscany, Italy)**

❖ **The infrastructure is hosted in the European Gravitational Observatory (EGO)**

Virgo is designed and built by a collaboration between the French Centre National de la Recherche Scientifique (CNR) and the Italian Istituto Nazionale di Fisica Nucleare (INFN).

The EGO-Virgo is an international collaboration of scientist from France, Italy, Netherlands, Poland, Hungary and Spain.

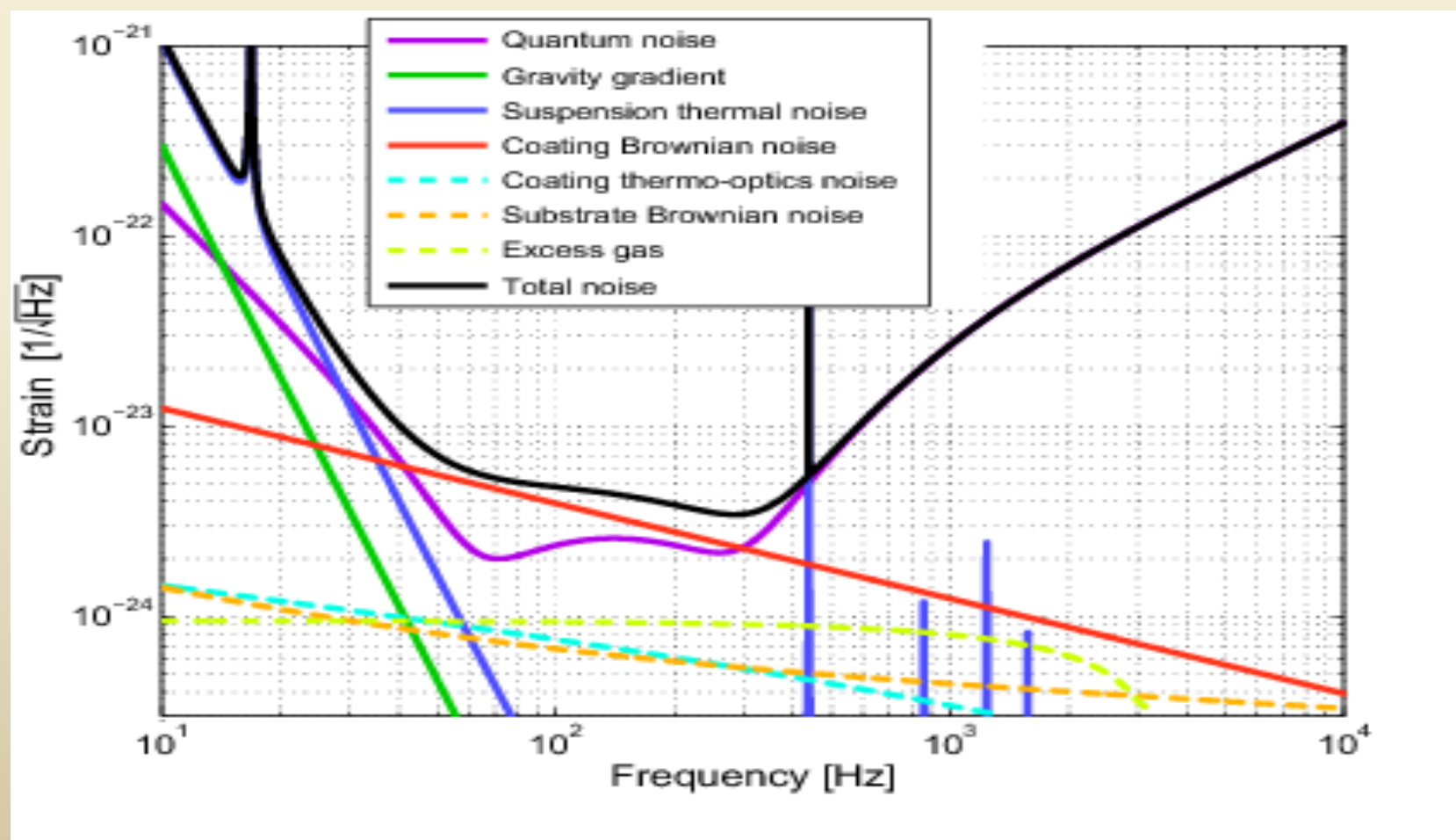
Advanced Virgo



- Michelson ITF + 3 km long FP cavities
- Detection band [10 Hz, 10 kHz]

This makes possible to observe a signal coming from a typical binary system (NS-NS of $1.4 M_{\odot}$) up to **150 Mpc** with respect to the 15 Mpc of Virgo

Design strain sensitivity curve



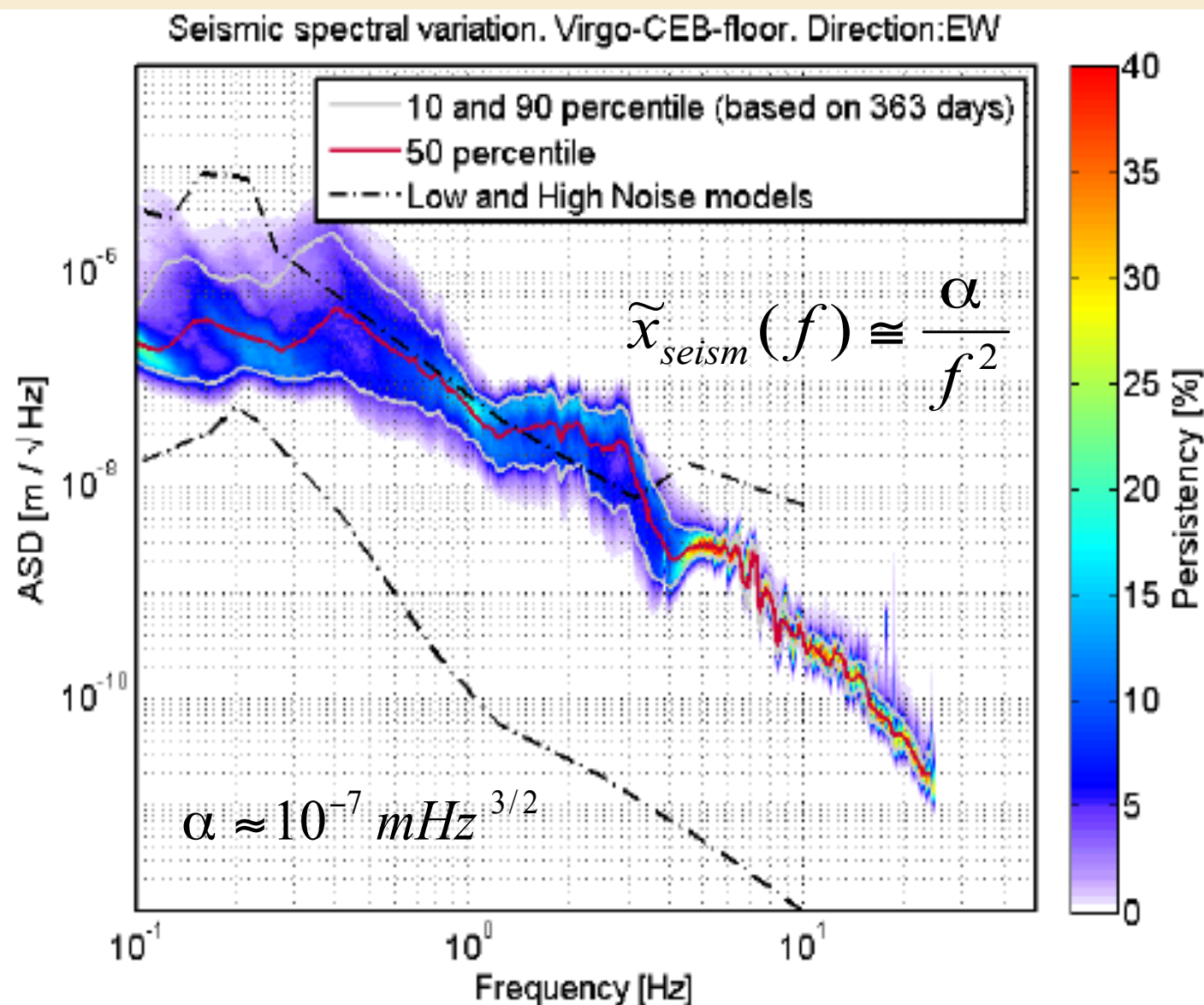
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VIRGO interferometer has been designed to detect GW starting from 10 Hz

➤ **Seismic noise:** is the dominant noise at low frequencies

Typical amplitude spectral density



In the detection band ($f > 10$ Hz) the seismic noise reaches the values:

$$\tilde{x}_{seism} \approx 10^{-9} m / Hz^{1/2} \quad f \approx 10 Hz$$

To detect the little displacement due to a GW we need a residual motion at 10 Hz of

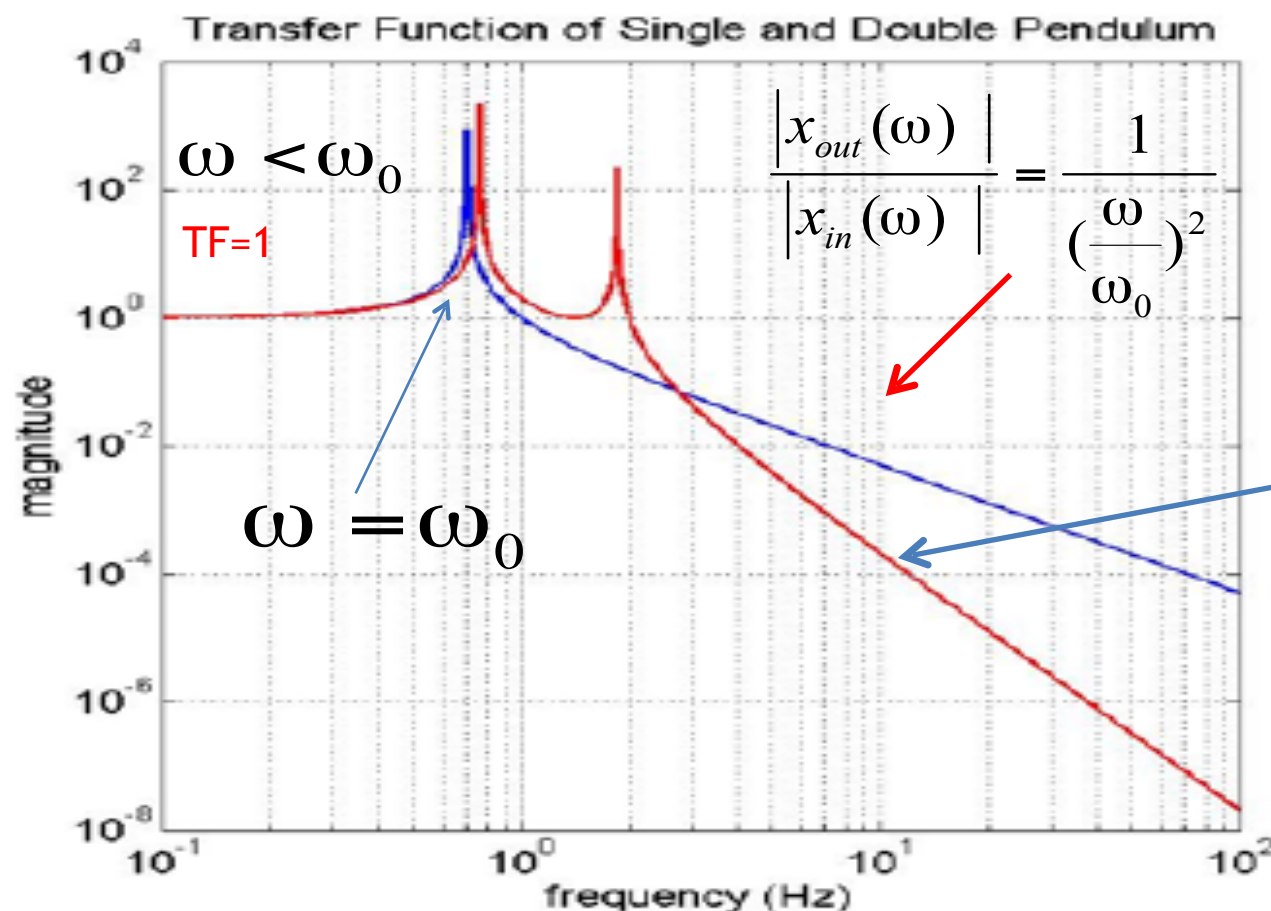
$$\tilde{x} \approx 10^{-18} m / Hz^{1/2}$$

a seismic isolation with an attenuation factor~ 10 order of magnitude is needed!!!

A good approximation of the free falling mass is represented by the simple pendulum



$$\frac{|x_{out}(\omega)|}{|x_{in}(\omega)|} = \frac{1}{1 - \left(\frac{\omega}{\omega_0}\right)^2}$$



Having 2 cascaded harmonic oscillators we obtain

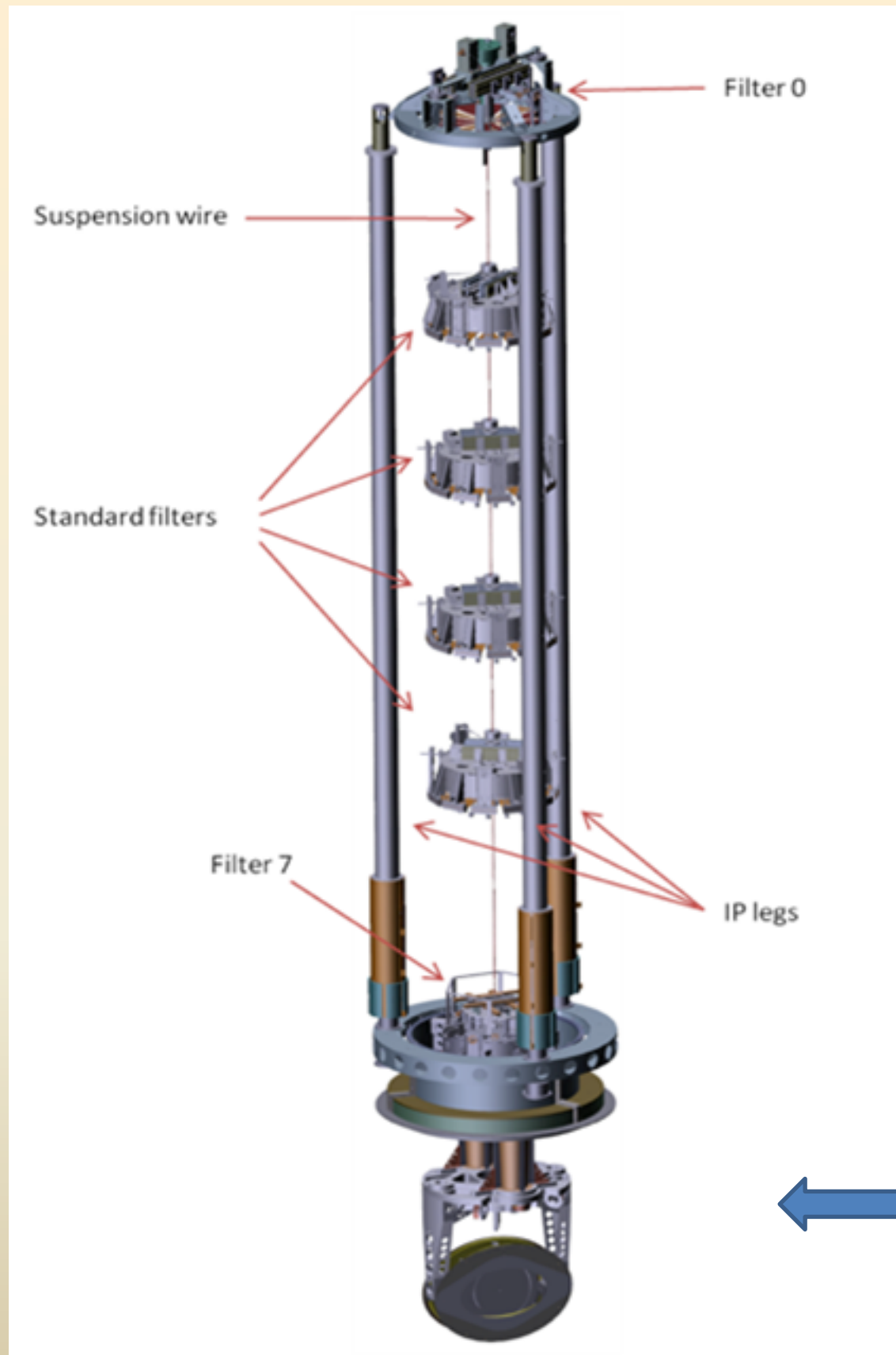
$$\frac{|x_{out}(\omega)|}{|x_{in}(\omega)|} = \frac{A}{(\omega)^4}$$

$$A = \omega_1^2 \cdot \omega_2^2$$

Solution adopted in VIRGO is based on the idea to cascade a certain number of harmonic oscillators of length ~1 m to obtain a sophisticated mechanical structure:

The SUPERATTENUATOR

The Superattenuator



The suspension system is developed by INFN:

- Superattenuator: INFN Pisa
- Payload: INFN Roma1

VIRGO uses this system for all optics and benches excepted for auxiliary benches

✓ Pre-isolation stage:
the Inverted Pendulum (IP-3 legs structure)
+ mechanical filter (called Filter 0-F0)

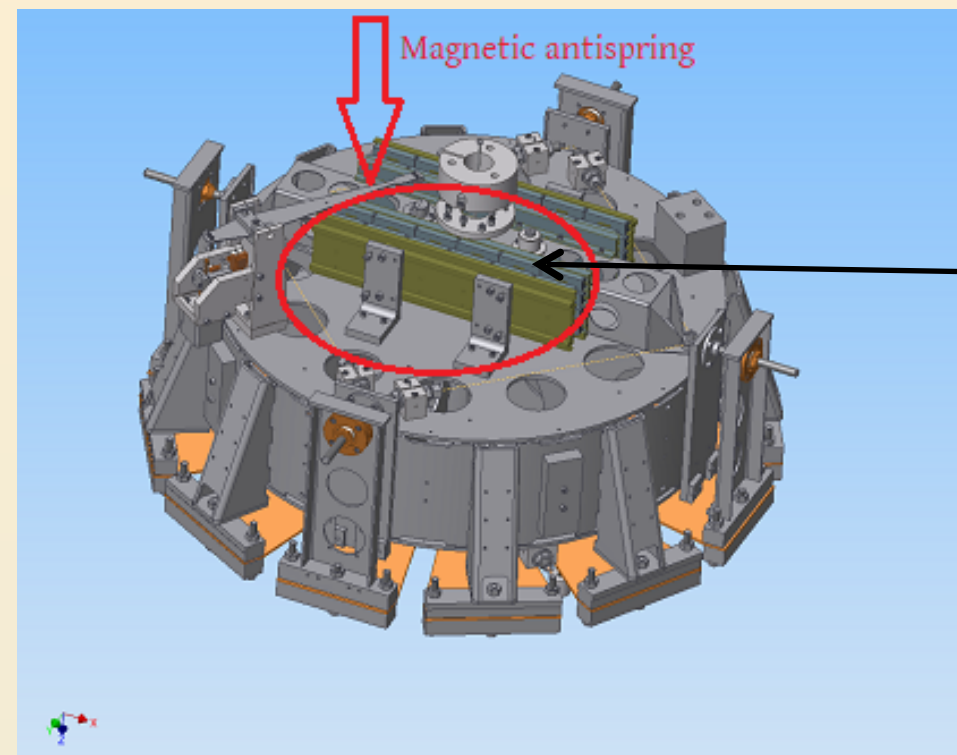
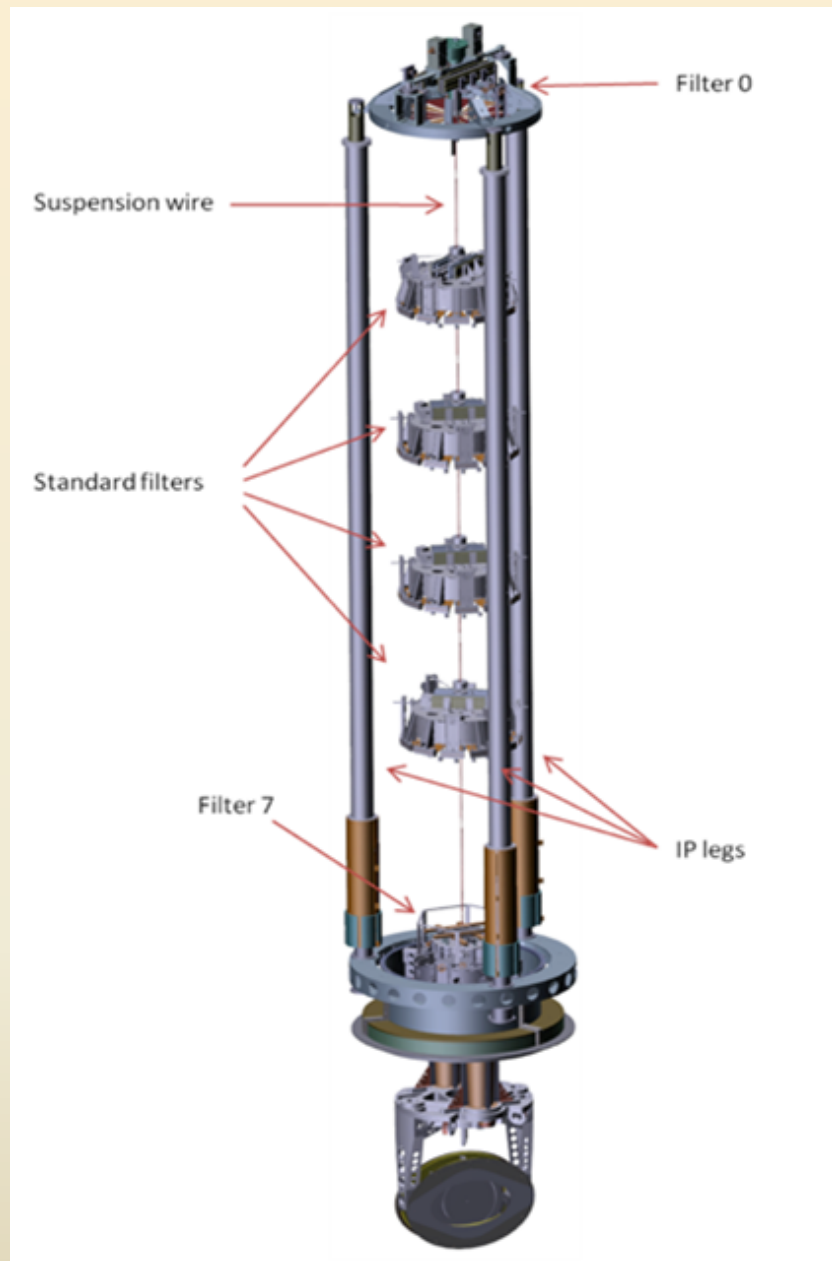
✓ The passive multi-stage pendulum chain:
five mechanical filters F1, F2, F3, F4 and F7
(Steering Filter).

✓ Last stage or payload: the marionette and
the mirror.

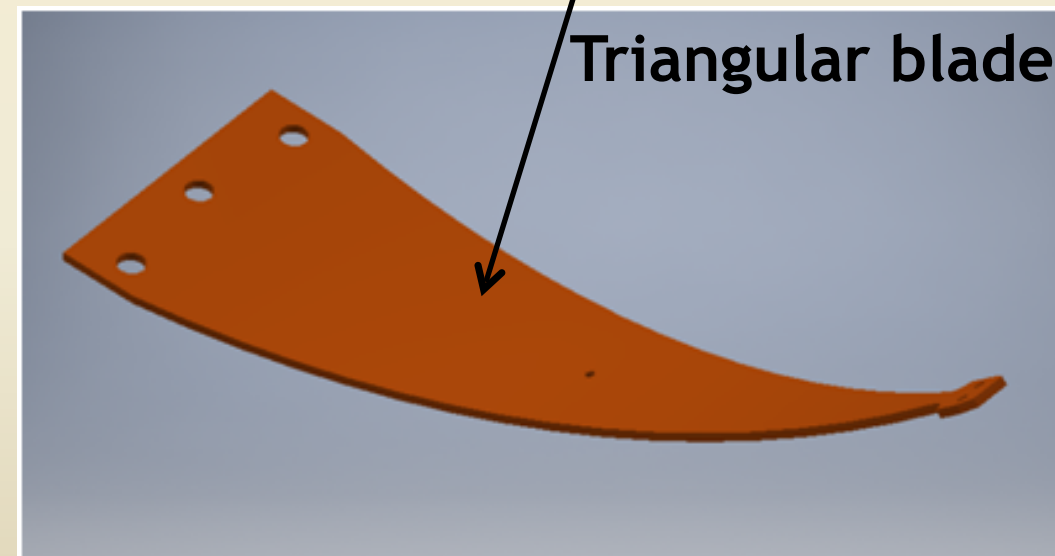
The normal modes of the pendulum
mechanical structure are confined
below 2 Hz

Mechanical attenuators of the seismic vibrations

The system provides a good seismic isolation in horizontal direction (IP) as well as the vertical one.



- Standard filter:
- set of magnetic anti-sprigs
 - elastic elements of triangular shape



The vertical normal modes of the mechanical filter are below 0.4 Hz

OUTLINE

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- Seismic noise and mechanical attenuators of the seismic vibrations: The Superattenuator.

- Suspension control

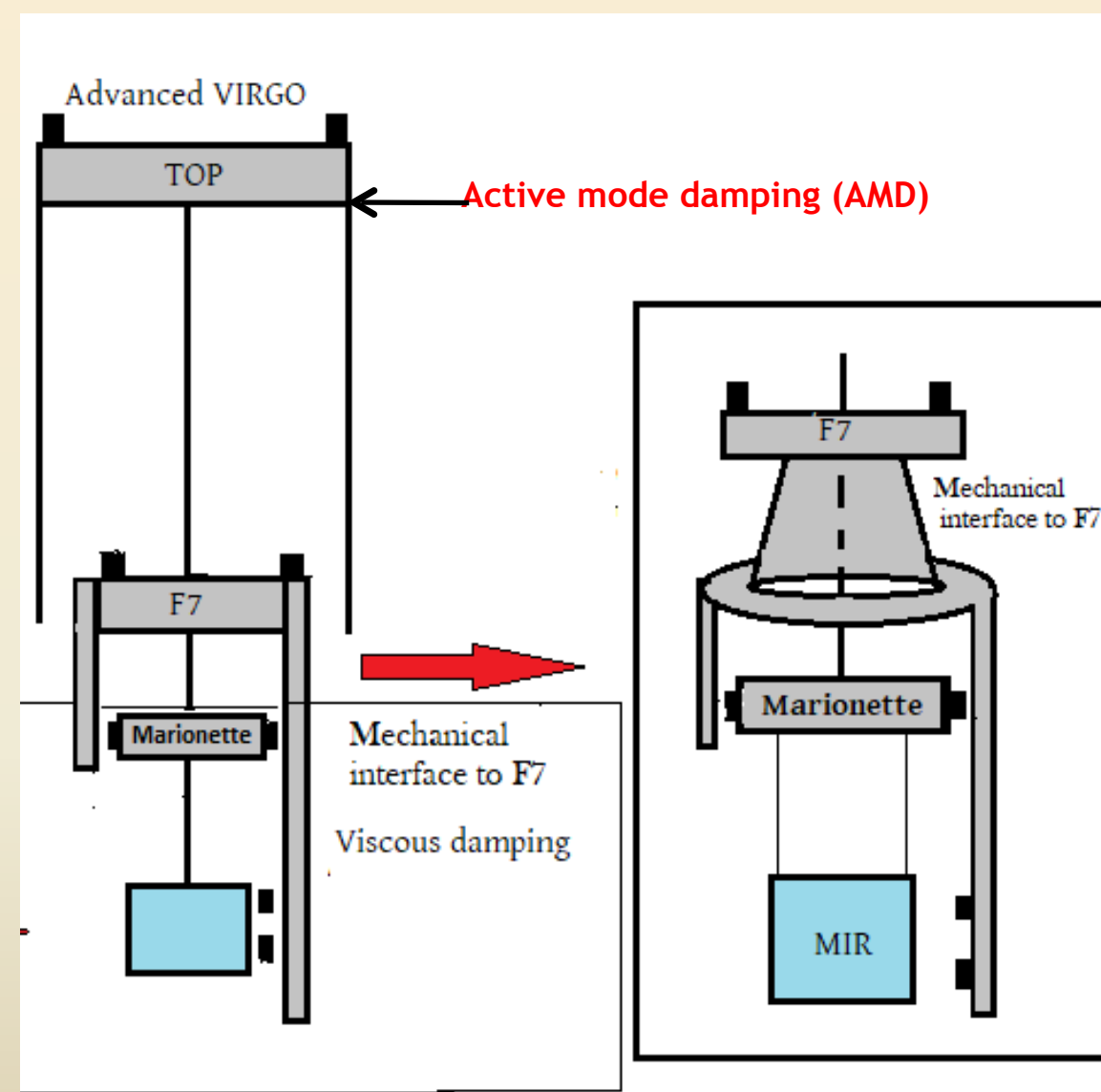
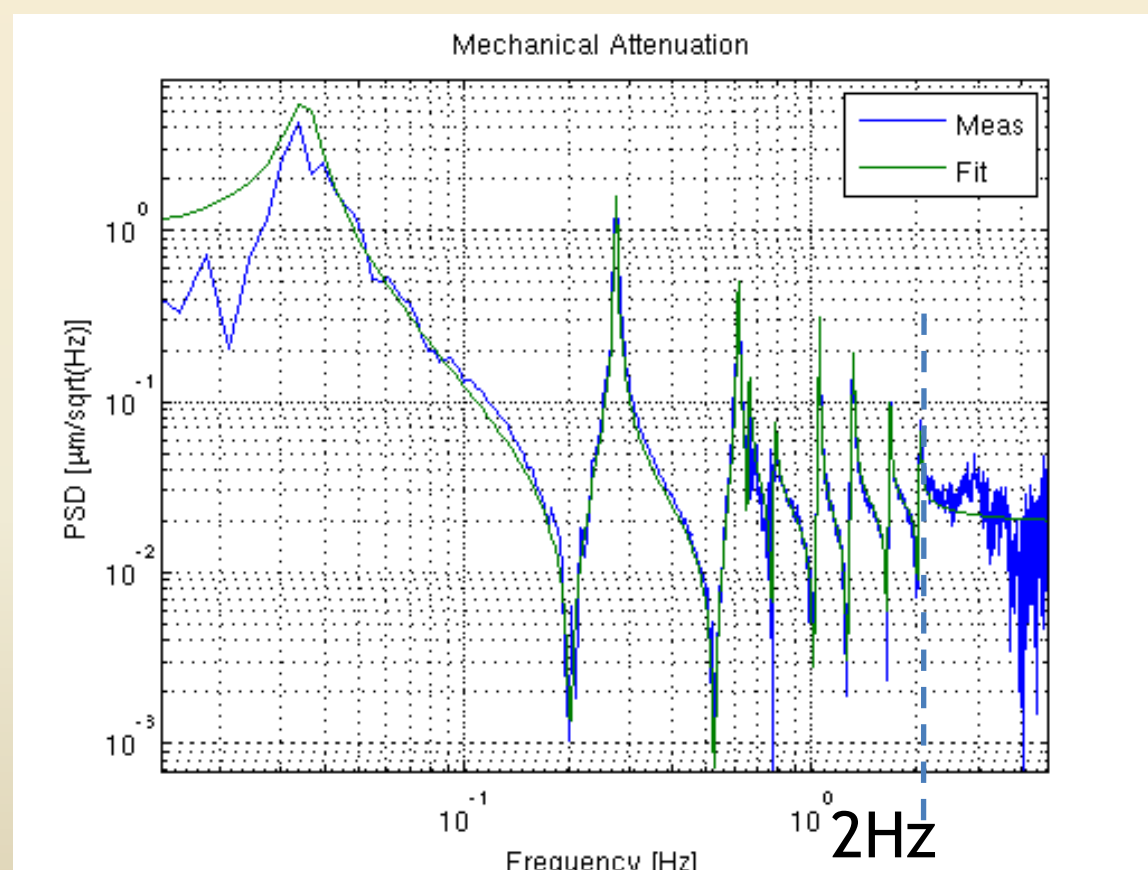
- Blending technique

- Above 100 mHz
 - Below 100 mHz
 - GIPC Control

- Suspension control Noise

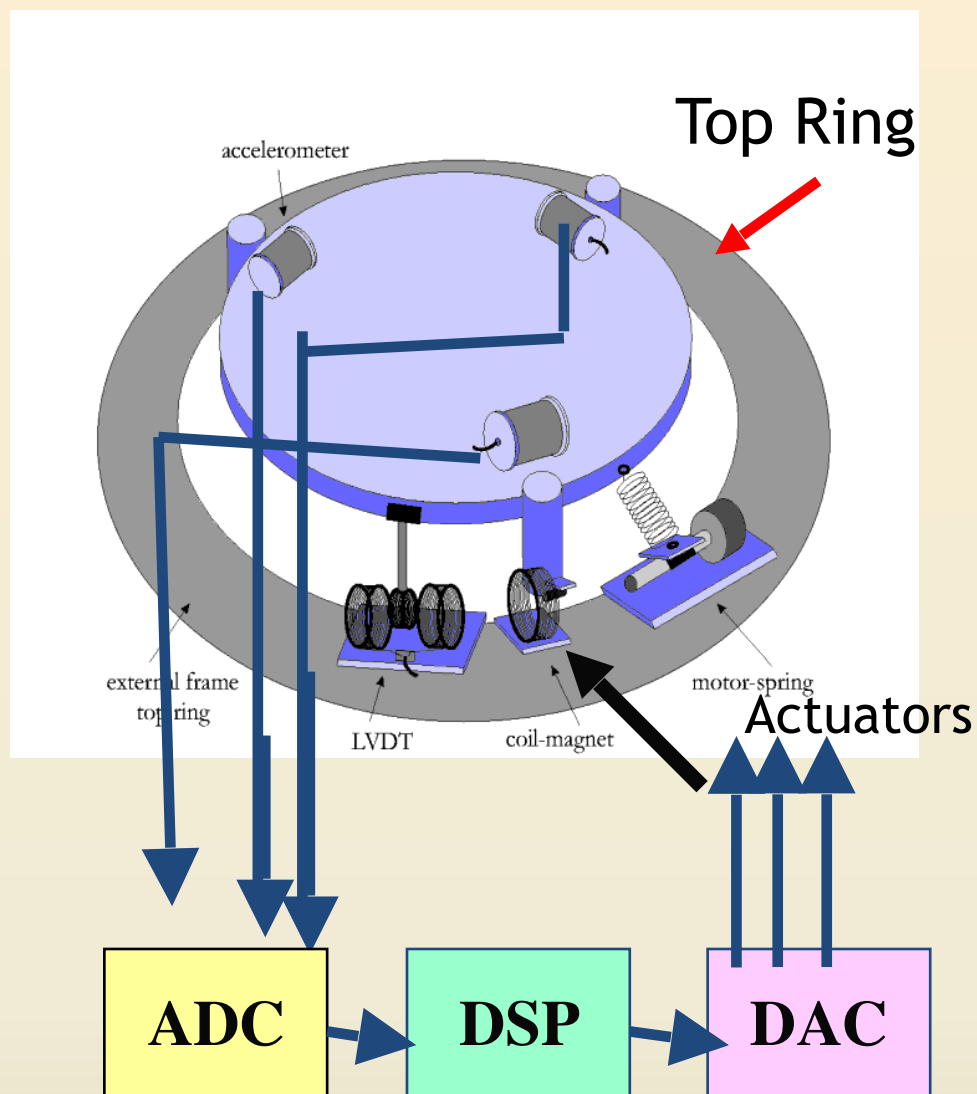
By using sensors and actuators a **hierarchical feedback control** system has been implemented in four different points: on **top of the suspension**, on the **Filter7, Marionette stage and on the Mirror**. The goal of the feedback action is to reduce the swinging of the free falling masses.

- 18 position sensors (LVDT)
- 5 inertial sensors (ACC under digital control)
- 23 magnetic actuators (coils)



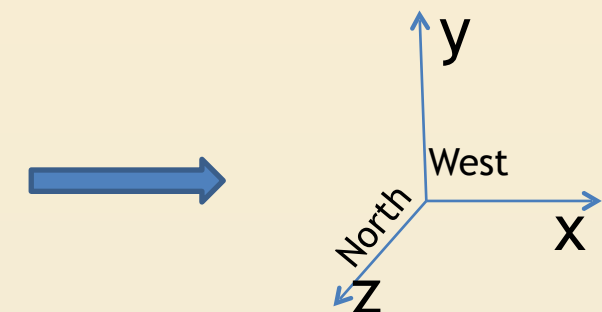
Suspension control: *IP control*

On the Superattenuator (SA) top ring a set of sensors and actuators are installed for feedback control purpose.



At this level is implemented an Active Mode Damping (AMD) of the SA resonance modes for seismic noise reduction.

➤ To implement the AMD control we diagonalize sensors in **Virgo reference frame**



For the horizontal translation we have (where $i = z, x; j = x, z;$):

$$\text{LVDT: } \hat{s}_{iL}(\omega) = \hat{s}_i(\omega) - \hat{s}_{iLs}(\omega) + \hat{n}_{iLe}(\omega)$$

$\hat{s}_{iLs}(\omega)$ is the seismic contribution $\hat{n}_{iLe}(\omega)$ is the electronic noise contribution

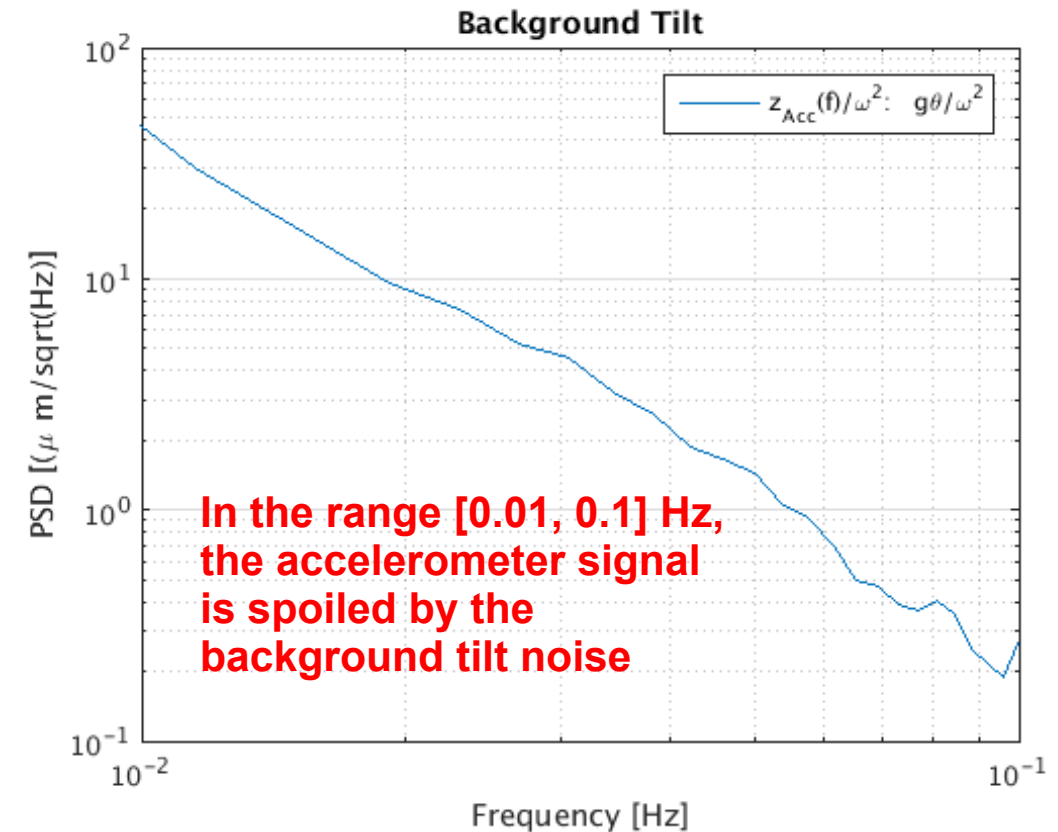
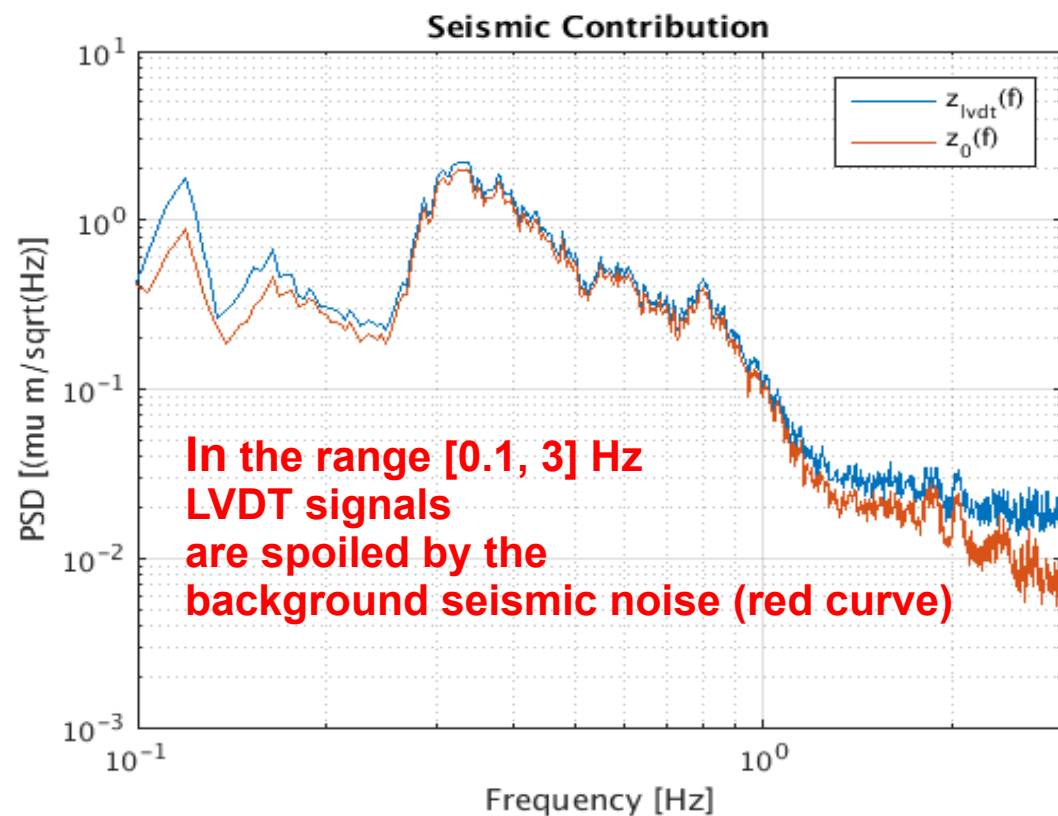
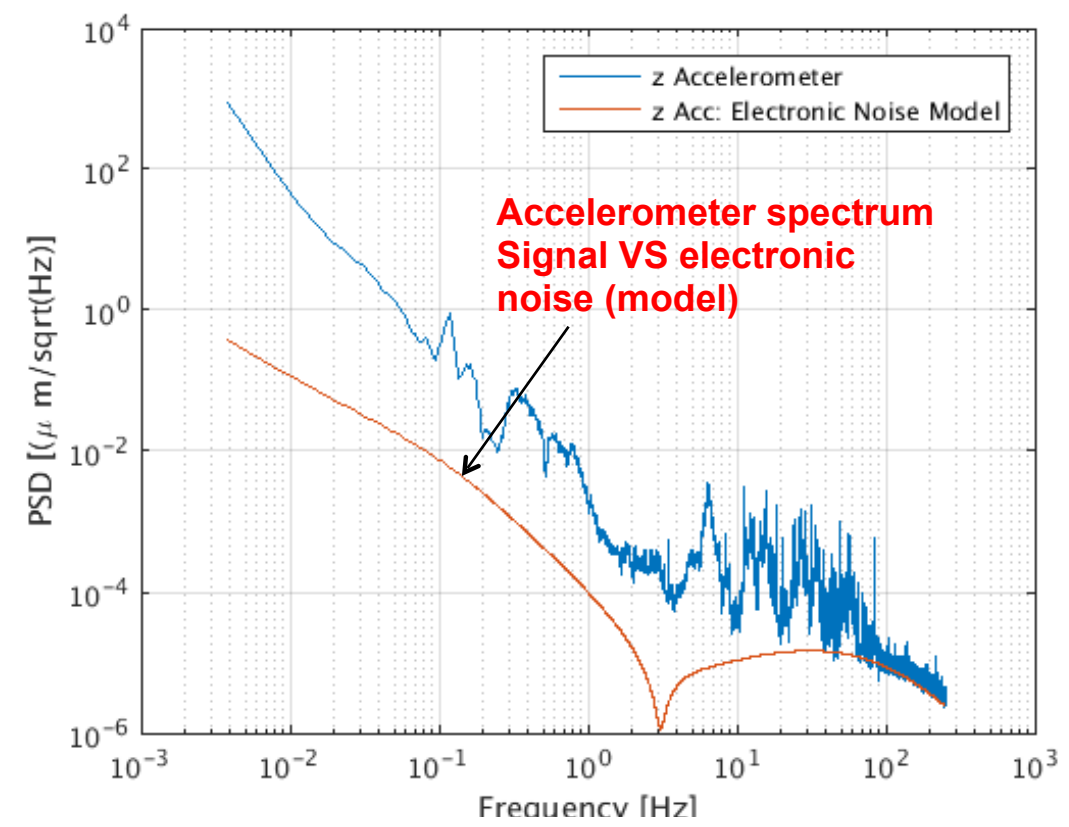
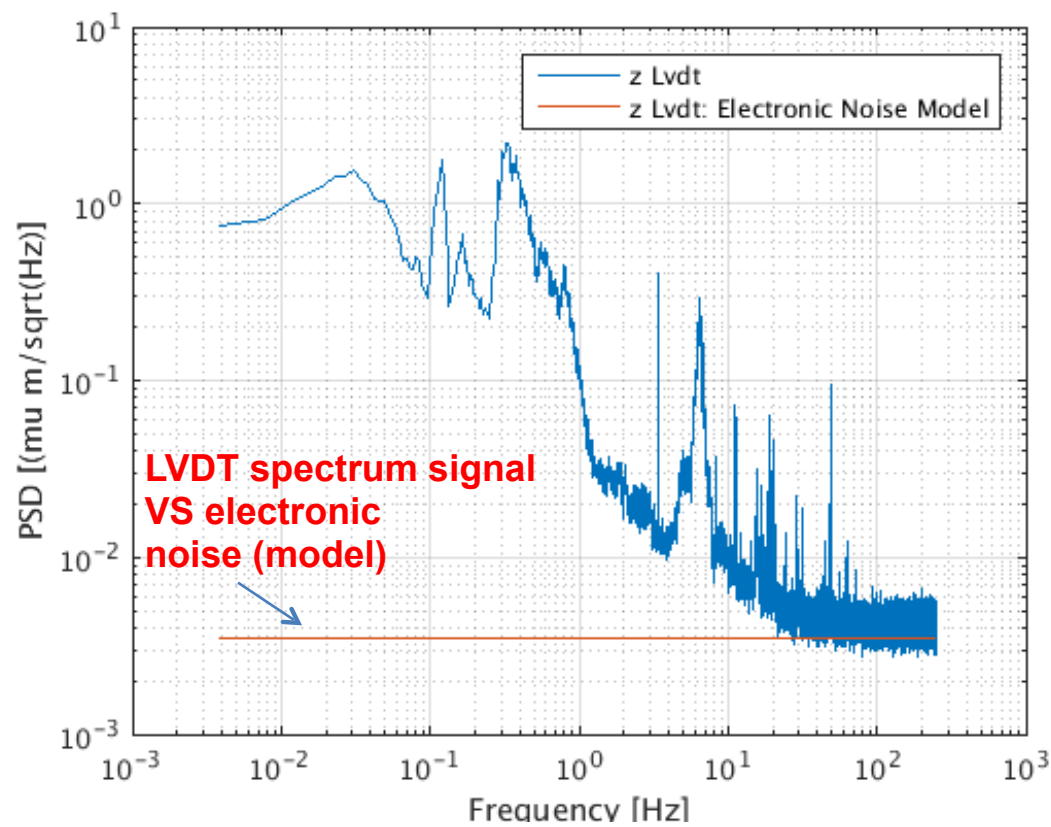
$$\text{ACC: } \hat{a}_{iA}(\omega) = \hat{a}_i(\omega) - g \cdot \hat{\theta}_j(\omega) + \hat{n}_{iAe}(\omega)$$

$\hat{n}_{iAe}(\omega)$ is the electronic noise contribution

$g \cdot \hat{\theta}_j(\omega)$ is the background tilt contribution

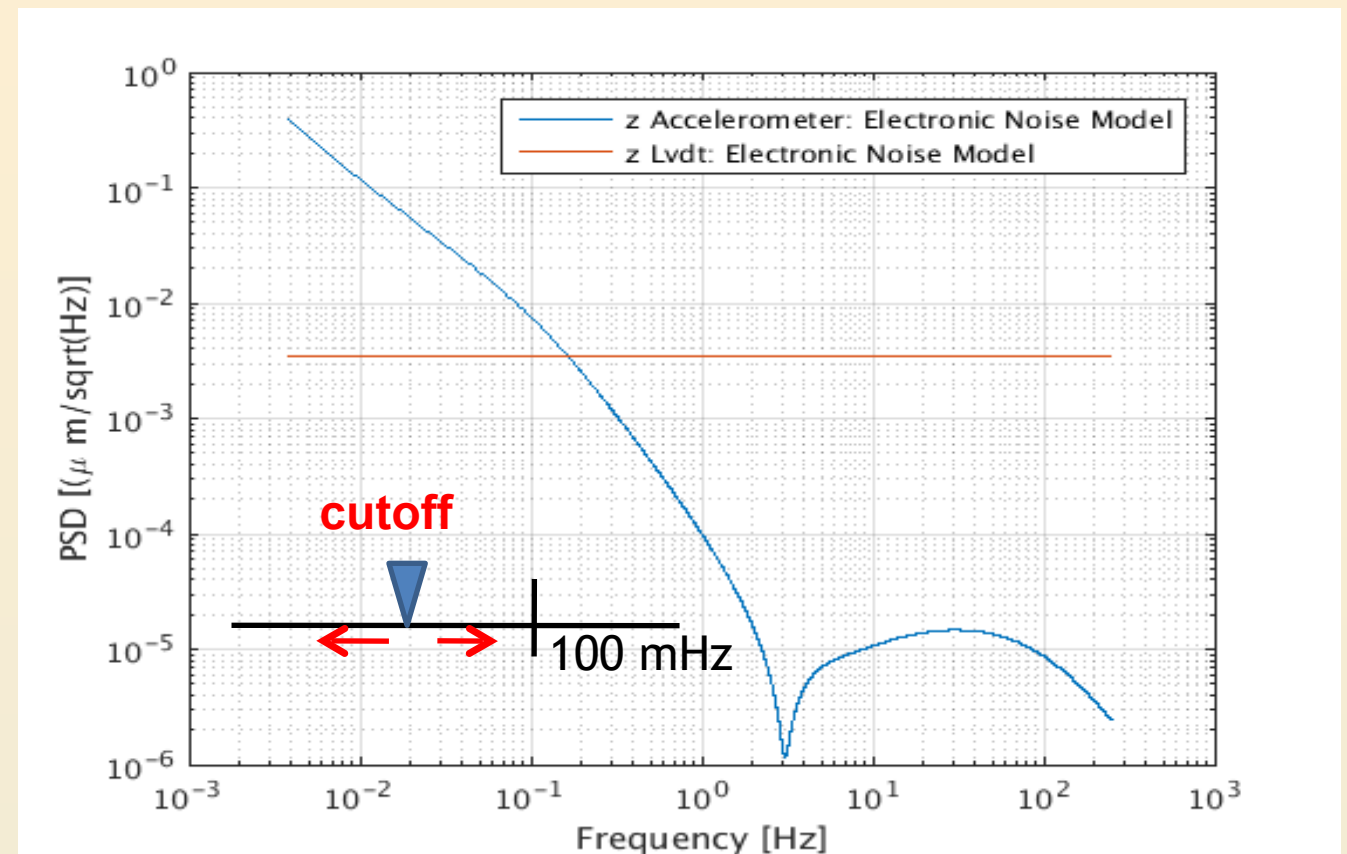
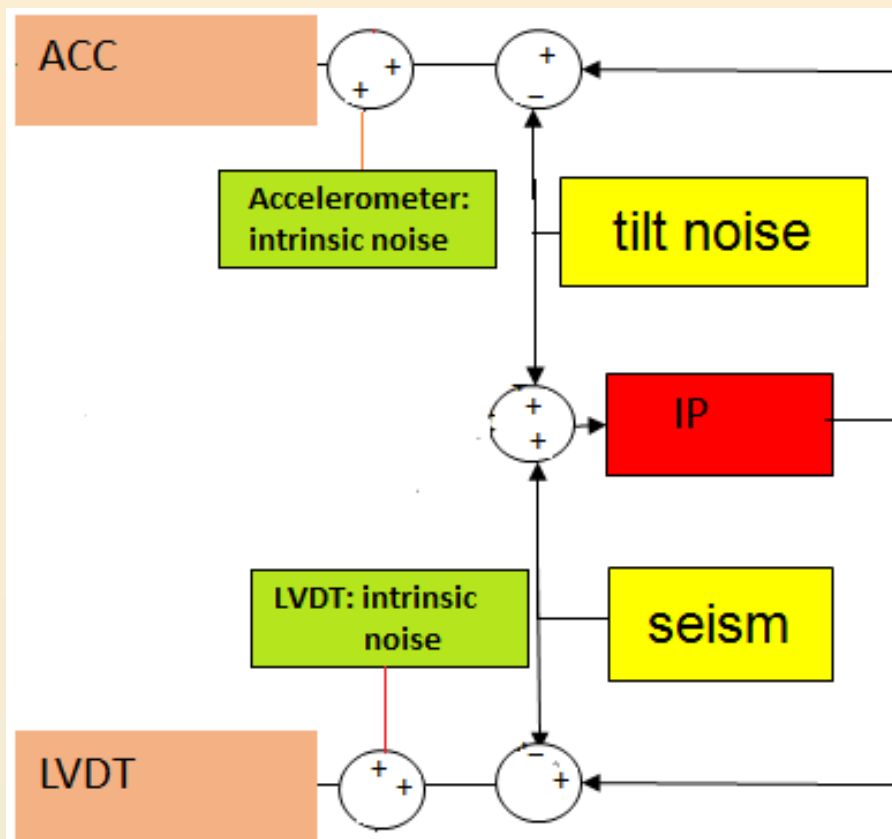
Active Mode Damping: *noise of sensors*

Let's consider the virtual sensors along z axis



VIRGO Active Mode Damping: *the Blended Virtual Sensor (BVS)*

To take the better part of both signals in Virgo a *blended virtual sensing signals*,
Is obtained through neutral prefiltering.



At low frequencies we are limited by
accelerometer electronic noise



High Pass filter (HP)

$$\hat{HP}(\omega) + \hat{LP}(\omega) = 1$$

Low Pass filter (LP)



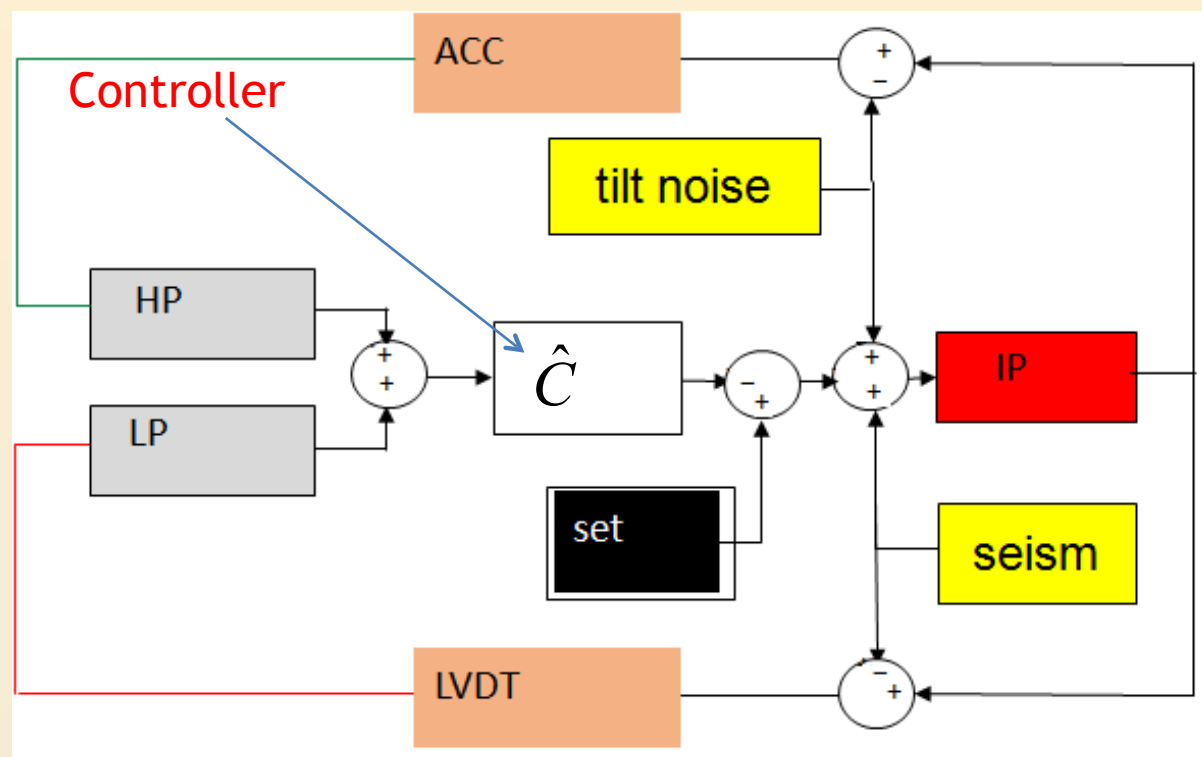
✓LP filter must be shaped taking into account the background disturbance

✓For LP filter typical cutoff is below 100 mHz

For z d.o.f the BVS signal is :

$$\hat{S}_{zv}(\omega) = \hat{LP}(\omega) \cdot \hat{s}_{zL}(\omega) - \omega^{-2} \cdot \hat{HP}(\omega) \cdot \hat{a}_{zA}(\omega)$$

Inertial Damping: *block diagram*

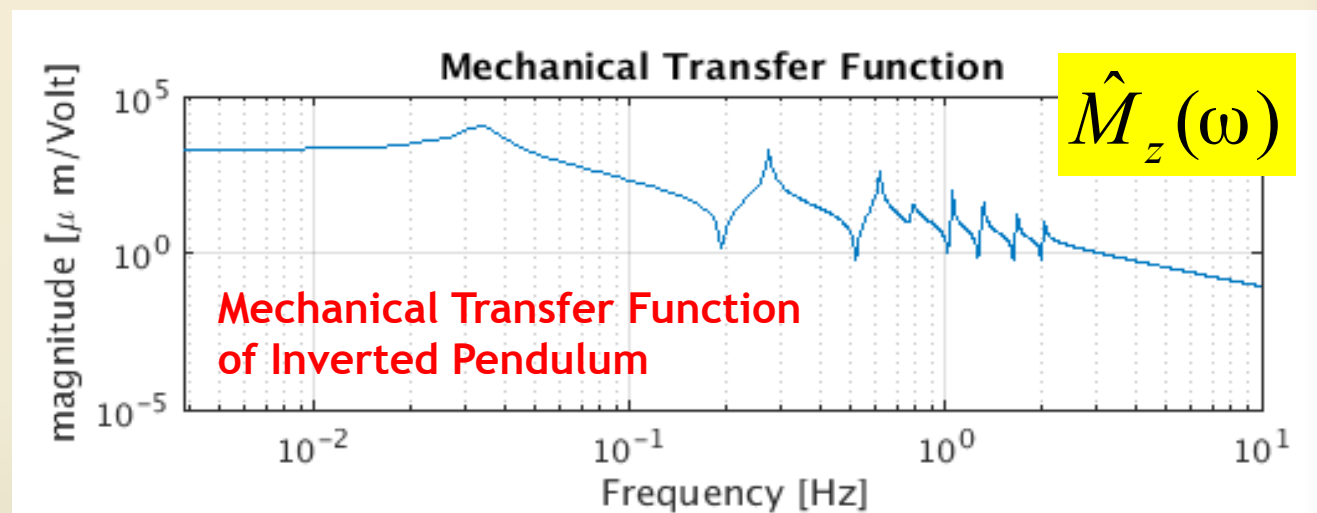


Block Diagram of Active mode Damping control used in Virgo

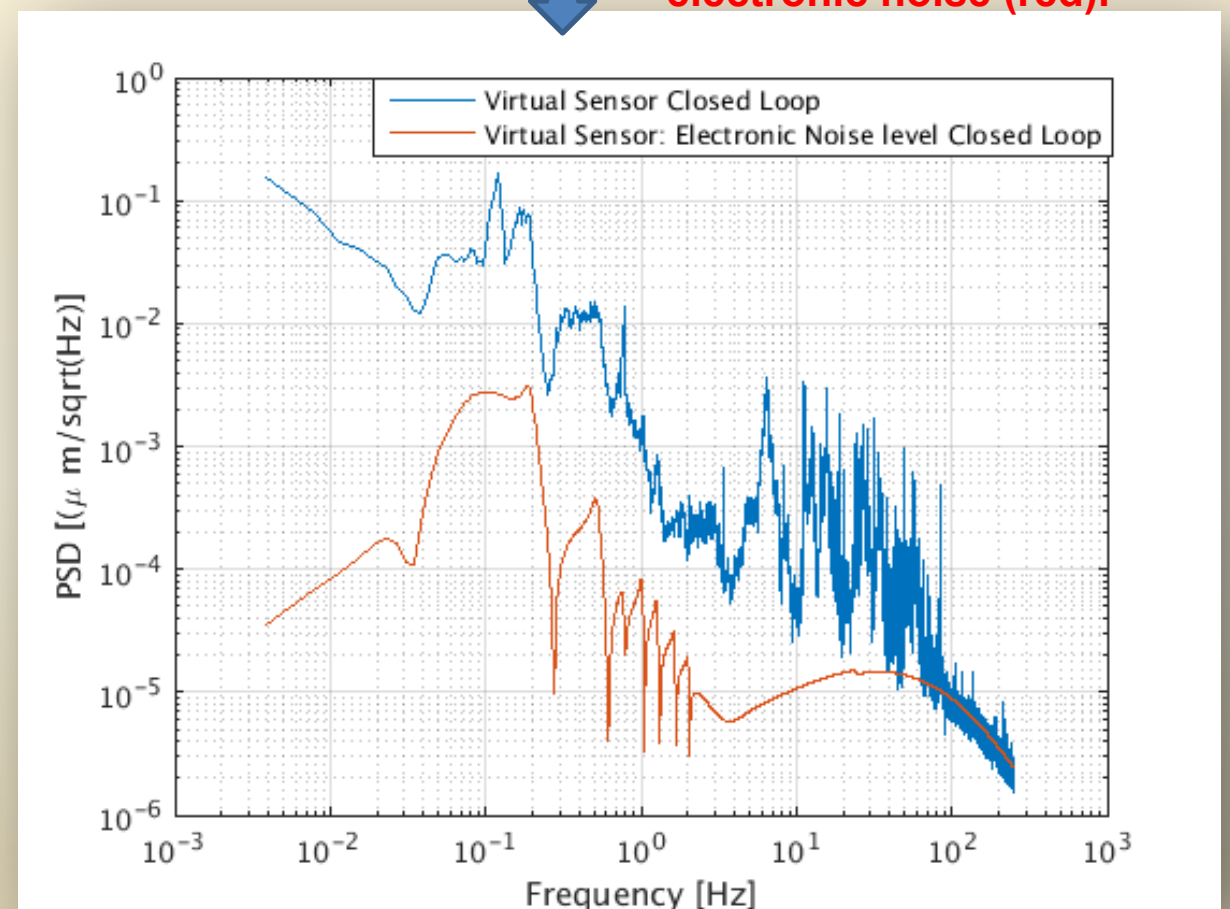
The closed loop signal along the i-th d.o.f is

$$\hat{S}_{iv}^{CL}(\omega) = \frac{\hat{S}_{iv}(\omega)}{1 - \hat{M}(\omega) \cdot \hat{C}(\omega)}$$

Virtual sensor closed loop, compared with its electronic noise (red).



In ideal condition, this spectrum should reach the electronic noise level

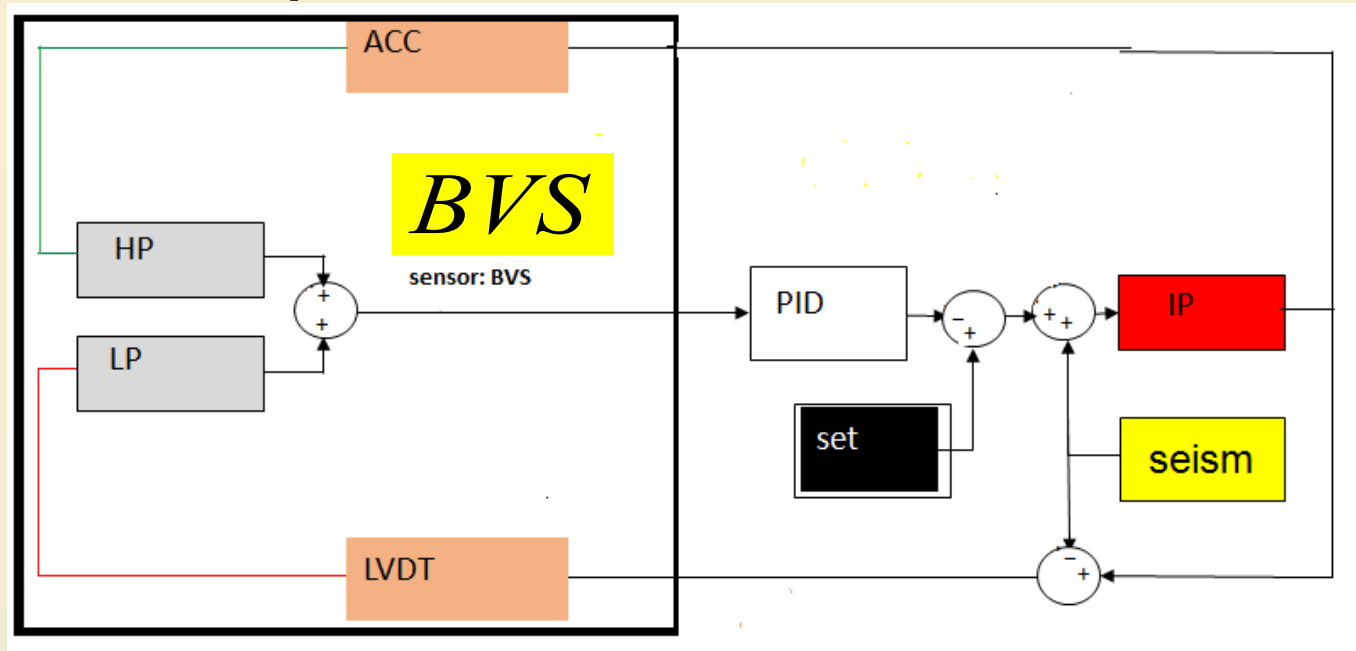


We have an excess of seismic noise in the region [0.1, 1]Hz!!!

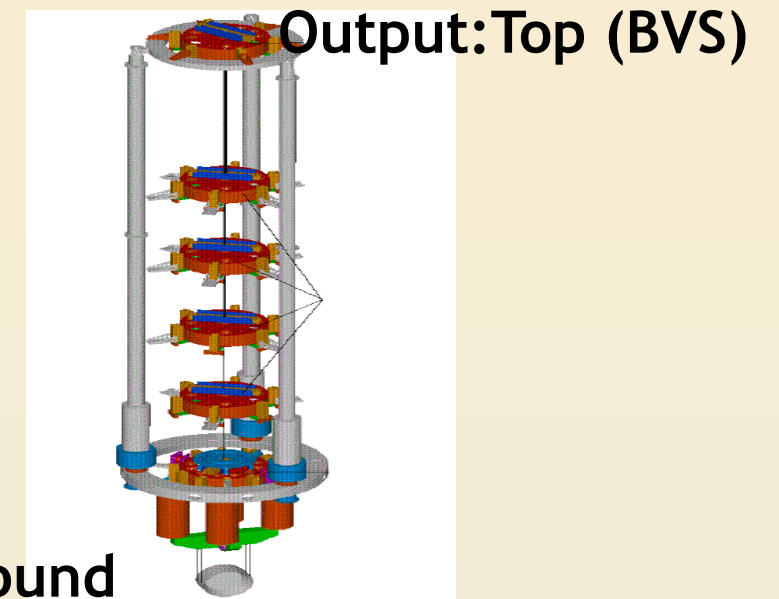
Blending technique: above 100 mHz

Above 100 mHz the main source of noise contaminating the BVS sensor, is the seismic noise: $[0.100 \div 3]\text{Hz}$.

To shape the LP filter and to tune the blending frequency we need to know the effective closed loop transfer function:



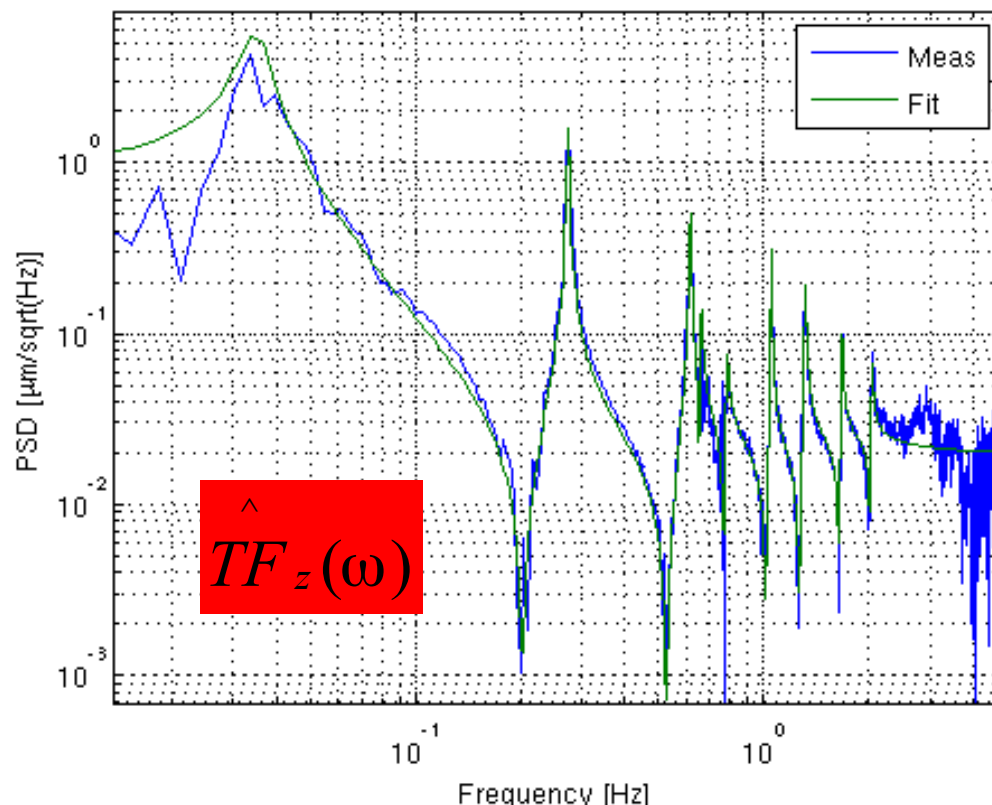
$$\hat{TF}_{eff}^{CL}(\omega) \approx \hat{TF}_{mecc}^{CL}(\omega) + \hat{TF}_{sens}^{CL}(\omega)$$



Input:ground

Output:Top (BVS)

Mechanical Attenuation



➤ Mechanical Contribution ➤ Sensing contribution

$$\hat{A}(\omega) = \frac{\hat{TF}_z(\omega)}{1 - \hat{M}_z(\omega) \cdot \hat{C}_z(\omega)}$$

$$\hat{B}(\omega) = -\frac{\hat{LP}(\omega) \cdot \hat{M}_z(\omega) \cdot \hat{C}_z(\omega)}{1 - \hat{M}_z(\omega) \cdot \hat{C}_z(\omega)}$$

$$\hat{s}_{zTOP}^{CL}(\omega) \approx [\hat{A}(\omega) + \hat{B}(\omega)] \cdot \hat{s}_{zLS}(\omega)$$

Blending technique: above 100 mHz

✓ Mechanical contribution (A) composed by

- The mechanical TF
- The corrector filter
- The mechanical attenuation

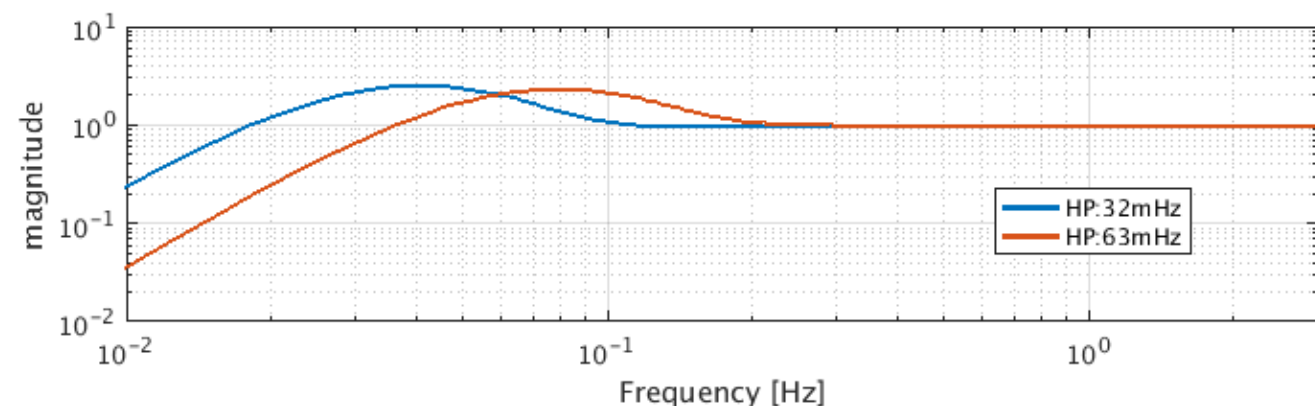
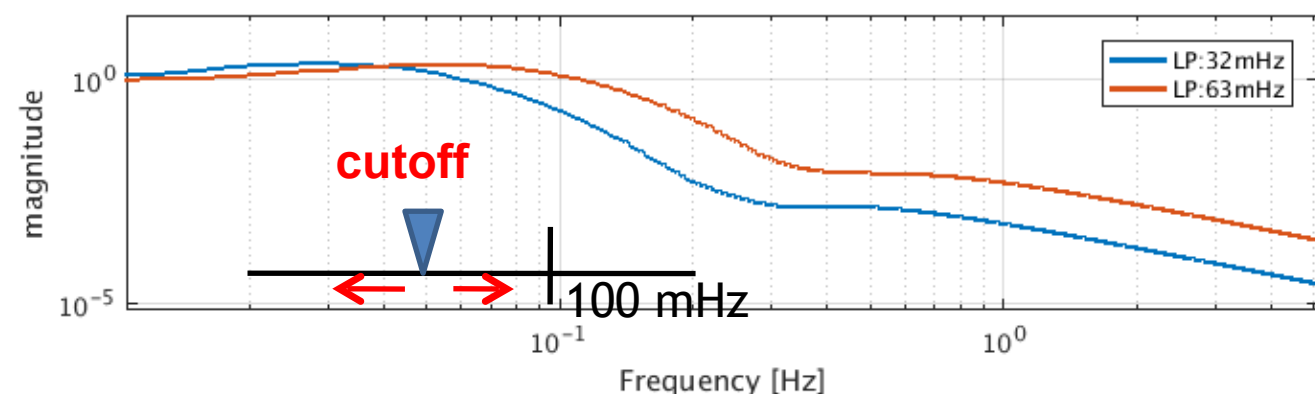
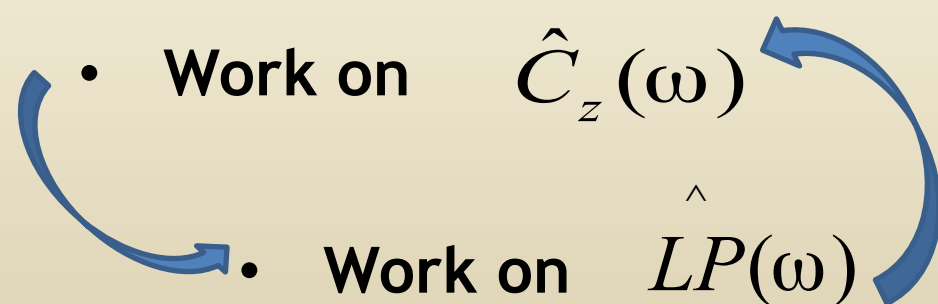
✓ Sensing contribution (B) composed by

- The mechanical TF
- The corrector filter
- Low Pass pre-filtering

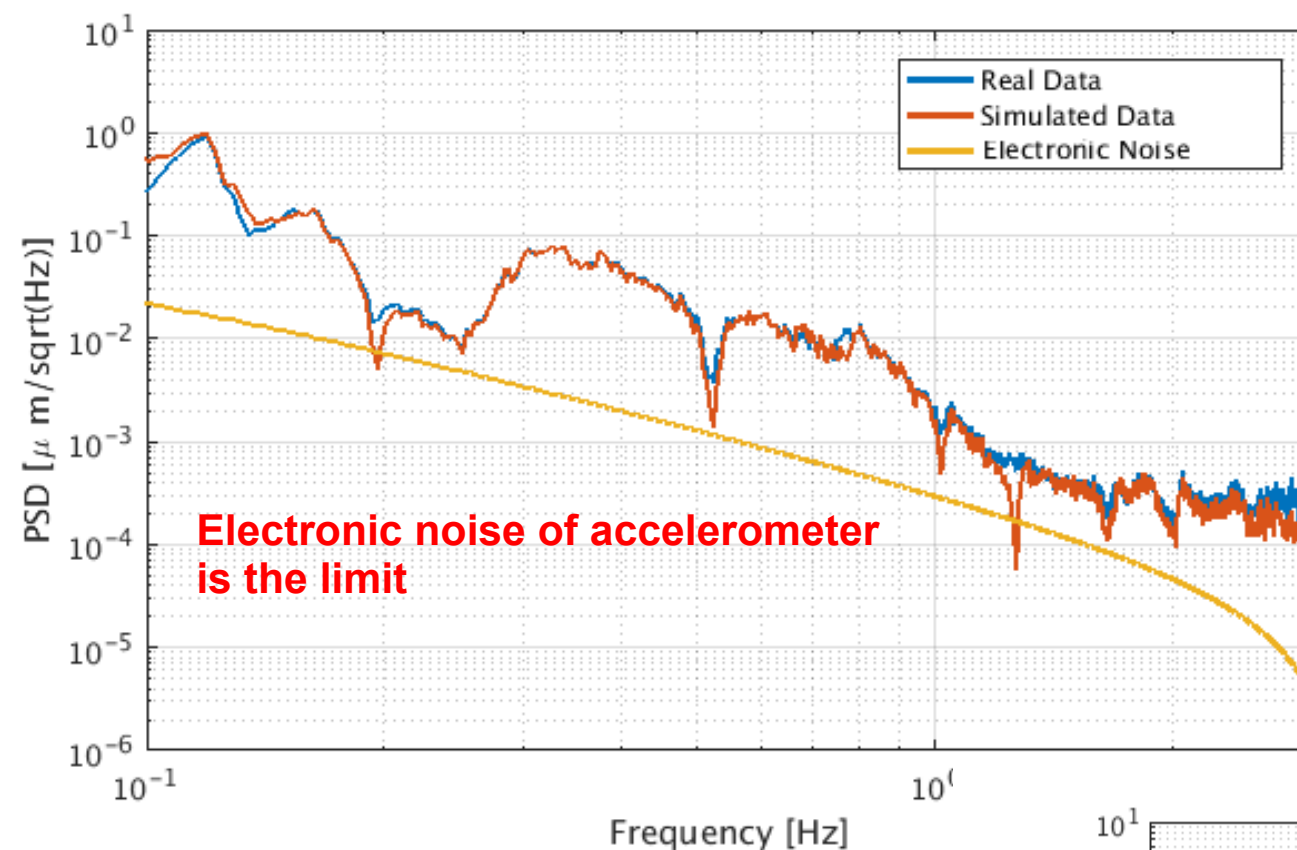
➤ A and B are two available handles to optimize the blending strategy

1) design preliminary corrector and a simple blending

2) Measure $\hat{TF}_z(\omega)$



➤ STEP 1 Real Data Simulation



➤ STEP 2 low pass tuning

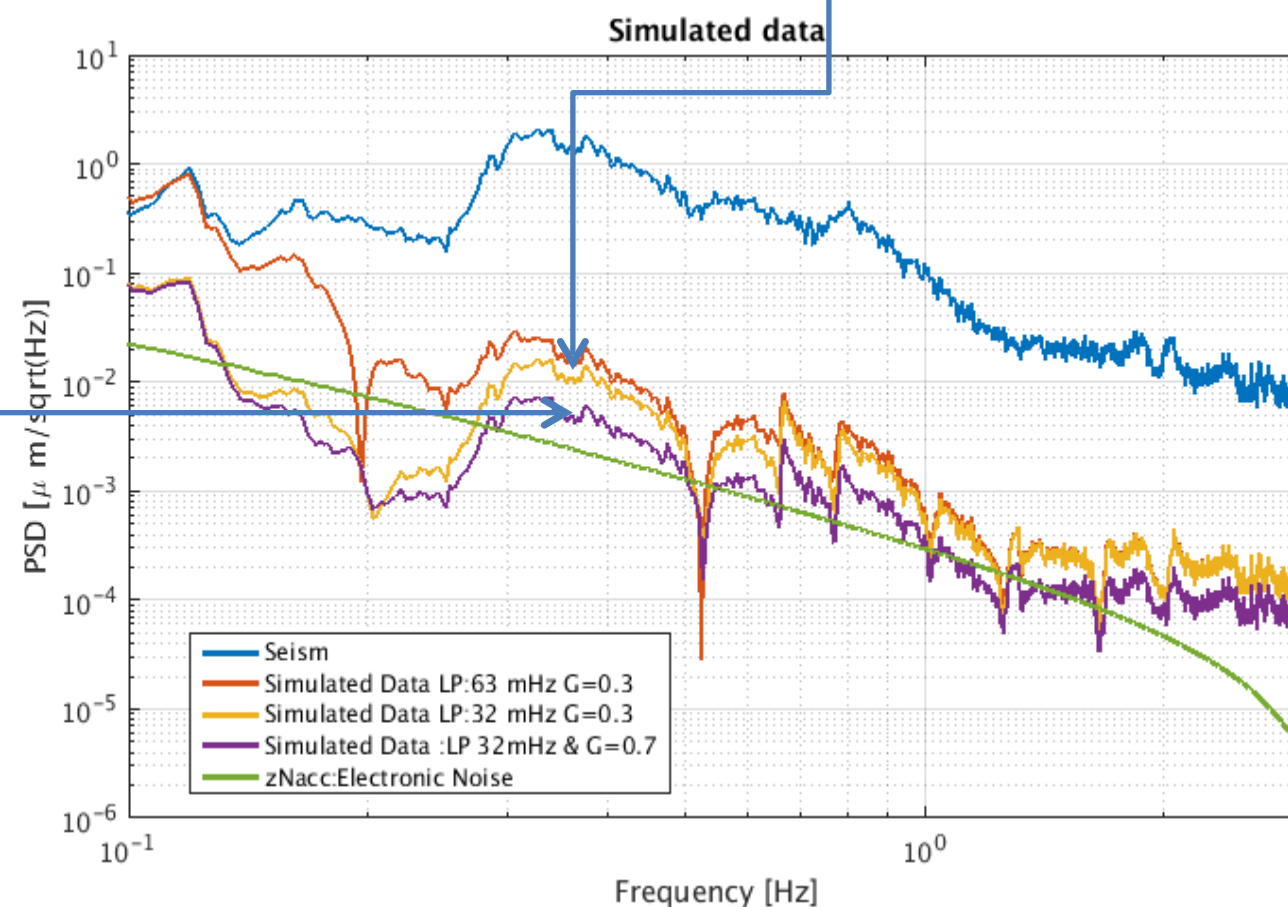
Tune LP (shape, blending frequency, etc.)

to change $\hat{B}(\omega)$

➤ STEP 3 corrector filter tuning

Tune $\hat{C}(\omega)$

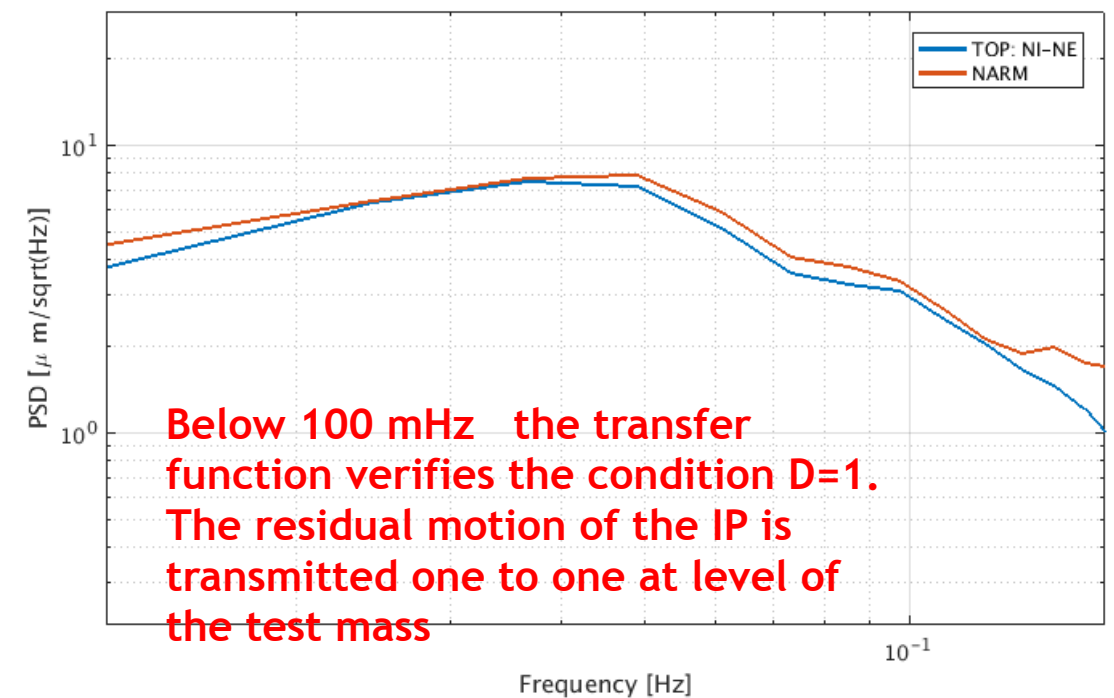
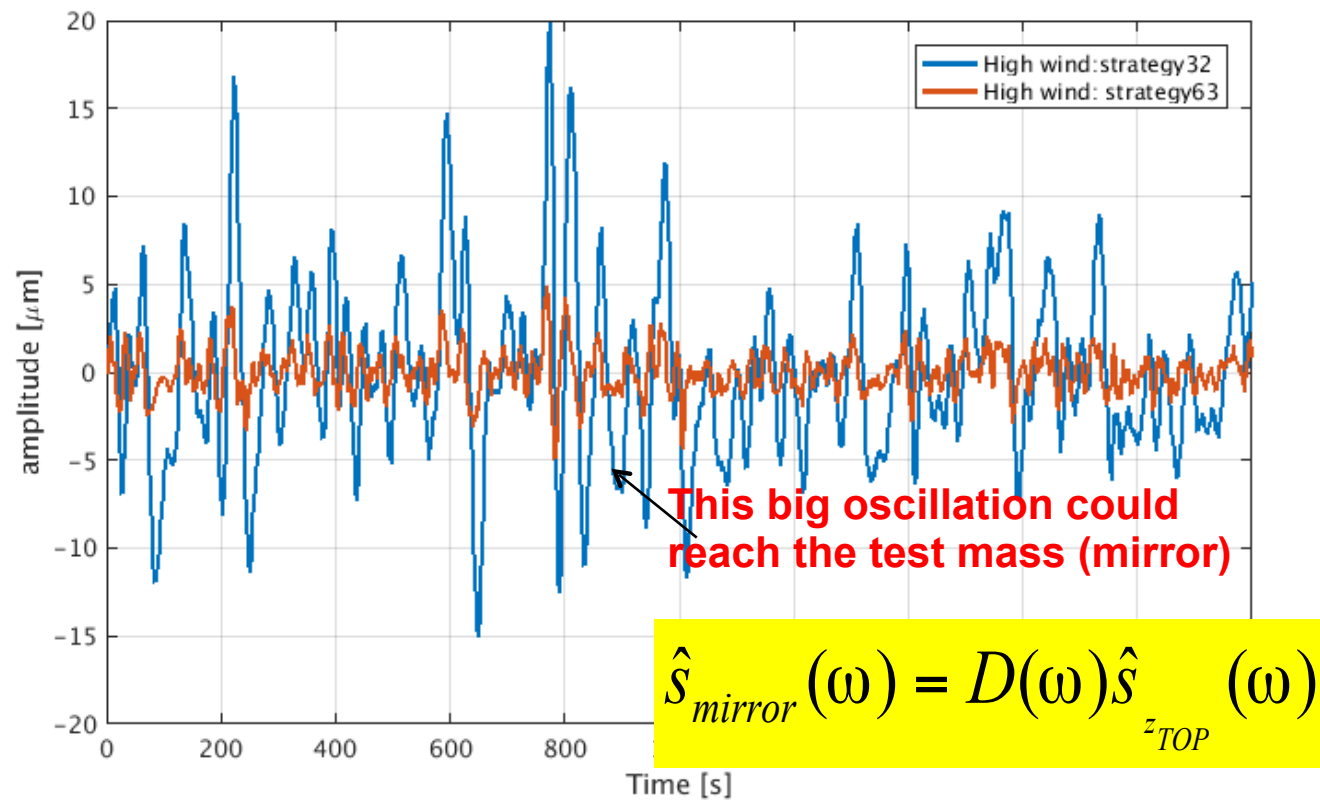
to change $\hat{A}(\omega)$



Below 100 mHz the noise of the accelerometer is dominant.

It is possible to quantify the re-injected accelerometer noise by defining the ratio of the HP filters:

$$r(\omega) = \frac{\hat{HP}'(\omega)}{\hat{HP}(\omega)} \Rightarrow \hat{s}_{z_{TOP}}'(\omega) = r(\omega) \hat{s}_{z_{TOP}}(\omega)$$



It is possible to study the impact of several strategies on the mirror motion and on the locking correction signal by using $r(\omega)$:

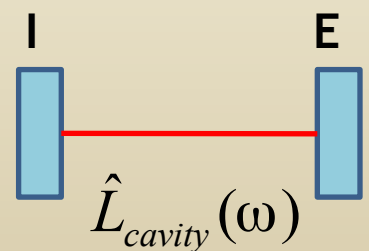
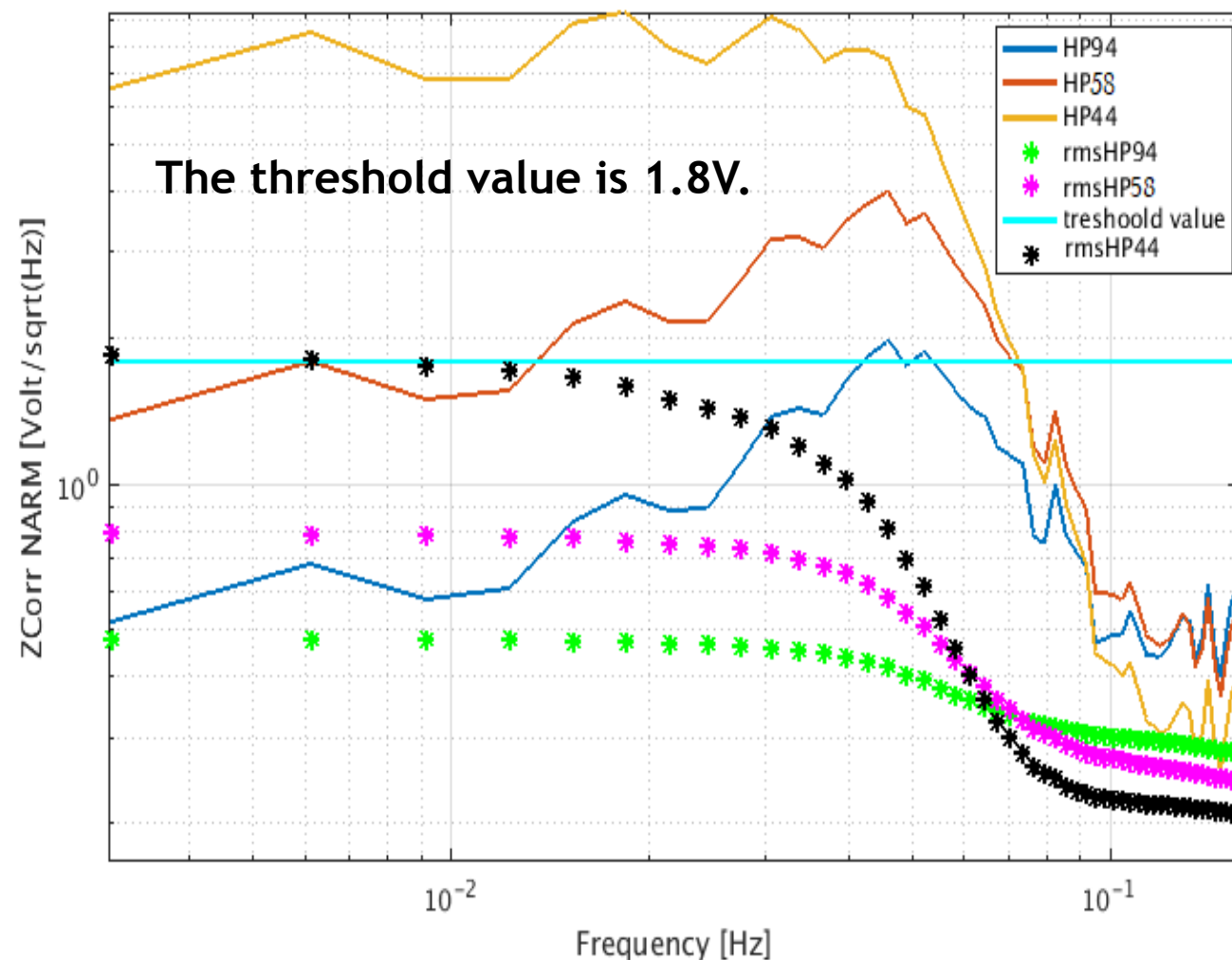


Diagram showing a cavity with mirrors I and E. The cavity length is labeled $\hat{L}_{cavity}(\omega)$. The equation for the cavity length is: $\hat{L}_{cavity} = c \cdot \hat{s}_{z_{Lock}} = \sqrt{(\hat{s}_{z_{TOP}}^I)^2 + (\hat{s}_{z_{TOP}}^E)^2}$.

Blending technique: below 100 mHz



We applied r on the locking correction signal to see which blending strategy makes it saturated.

The locking correction increases when moving the blending frequency from 94 mHz to 44 mHz. The rms of signal computed by applying the blending strategy with blending frequency at 44mHz (black star), in the range 10÷30mHz, is very close to the threshold value.

The chosen compromise for the scientific run O2 was the strategy63 because it stays below the threshold value in a large part of the environmental conditions.

Global Inverted Pendulum Control: GIPC

The tuning of the blending frequency is a “compromise”, to minimize at the same time the re-injection of seismic noise above 100 mHz and the disturbances due to the use of inertial sensors below 100 mHz.

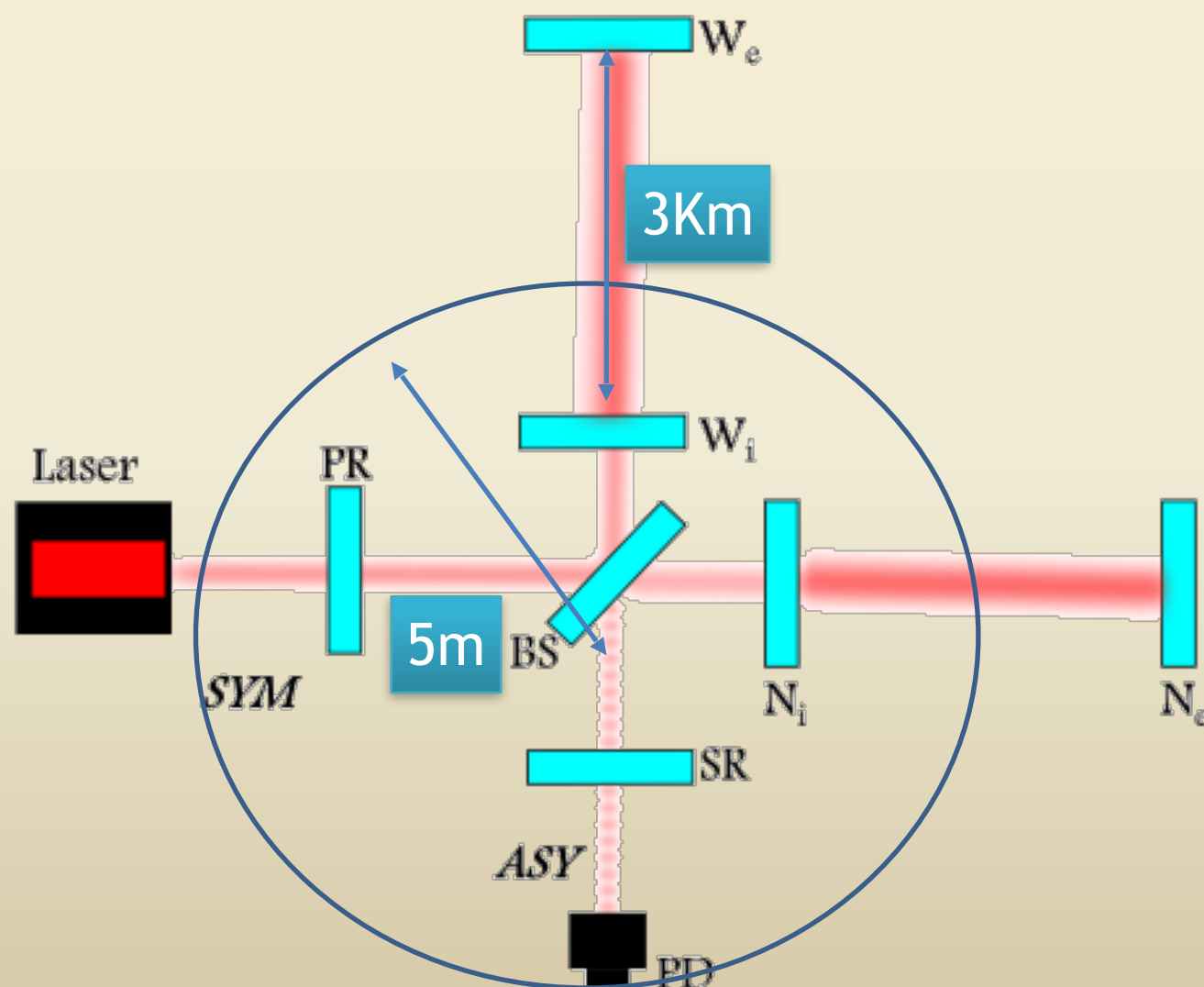
To apply a blending strategy with very low blending frequency we move to a different control scheme: Global Inverted Pendulum Control (GIPC).

Base changing: the translational coordinates of the different IP are mixed in order to build two common coordinates (one for X and one of Z), and many differential coordinates

the diagonalized LVDT sensors see, along the i -th direction, coherent seismic contributions.

Central area:

Not in scale!



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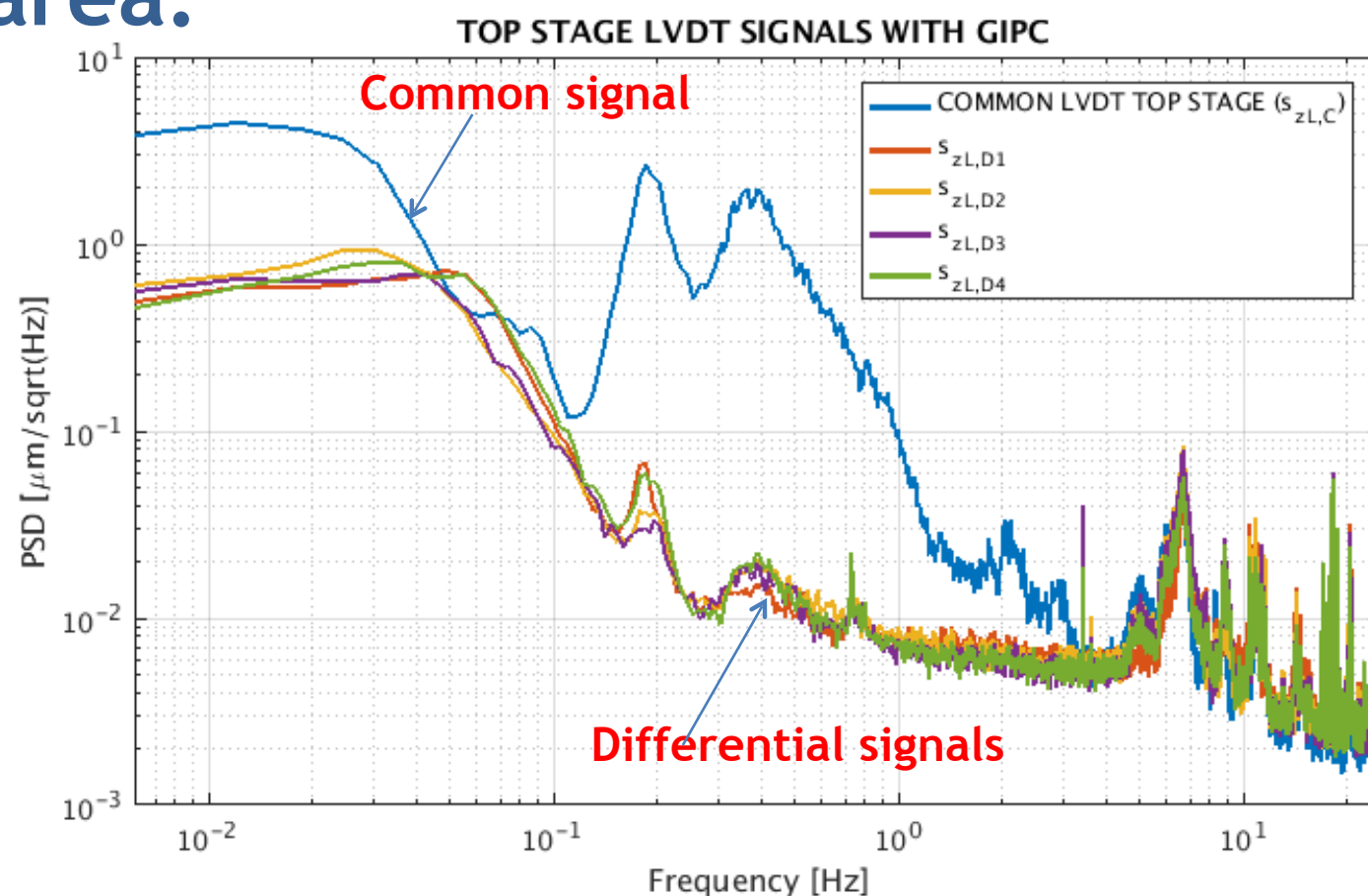
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Central
area:

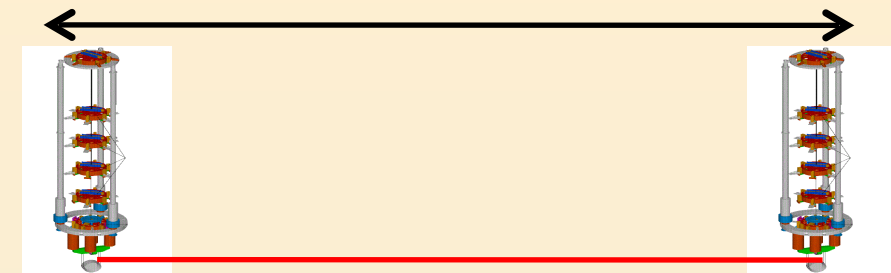
the diagonalized LVDT sensors see, along the i -th direction, coherent seismic contributions.



To clean the common signal from the seismic component we can use a blending strategy at 32mHz (without spoiling the locking signal of the interferometer).

We can apply a strategy at 63mHz on the differential signals because these not introduce seismic contribution

For the cavity the situation is different: we have two IPs located at 3 Km from the central area



The seismic contributions contaminating the LVDT of End and Input suspensions are uncorrelated and, consequently, the recombination adopted for the central area is not effective.

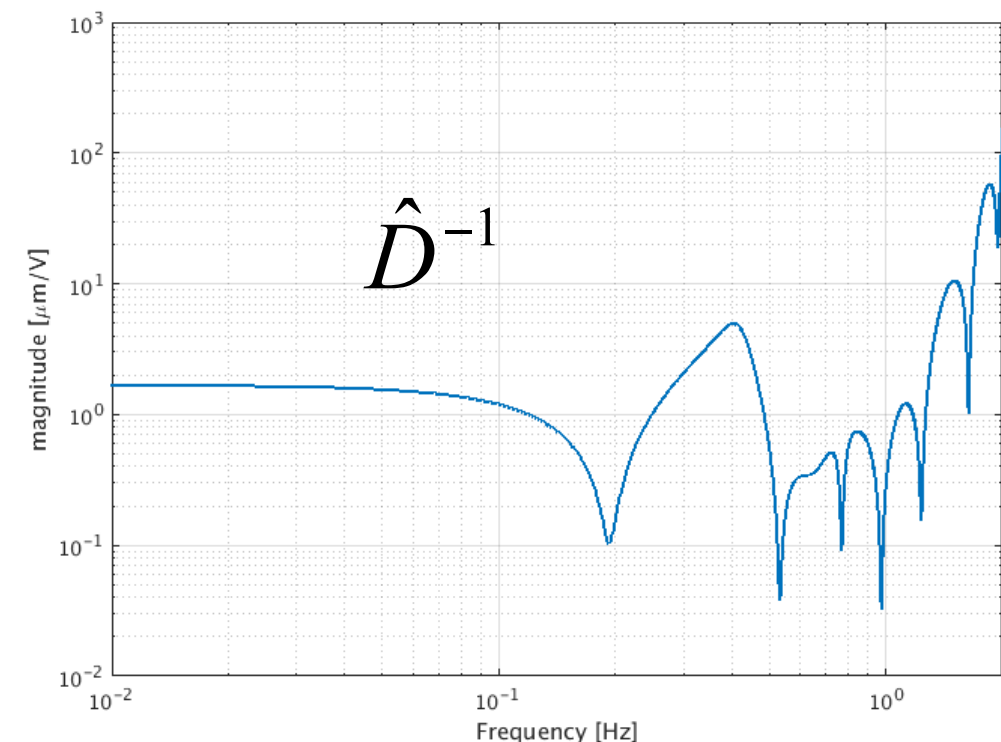
We need an additional differential signal equivalent to the LVDT:

The signal monitoring the elongation of the cavity ΔL

From the top to the bottom there are 8 stages of attenuation
To correctly implement the GIPC control the signal must be treated in order to become equivalent to the LVDT

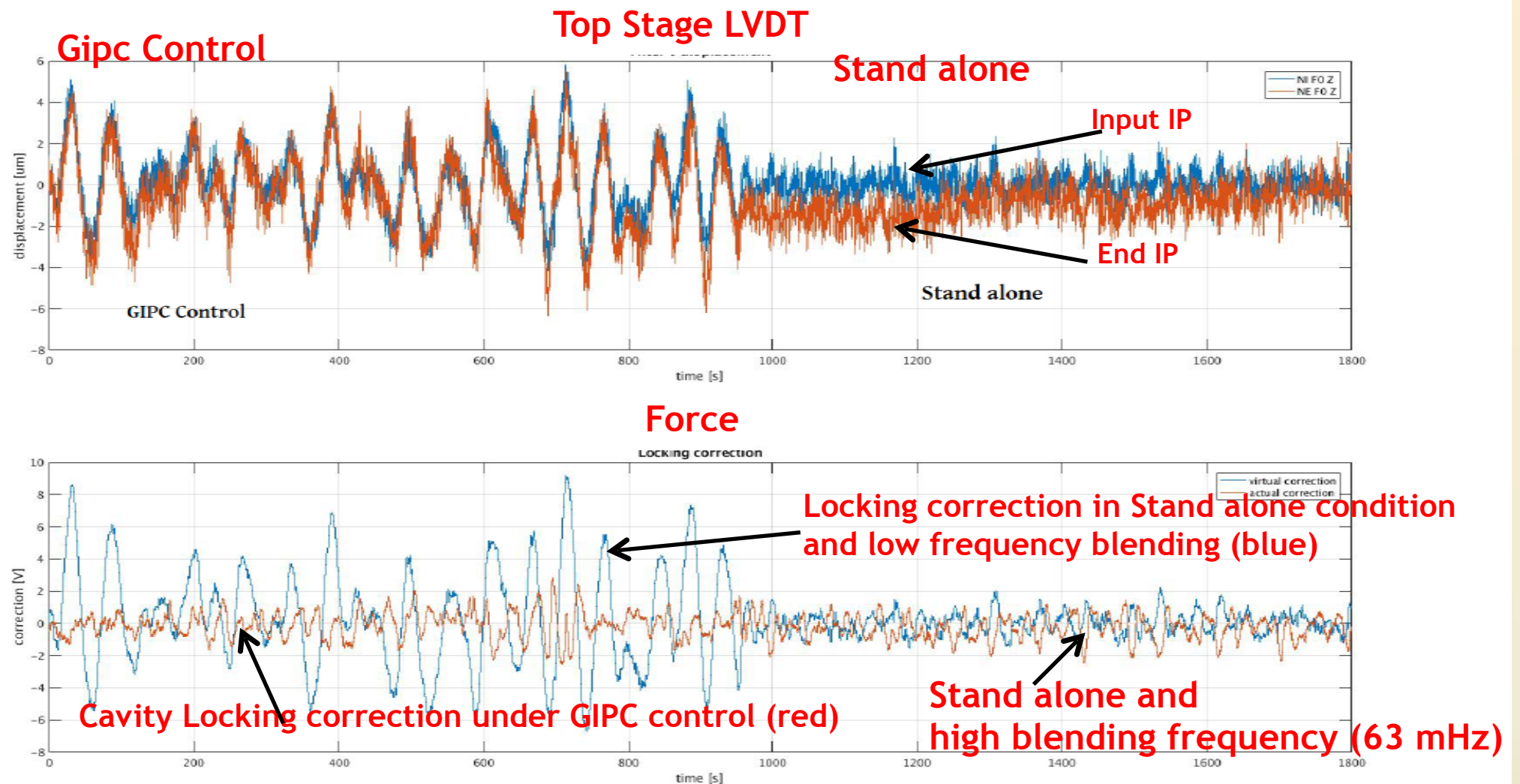
$$L_{vdt}^{end} \approx \hat{D}^{-1} \cdot \Delta L$$

D is the transfer function between top stage (input) to mirror (output)



Blending technique (very low blending frequency)

On the
cavity



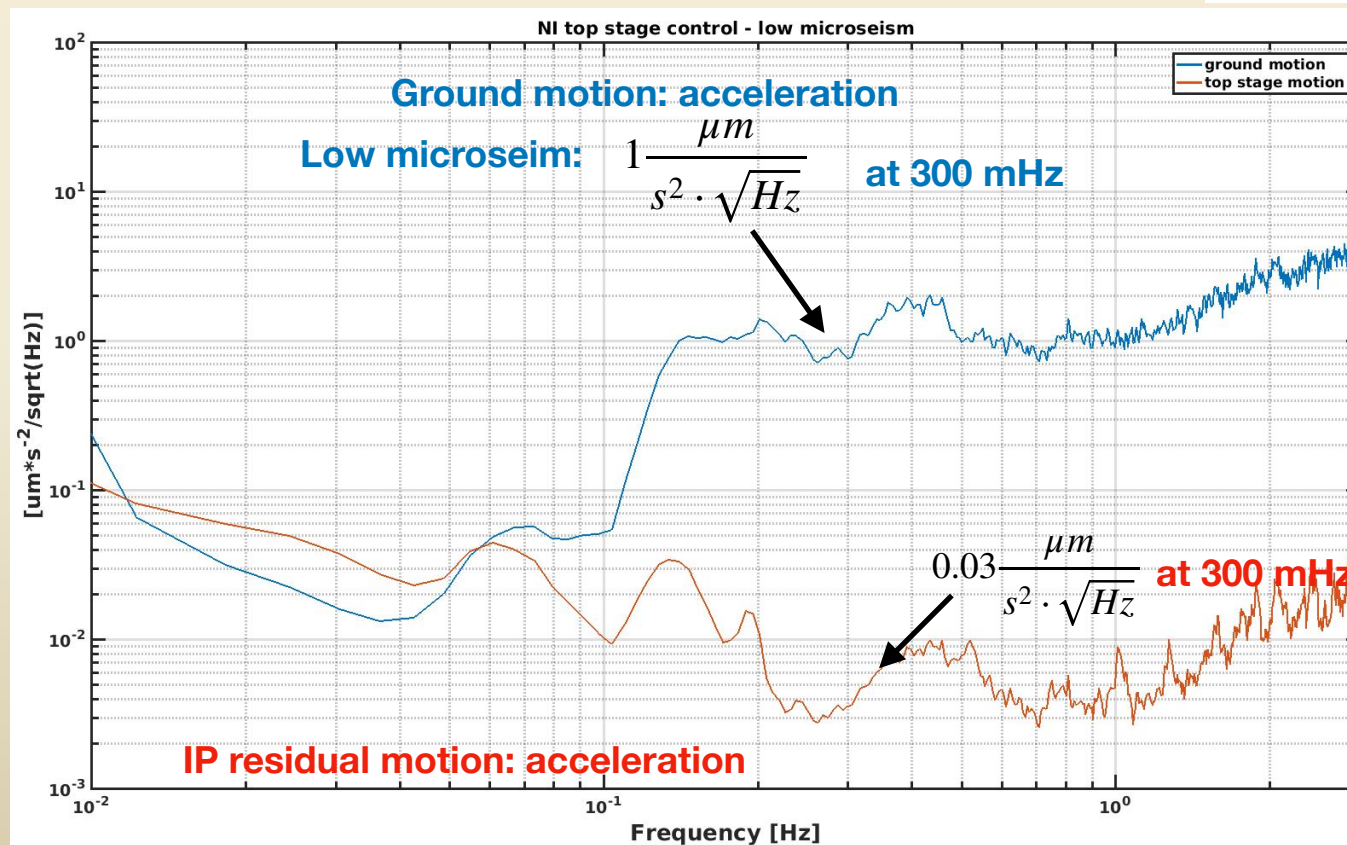
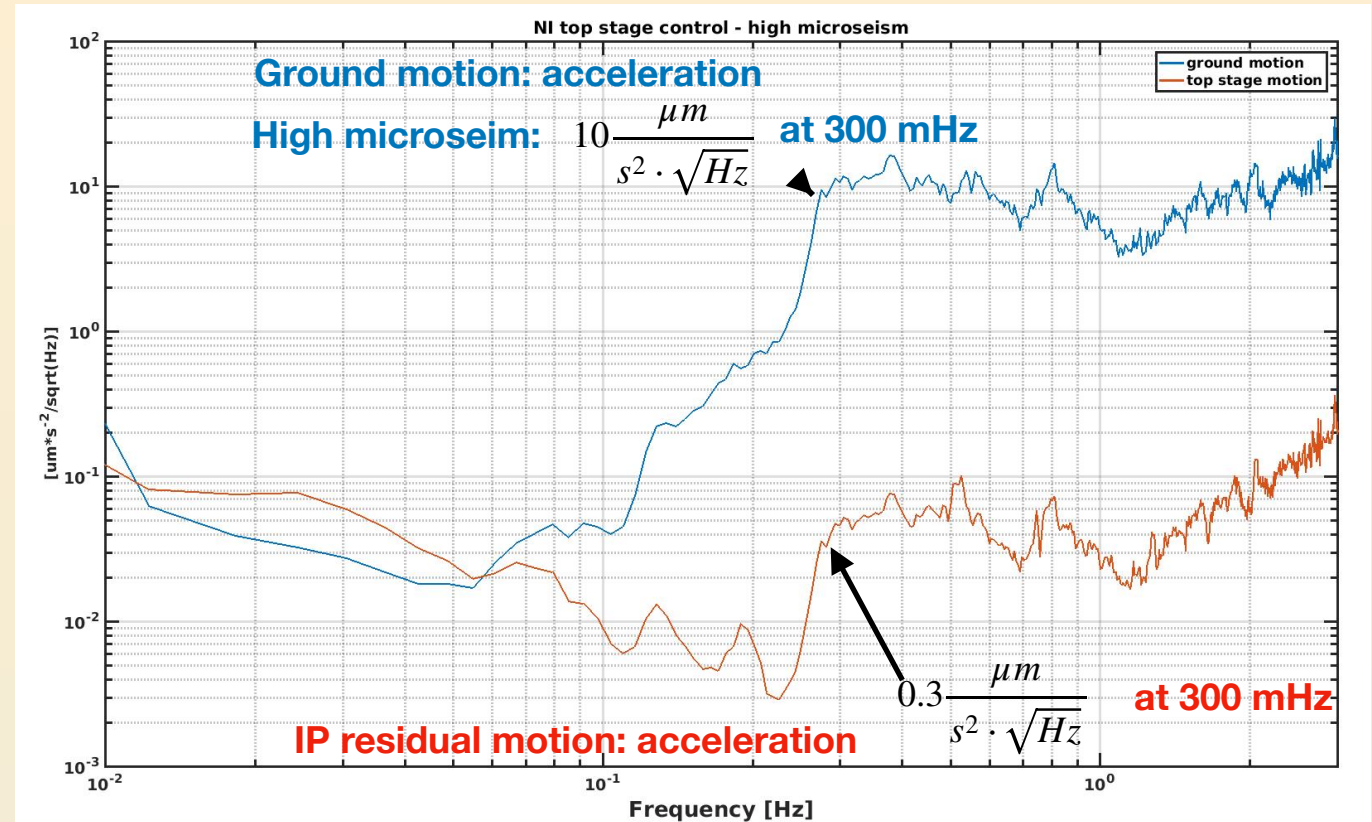
✓ The length of the cavity remains unchanged and the locking correction is reduced

✓ Since the End IP is controlled with the differential GIPC signals, it sees and consequently follows the motion of Input IP

When the IFO is locked these loops are engaged

◆ IPs are under GIPC control (X,Z)

◆ Marionette: Pitch and Yaw under automatic alignment (global control)



High microseism

Here we show the IP residual motion in two different environmental conditions

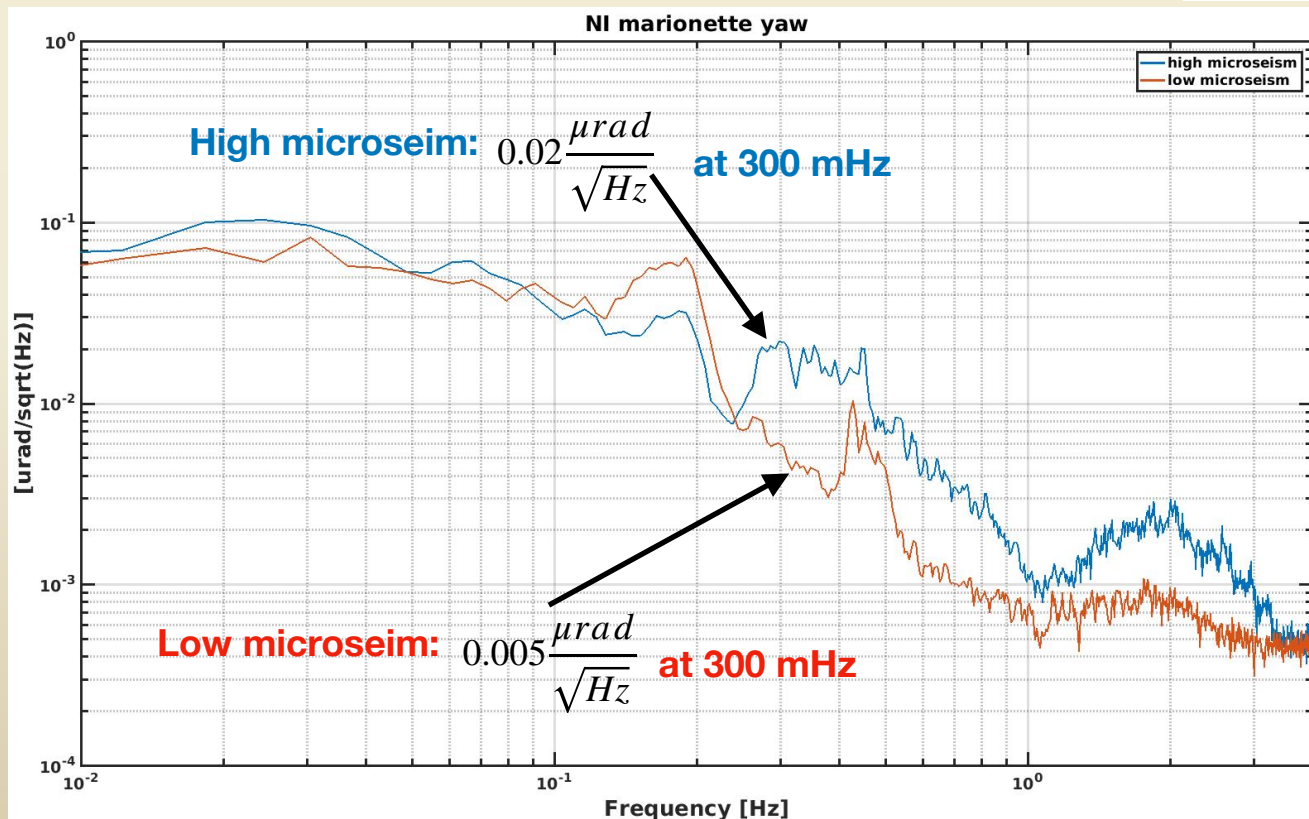
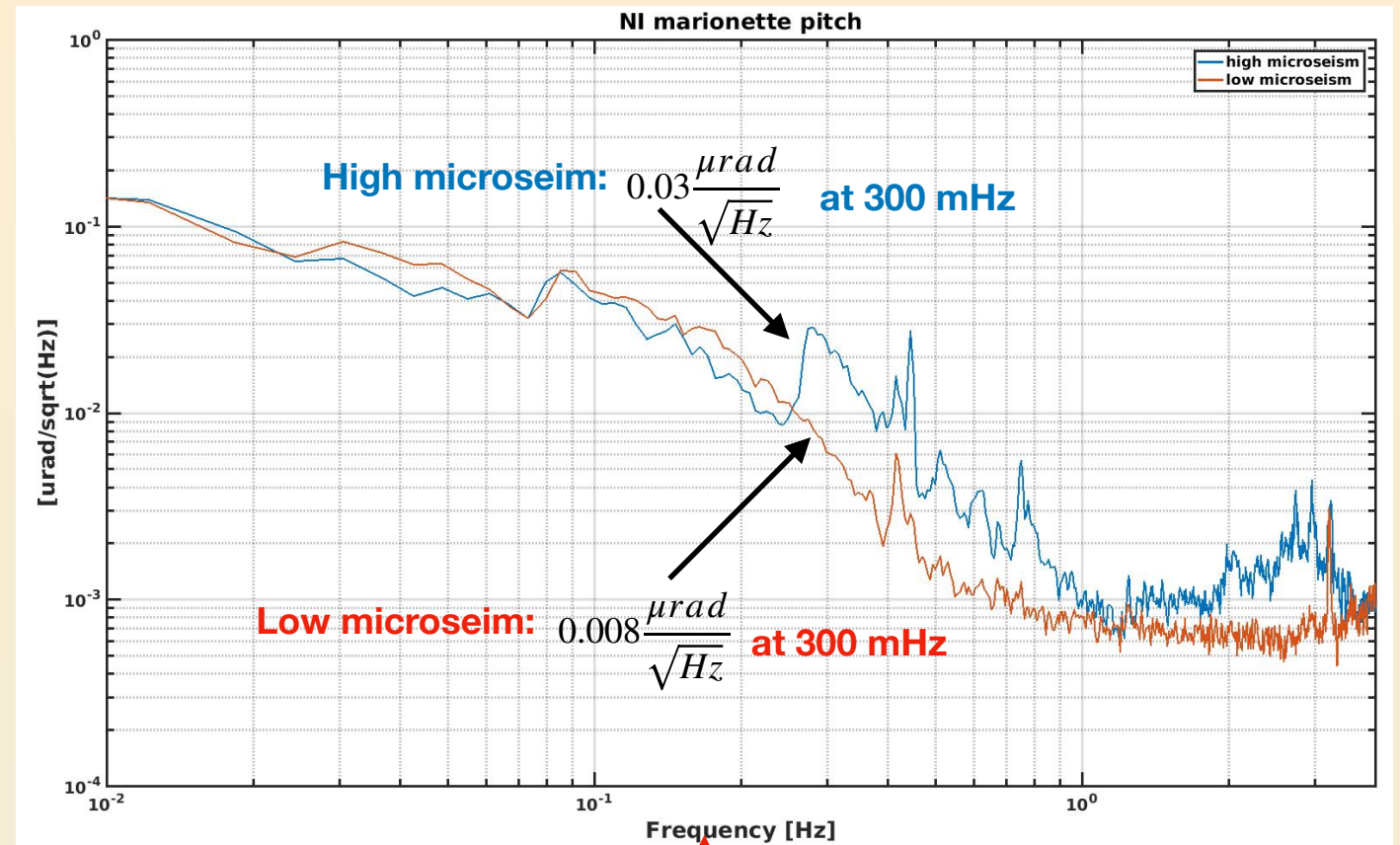
Low microseism

Plots by Paolo Ruggi
(EGO-Virgo collaboration)

When the IFO is locked these loops are engaged

◆ IPs are under GIPC control (X,Z)

◆ Marionette: Pitch and Yaw under automatic alignment (global control)



Pitch

Here we show the marionette angular residual motion for Pitch and Yaw in two different environmental conditions:

Yaw

High microseism
Low microseism

Plots by Paolo Ruggi
(EGO-Virgo collaboration)

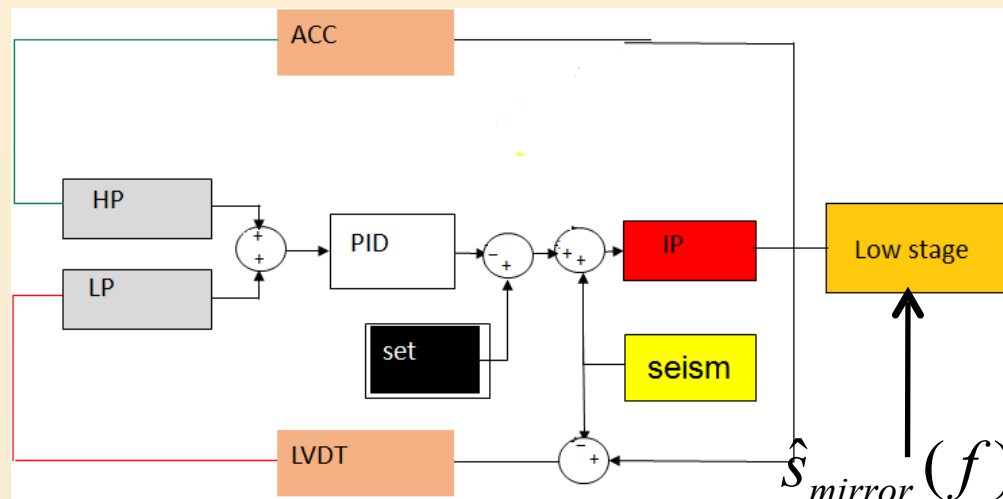
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 - **Suspension control Noise**

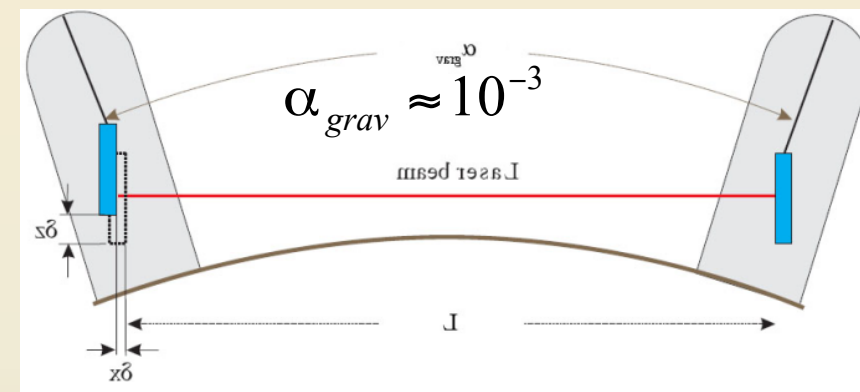
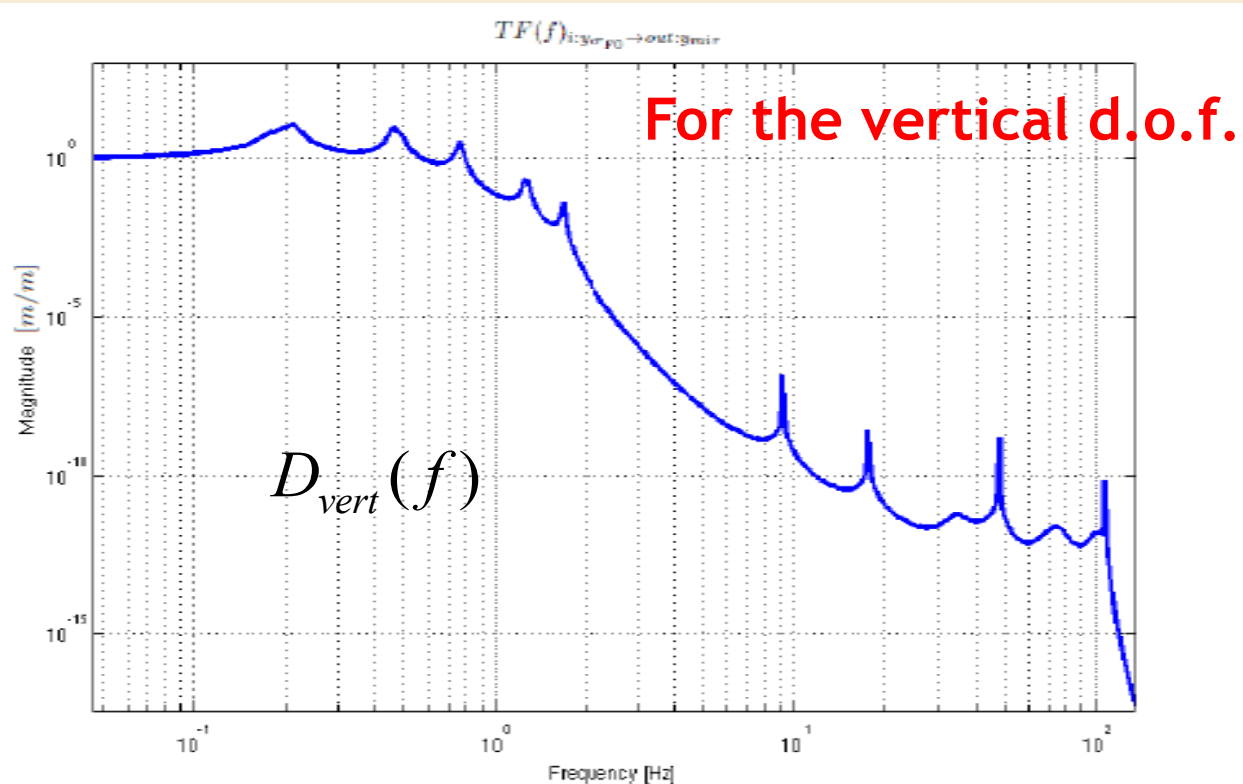
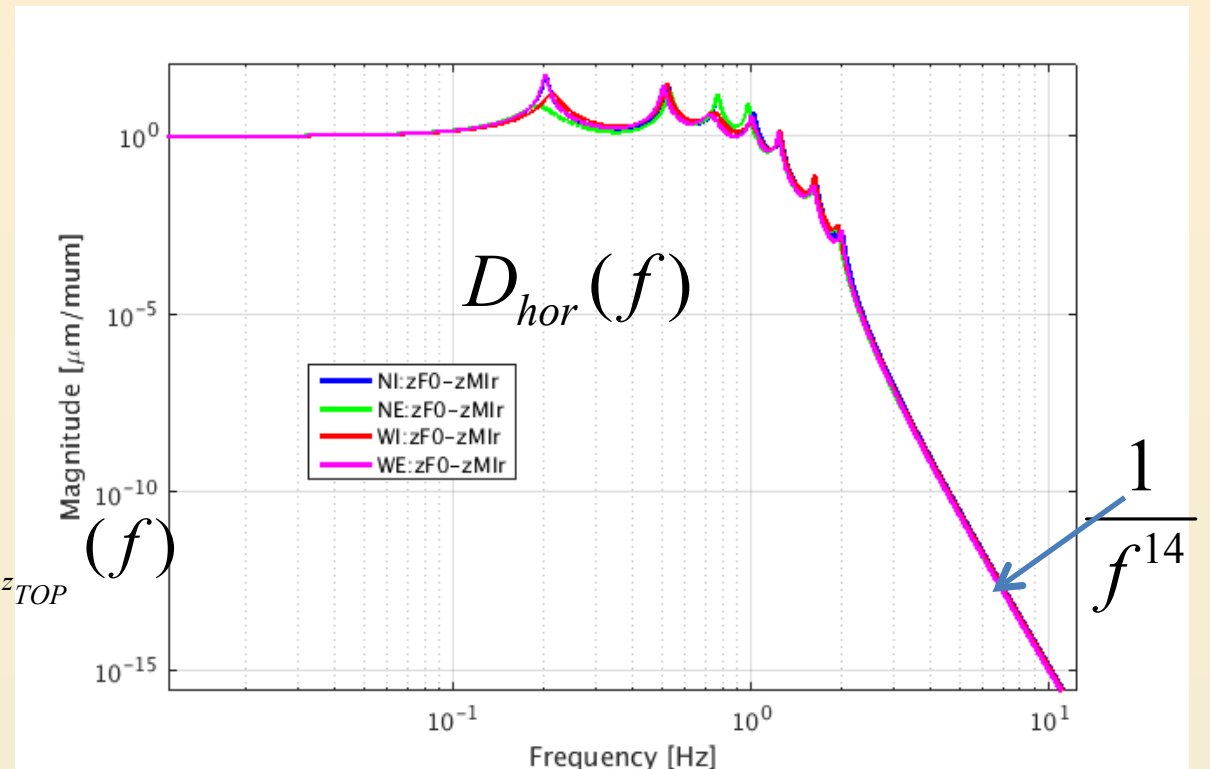
Below 10 Hz the Virgo sensitivity is limited by mechanical noise:

- Horizontal seismic noise where the mechanical attenuation is low $f < 2$ Hz
- Vertical seismic noise transmitted to the horizontal direction due to the inclination of the test mass
- Angular control noise $f < 10$ Hz
- Other possible control or actuation noise

VIRGO low frequency sensitivity



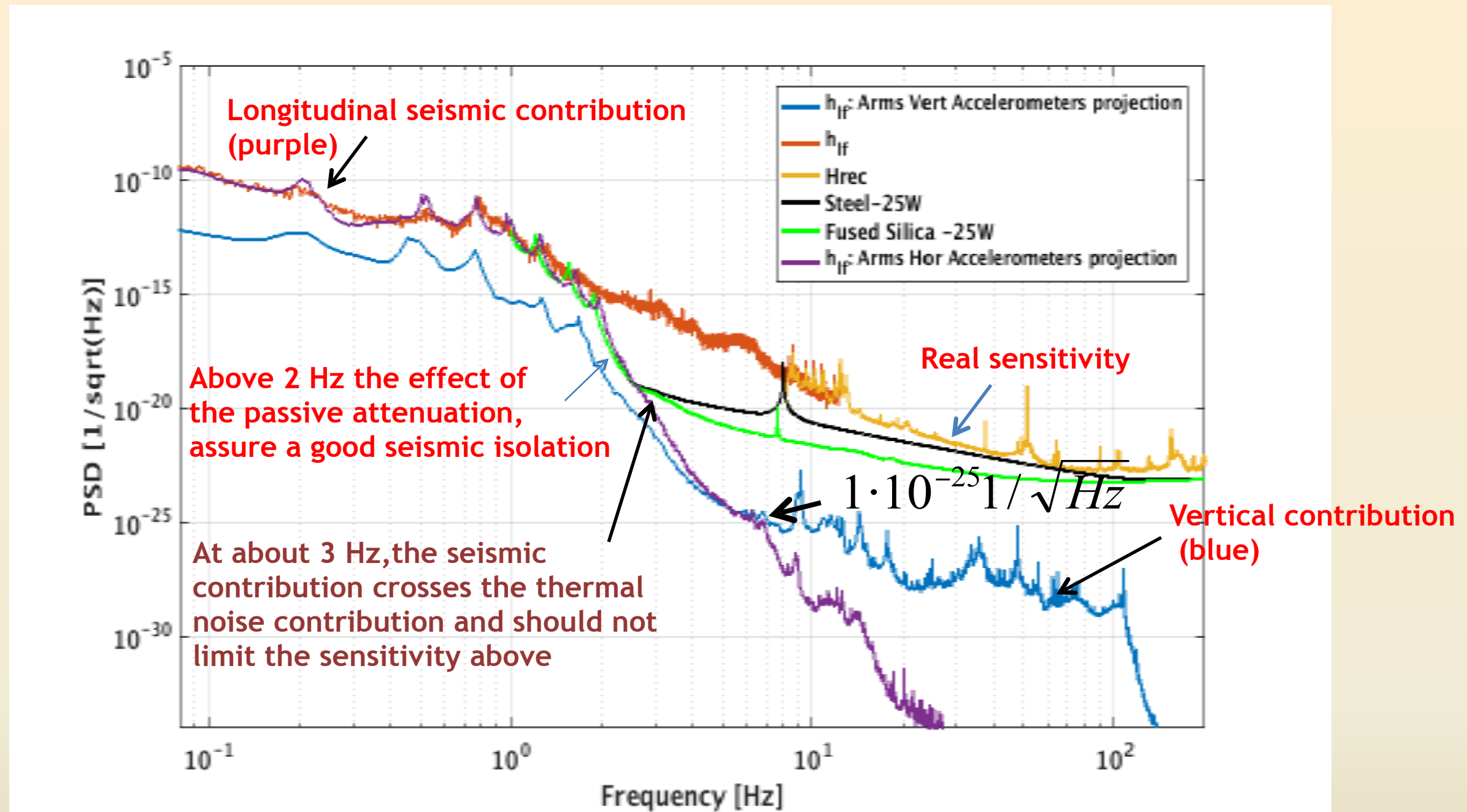
$$\hat{s}_{mirror}(f) = D_{hor}(f) \hat{s}_{z_{TOP}}(f)$$



The coupling effect between the horizontal and vertical directions due to the Earth curvature on distance like 3 Km is not negligible

$$\hat{s}_{mirror}(f) = \alpha_{grav} \cdot D_{vert}(f) \hat{s}_{y_{TOP}}(f)$$

By combining the signals of the suspensions of the FP cavities we can compute the low-frequency strain sensitivity



✓ In the region [0.1, 0.8] Hz the rms of the test mass speed (v), in low seismic noise conditions reaches the value $v < 10^{-7}$ m/s

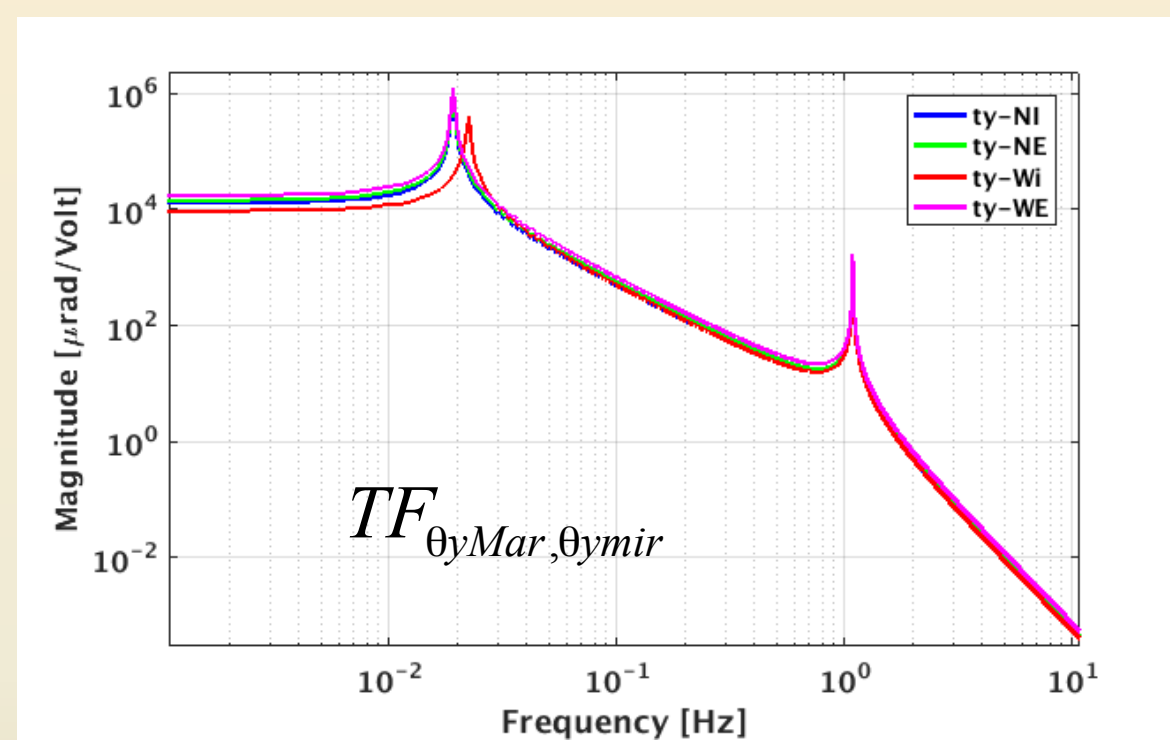
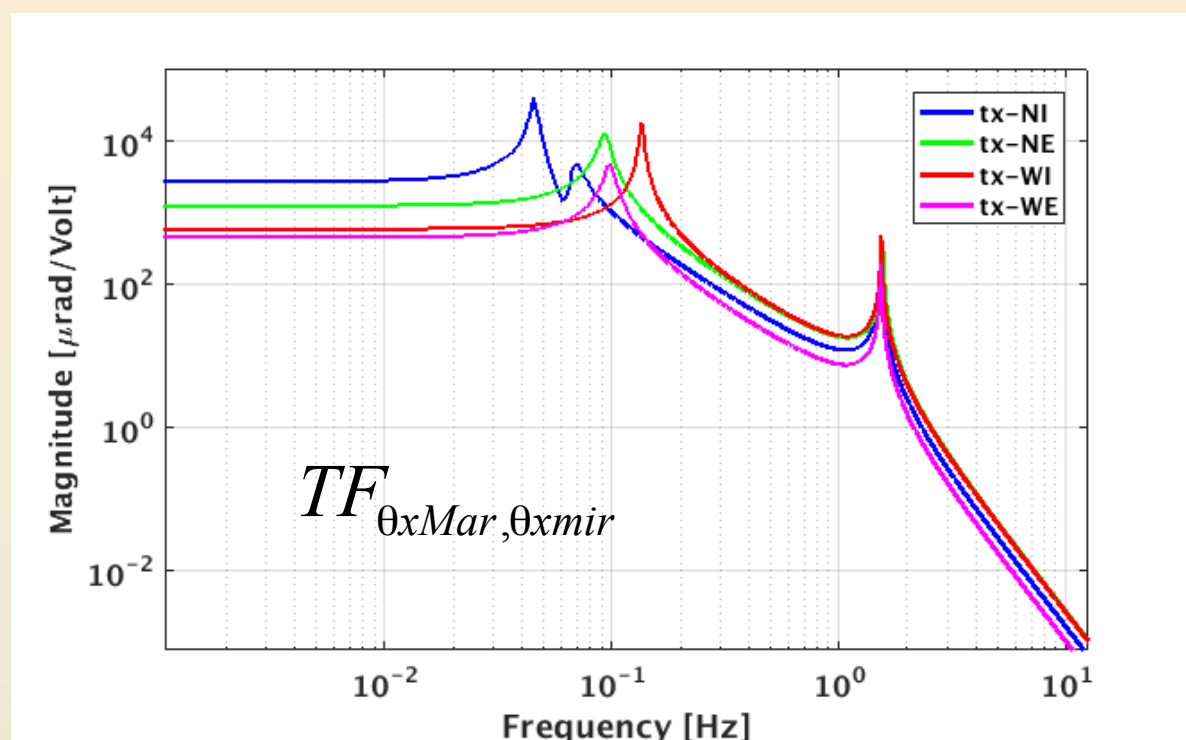
✓ In high seismic noise conditions, is still low enough to acquire the lock ($v < 5 \times 10^{-7}$ m/s)

Angular control Noise

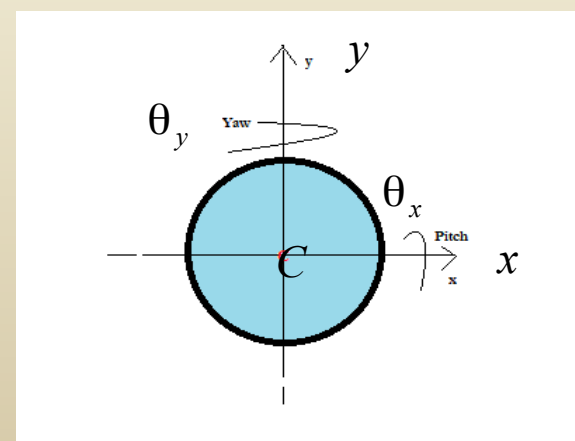
Above 2 Hz, the feedback force sent through the coils on the marionette can re-inject angular control noise

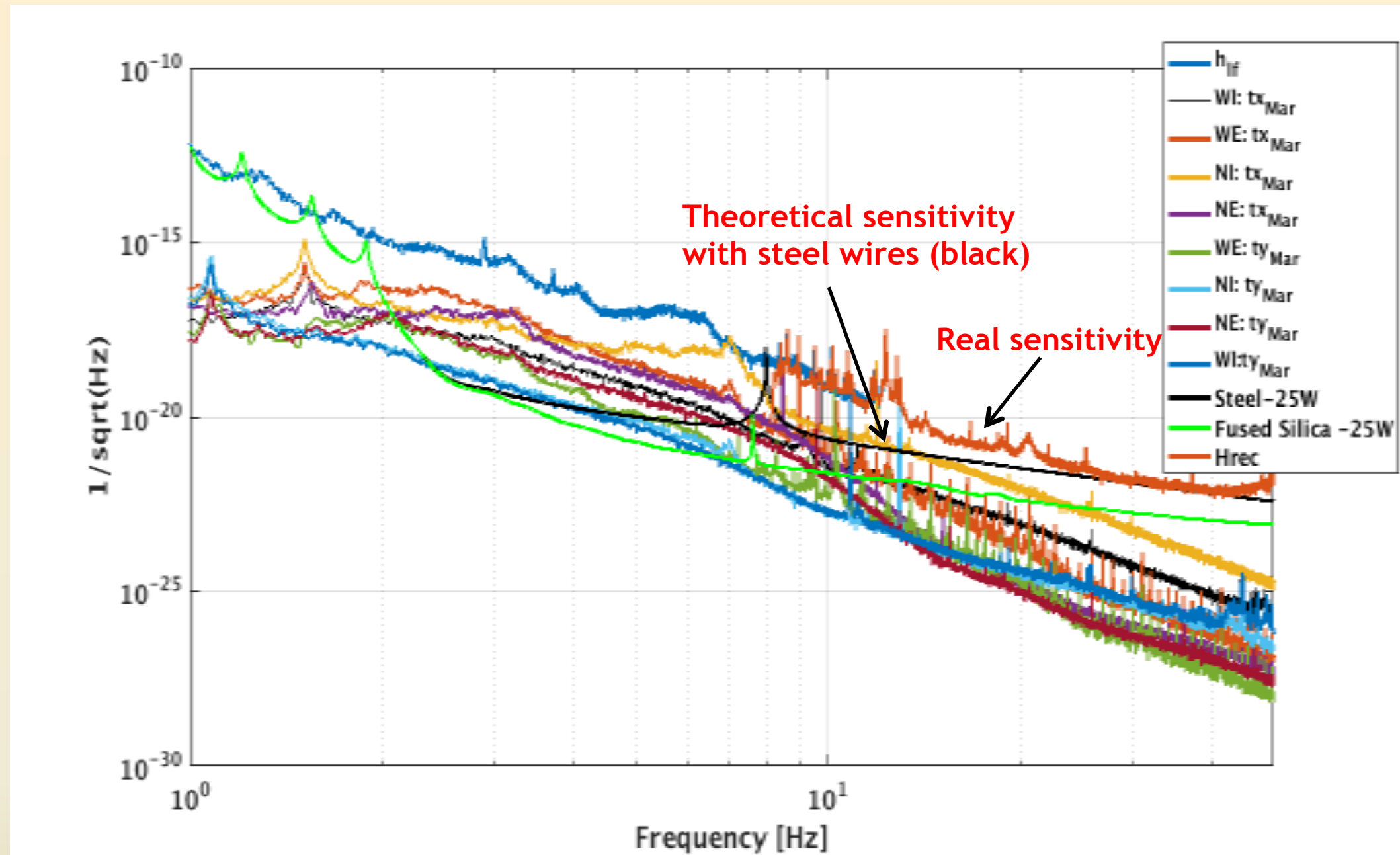
The residual motion of the mirror in Pitch and Yaw is

$$\hat{s}_{\theta_i, \text{mir}}(f) = c_{\theta_i} TF_{\theta_i \text{Mar}, \theta_i \text{mir}} \hat{s}_{\theta_i, \text{MarCorr}}$$



c_{θ_i} is the parameter that quantifies the decentring of the beam with respect to the center of the mirror (C).





Estimated $c_{\theta_i} \approx 50 \mu m$ 

	c_{θ_i} Pitch (m)	c_{θ_i} Yaw (m)
NI	0.7×10^{-4}	0.8×10^{-5}
NE	0.3×10^{-4}	0.4×10^{-5}
WI	0.1×10^{-4}	0.7×10^{-5}
WE	0.2×10^{-4}	0.4×10^{-5}



"That's all Folks!"

Thanks for your attention!!!!