



Commissioning of the Type A suspensions control of KAGRA

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OUTLINE

- **Introduction**
- **Seismic noise**
- **VIS**
- **Type A**
- **Noise budget of diagonalized sensors**
- **Blending technique**
- **Inertial damping: preliminary results**
- **Conclusion**

Introduction

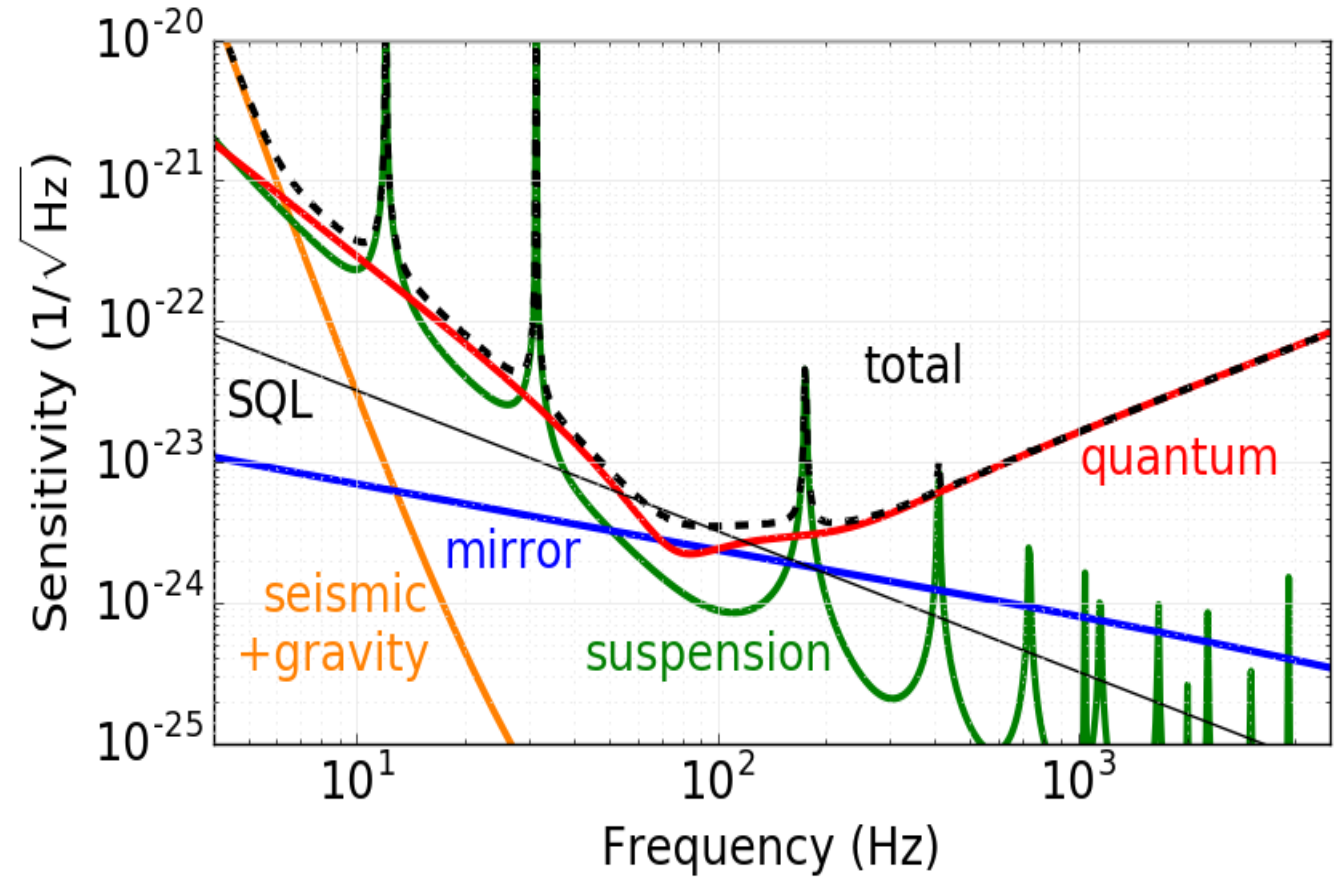
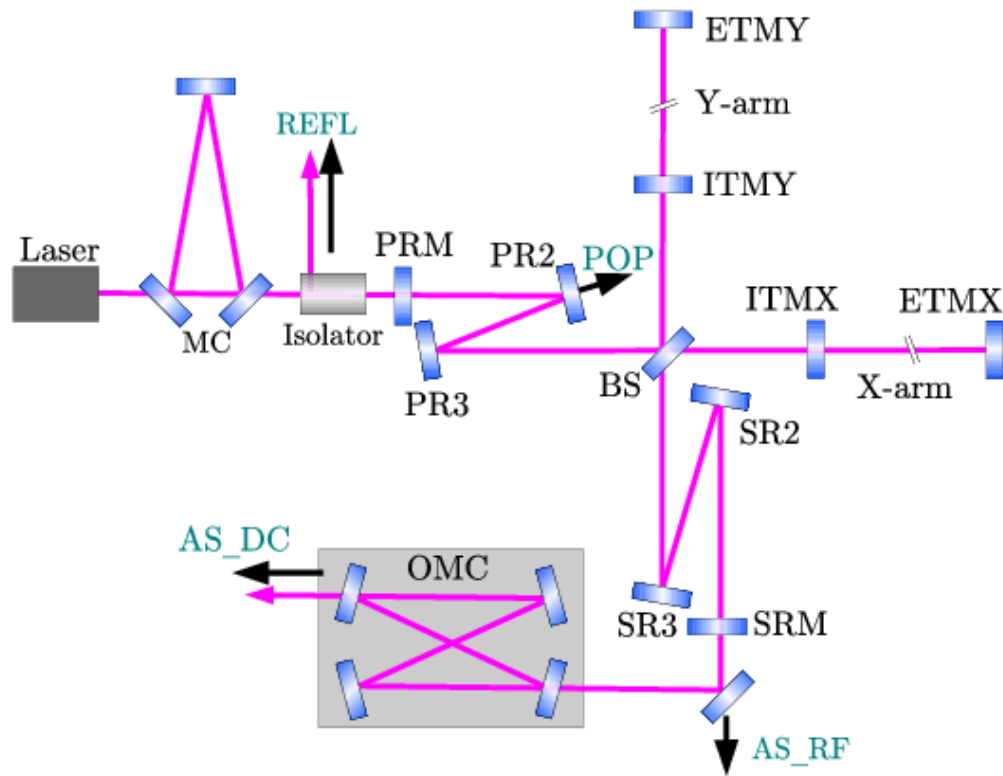


- ▶ Gifu Prefecture, Japan
- ▶ 3km Arm Length
- ▶ Underground
- ▶ Cryogenic



Introduction

Target sensitivity of KAGRA



- ◆ Michelson ITF + 3 km long FP cavities
- ◆ Detection band [10 Hz, 10 kHz]

Limitations: **Seismic Noise**, **Shot Noise**, **Thermal Noise**..

Underground

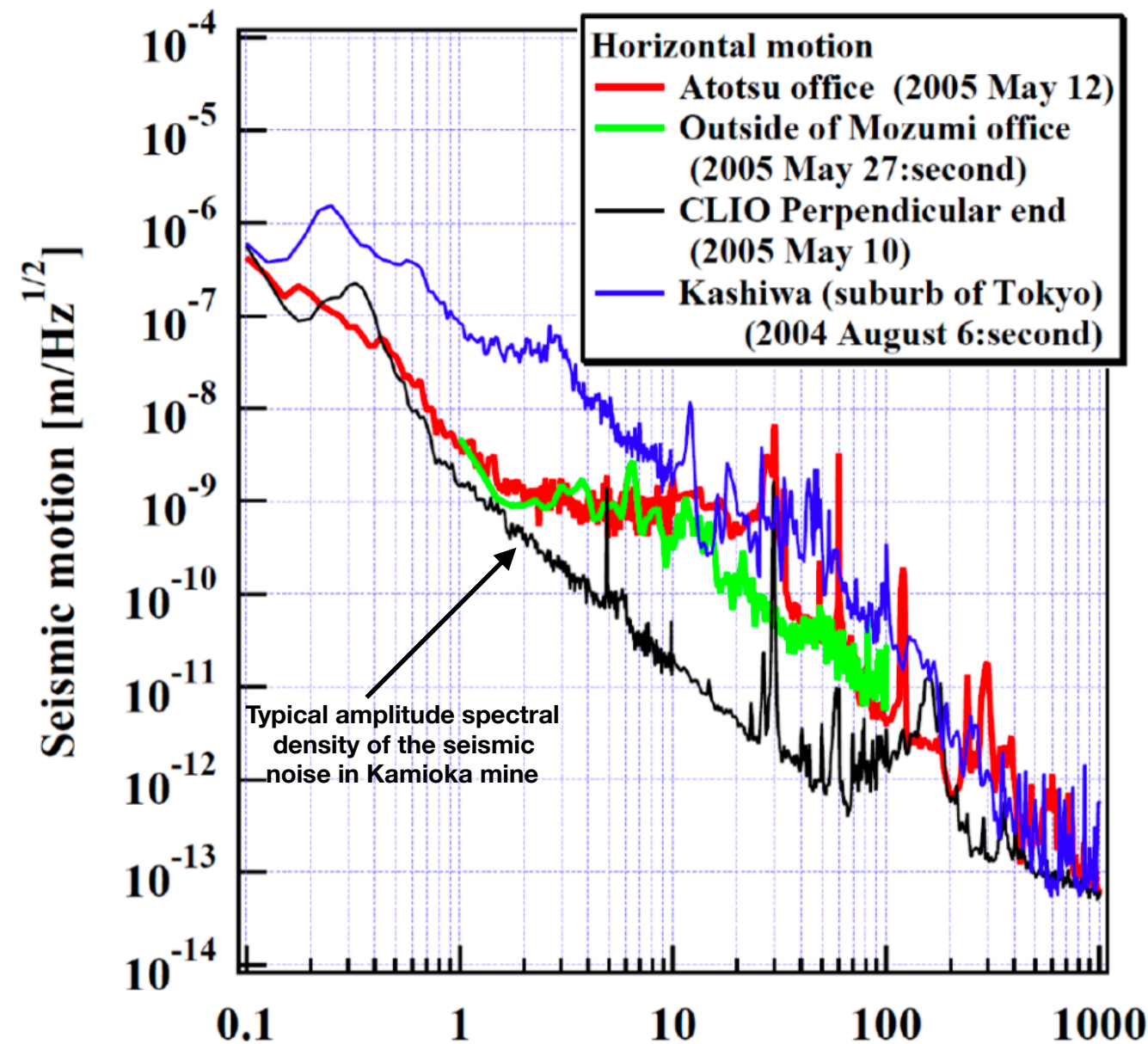
Reduce Seismic Noise

Cryogenic

Reduce Thermal Noise

Seismic Noise

KAGRA interferometer has been designed with the intent to develop an experimental apparatus for GW starting from 10 Hz.



* **Seismic noise**: is the dominant noise at low frequencies (below 10 Hz):

On Earth surface

$$\frac{10^{-6}m}{\sqrt{Hz}}$$

@150 mHz

Underground

$$\frac{5 \cdot 10^{-7}m}{\sqrt{Hz}}$$

* In detection band > 10 Hz the seismic noise reaches the values

On Earth surface

$$\frac{10^{-9}m}{\sqrt{Hz}}$$

Underground

$$\frac{10^{-12}m}{\sqrt{Hz}}$$

To detect the little displacement

due to a GW $\frac{10^{-18}m}{\sqrt{Hz}}$

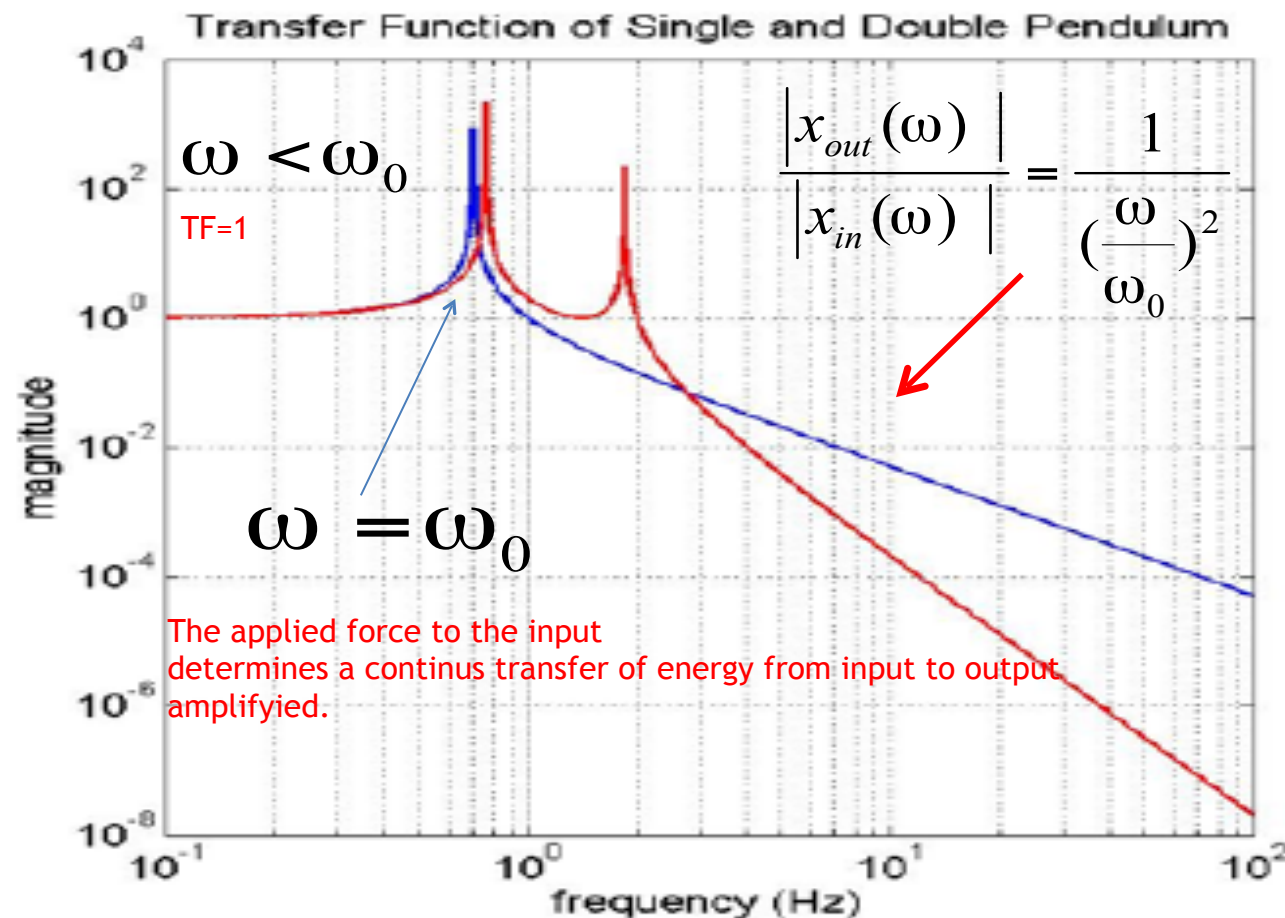
A seismic isolation with a capability attenuation ~ 10 orders of magnitude is needed!!!

- **Free-falling TM (Test Mass)**
- **Isolation from Seismic Noise**

Mechanical attenuators of the seismic vibrations

A good approximation of the free falling mass is represented by the simple pendulum

$$\frac{|x_{out}(\omega)|}{|x_{in}(\omega)|} = \frac{1}{1 - \left(\frac{\omega}{\omega_0}\right)^2}$$

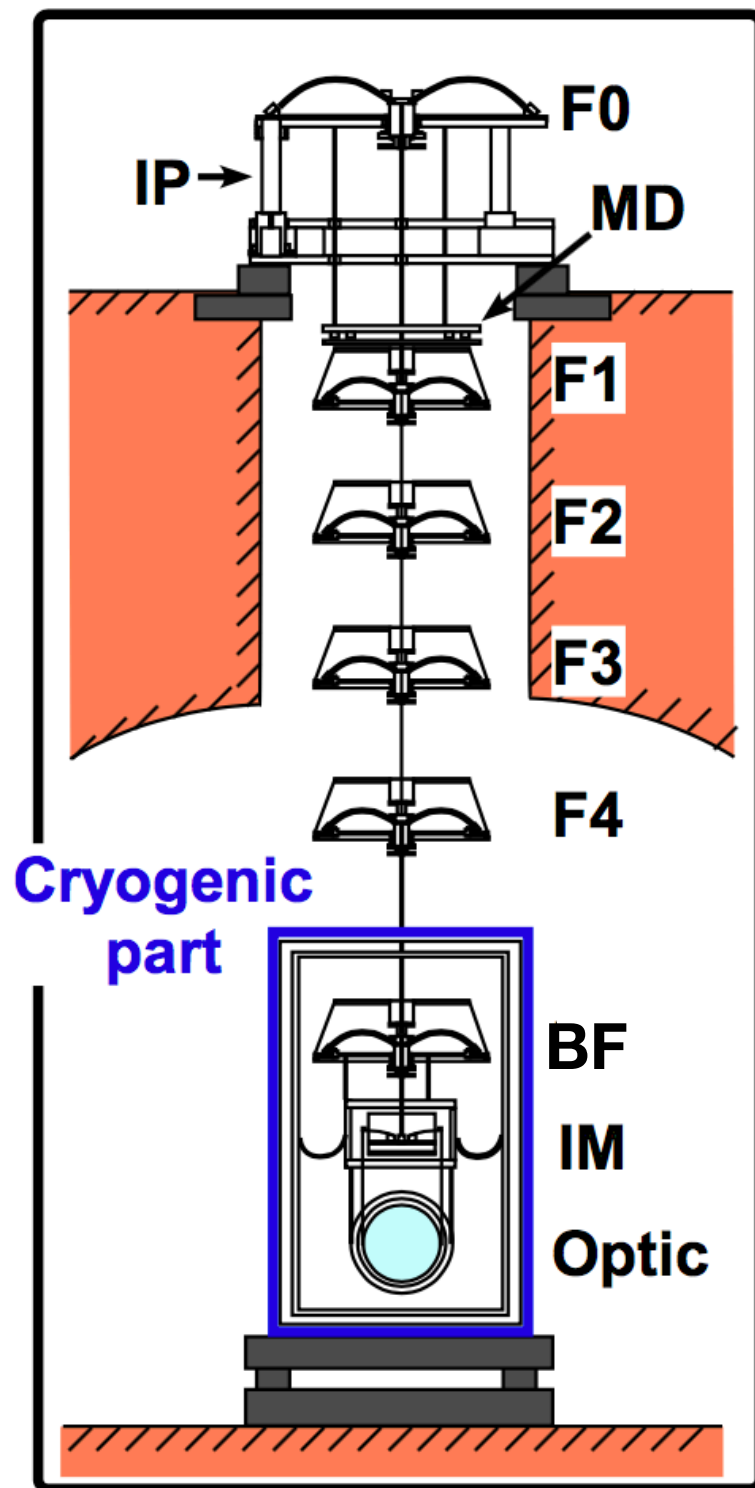


Cascading 2 harmonic oscillators

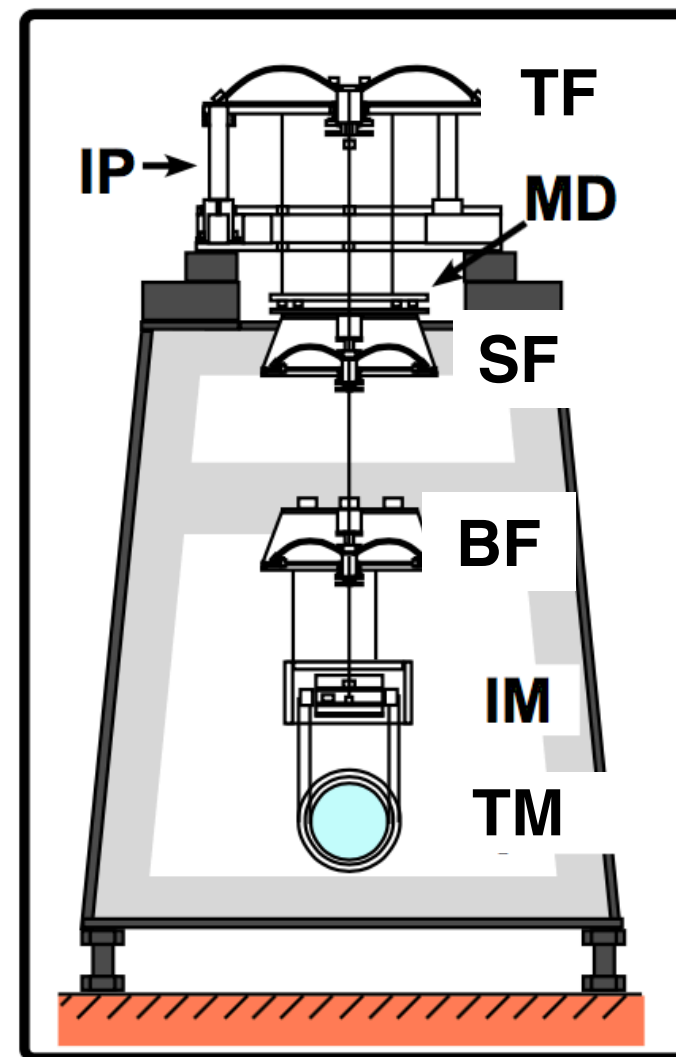
$$\frac{|x_{out}(\omega)|}{|x_{in}(\omega)|} = \frac{A}{(\omega)^4} \quad A = \omega_1^2 \cdot \omega_2^2$$

Solution adopted in KAGRA is based on the idea to replicate a certain number of harmonic oscillators of length ~ 2 m to obtain a sophisticated mechanical structure: VIS suspension system

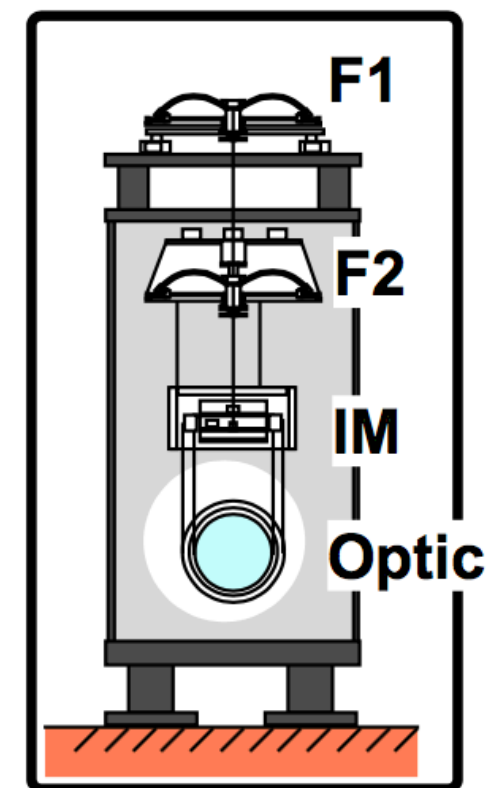
VIS Suspension Systems



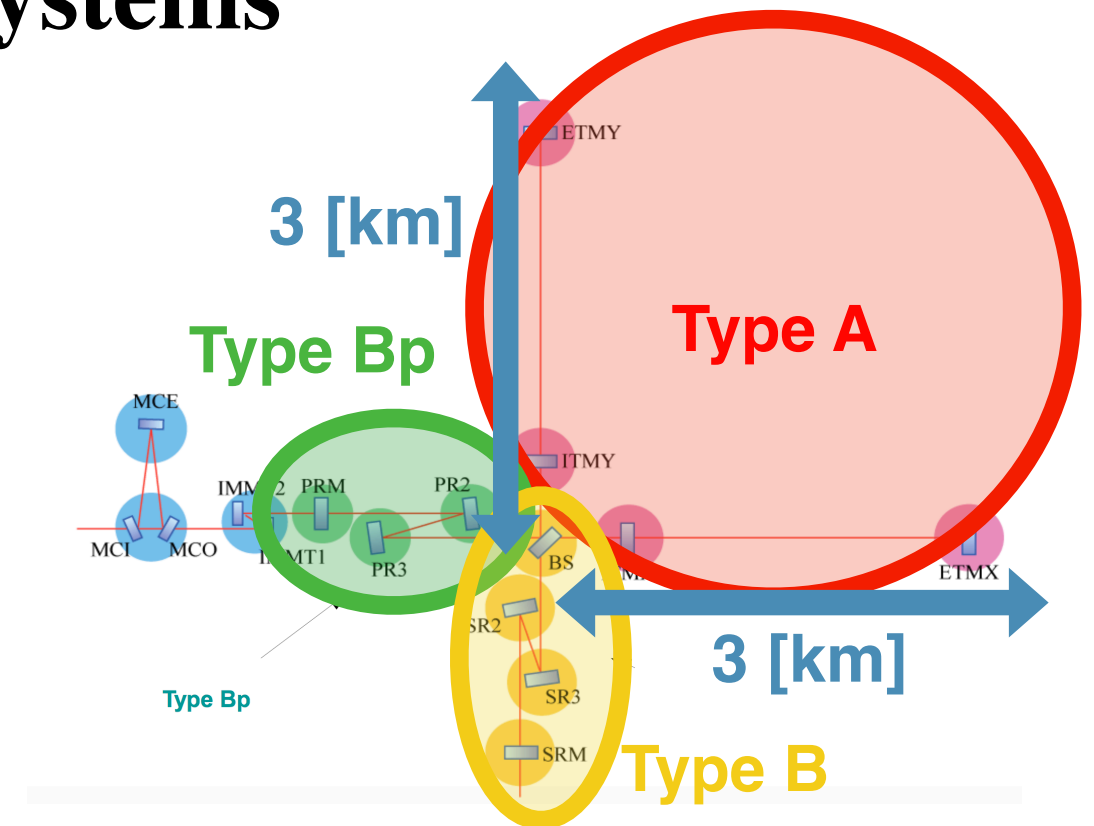
Type-A



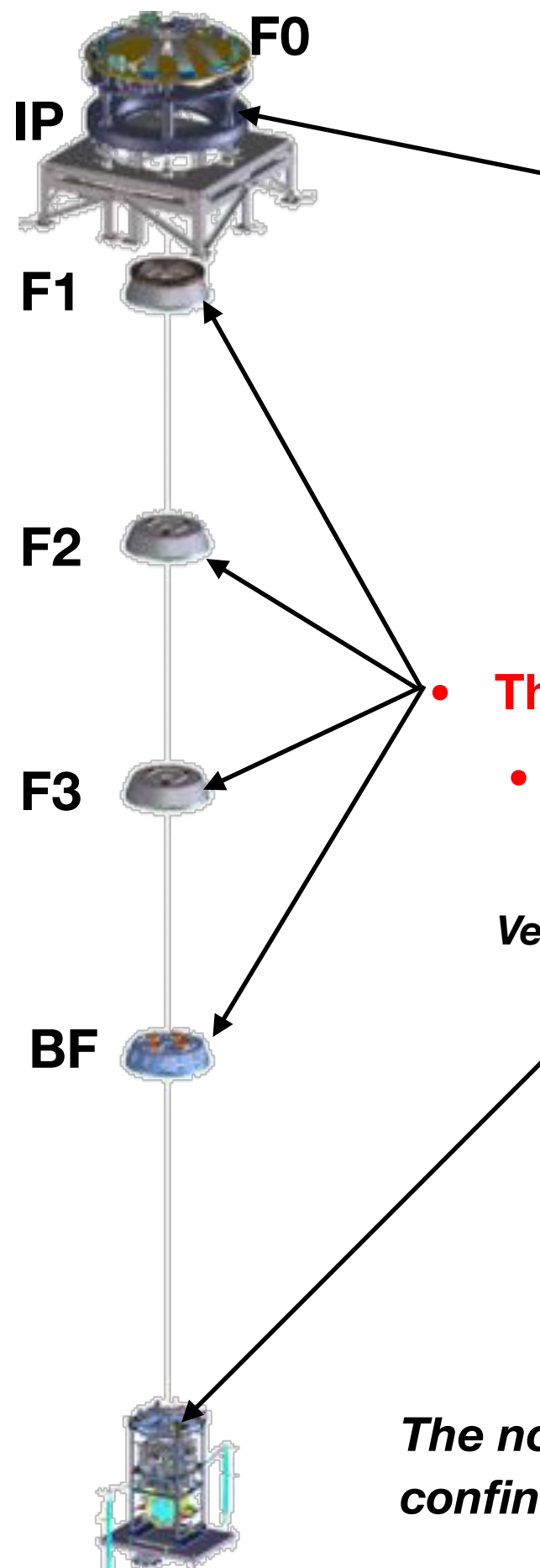
Type-B



Type-Bp



Type A suspension



- **Pre-isolation stage:**

- the Inverted Pendulum (IP-3 legs structure)
- mechanical filter (F0)

The system provides a good seismic isolation in horizontal direction (IP) as well as in the vertical one (GAS Filters).

- **The passive multi-stage pendulum chain:**

- Four mechanical GAS filters (F1, F2, F3, BF Steering Filter)

Vertical modes of the mechanical filters are below 1 Hz

- **The cryopayload:**

- Platform
- Marionette
- Intermediate mass
- Test mass

The normal modes of the pendulum mechanical structure are confined in low frequency region (below 2Hz)

Type A suspension:

Sensors and actuators

The **feedback control** could be implemented in different points:

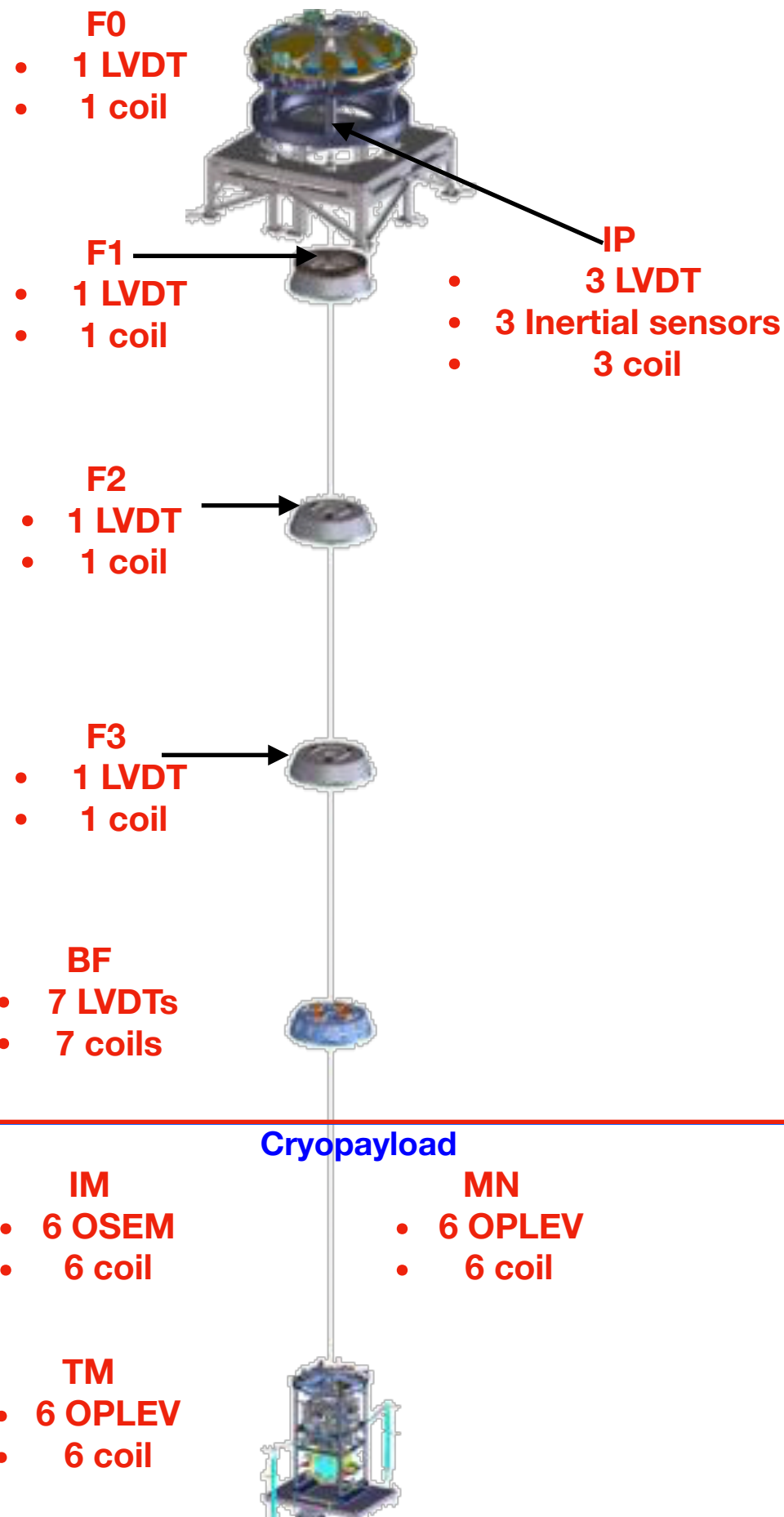
- Inverted Pendulum
- vertical GAS filters
- Bottom filter
- Marionette and Test Mass

1. Control on IP to reduce the motion in L, T and Y
2. Control on BF to reduce the Yaw motion of the chain
3. Control on top stage and GAS filter to reduce the Vertical motion
4. Control on the Marionette and Test Mass to reduce the Yaw and Pitch motion

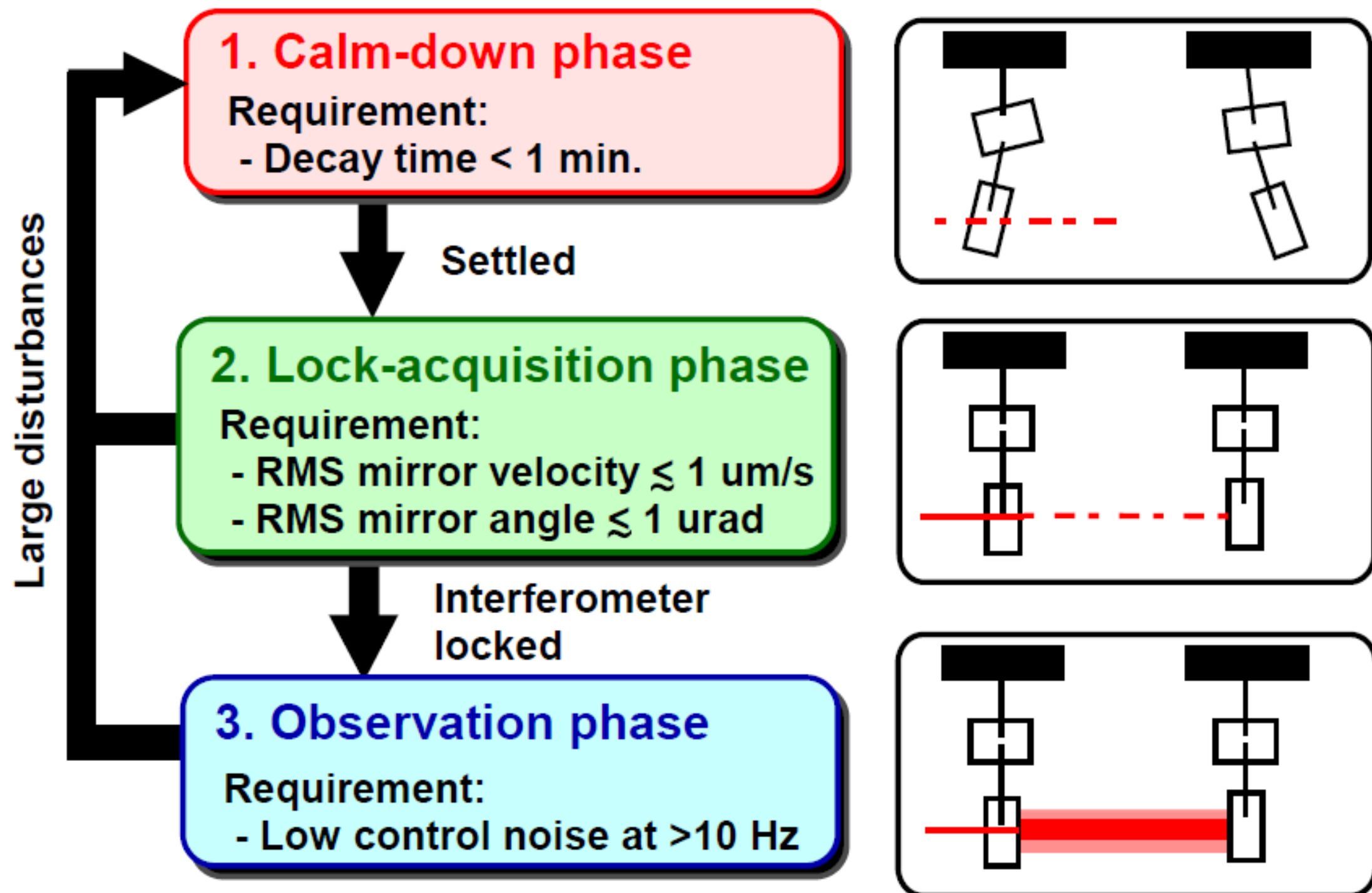
We focus our attention on the points 1 and 2.

For IP, BF and GAS Filters the adopted control strategies are:

- On the IP is implemented an Active Mode Damping of the resonance modes and for seismic noise reduction
- On the BF and on the GAS filters a viscous damping control of the resonance modes is implemented



Type A suspension: requirements



Type A: actuation points

- **F0**
- 1 LVDT
- 1 coil



Feedback control

- **F1**
- 1 LVDT
- 1 coil

- **F2**
- 1 LVDT
- 1 coil



Feedback control

- **F3**
- 1 LVDT
- 1 coil



Feedback control

- **BF**
- 7 LVDTs
- 7 coils



Feedback control

Cryopayload



Calm down phase:
✱ IP control

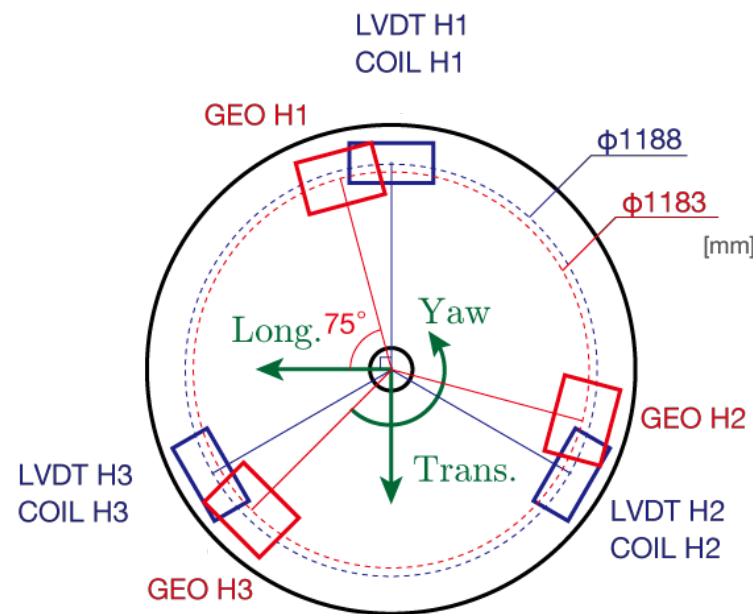
Calm down phase:
✱ GAS filters control

Calm down phase:
✱ BF Y control

Type A suspension: sensors and actuators

To implement the Damping control on the IP and on the BF first we build the diagonalized sensors and actuators in the (L,T,Y) base

IP



LVDTs sensing matrix

sensor base:
(H1, H2, H3)

Geometrical transformation

Euler base:
(L, T, Y)

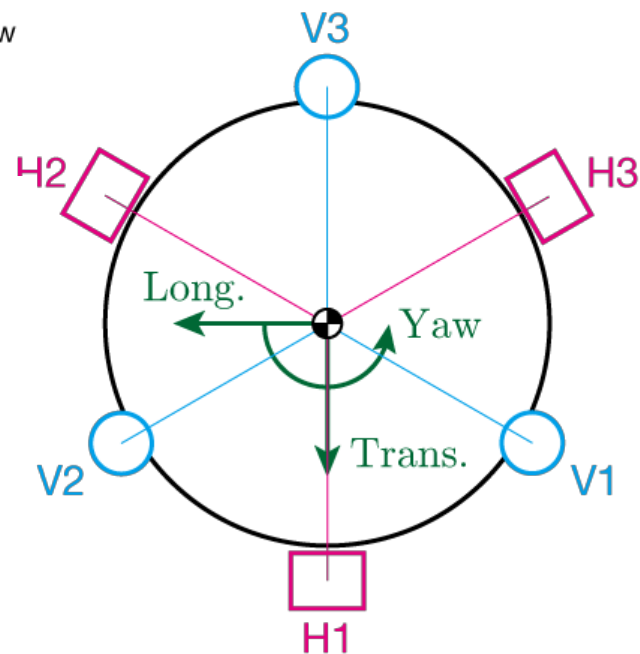
Read-out Driving matrix

Actuators base:
(H1, H2, H3)

Noise injection from each actuator (@2 Hz line)

Euler base:
(L, T, Y)

• Top view



BF

LVDTs sensing matrix

sensor base:
(H1, H2, H3)
(V1, V2, V3)

Geometrical transformation

Euler base:
(L, T, Y)
(P, R, V)

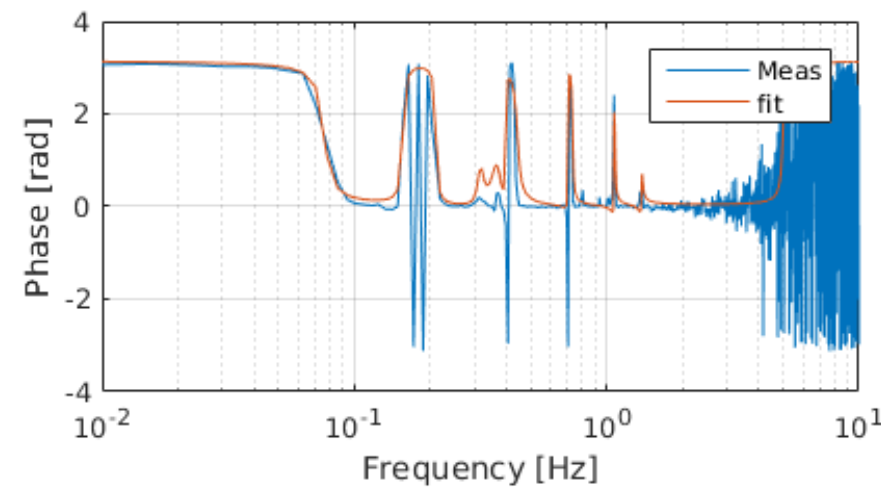
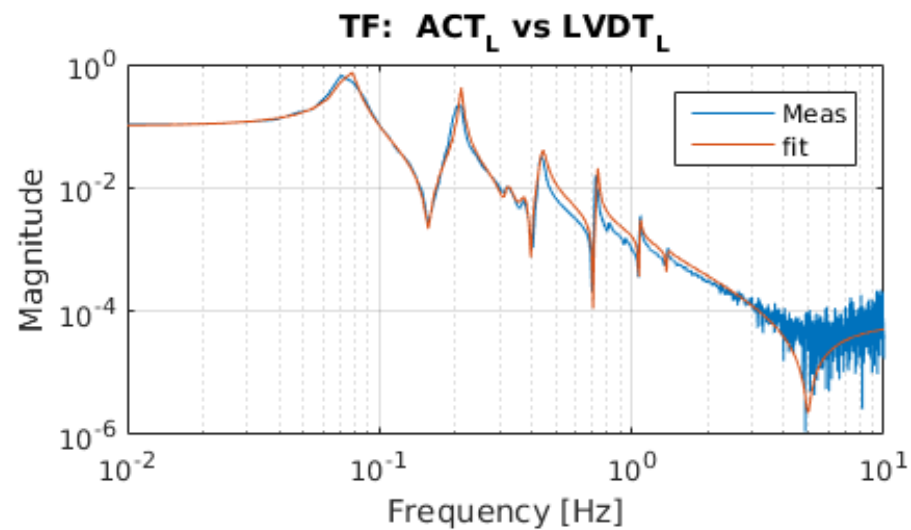
Driving matrix

Actuators base:
(H1, H2, H3)
(V1, V2, V3)

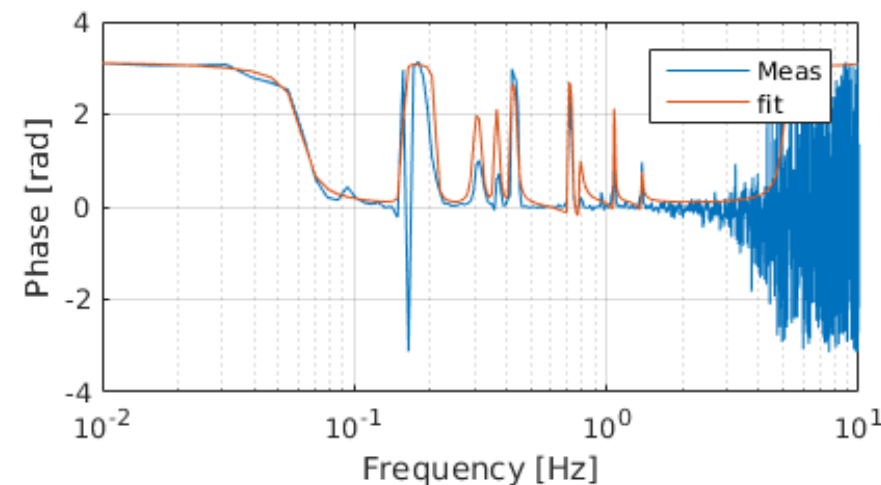
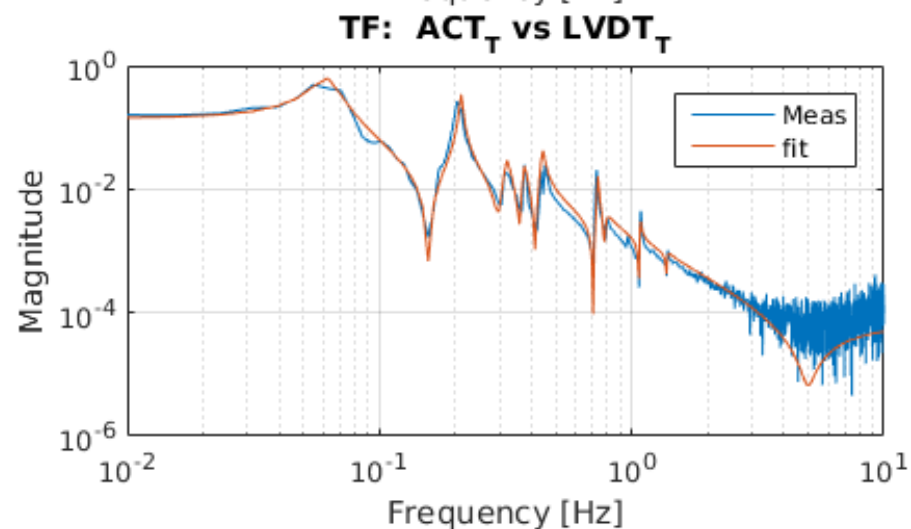
Geometrical transformation

Euler base:
(L, T, Y)
(P, R, V)

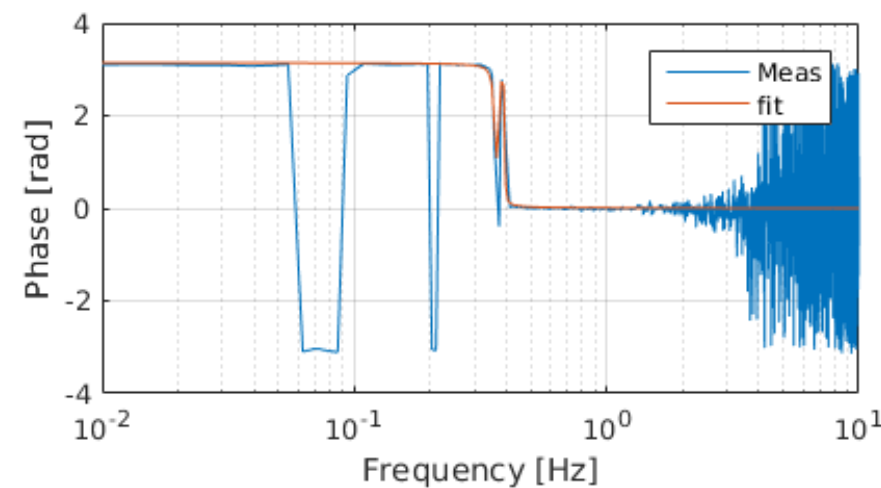
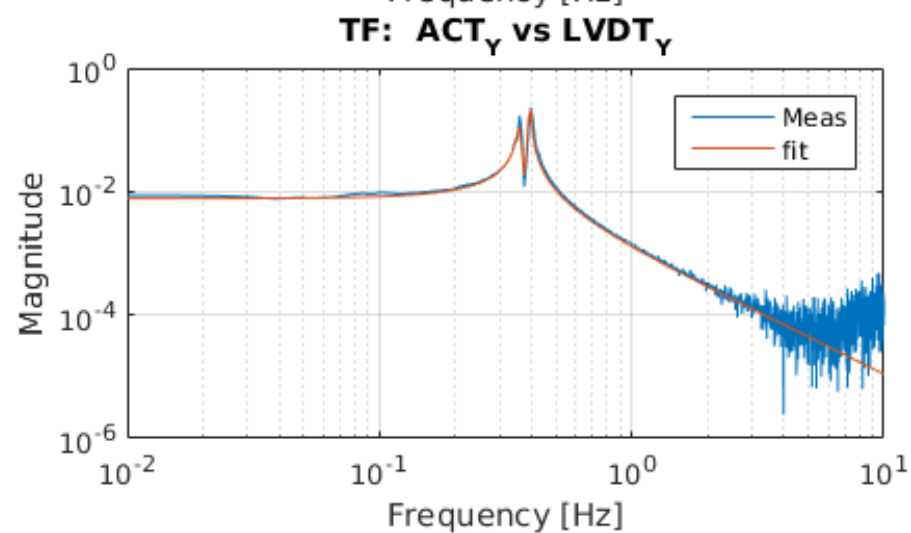
Inverted Pendulum (IP) mechanical transfer functions



IP: L mode 0.067 Hz

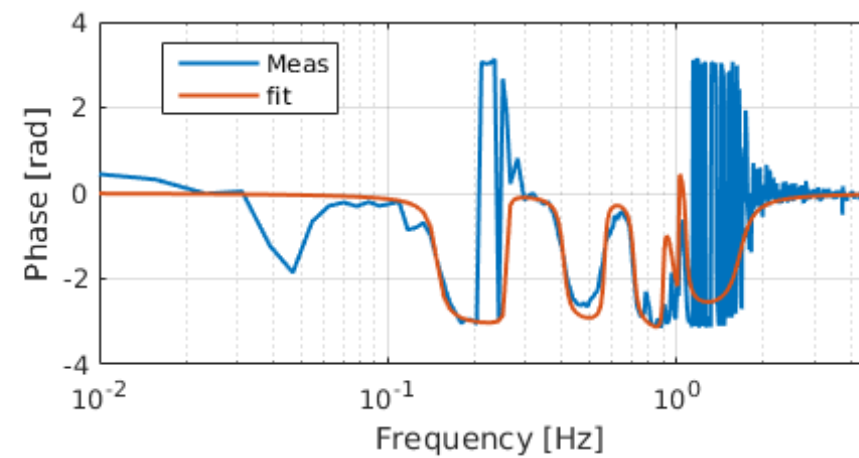
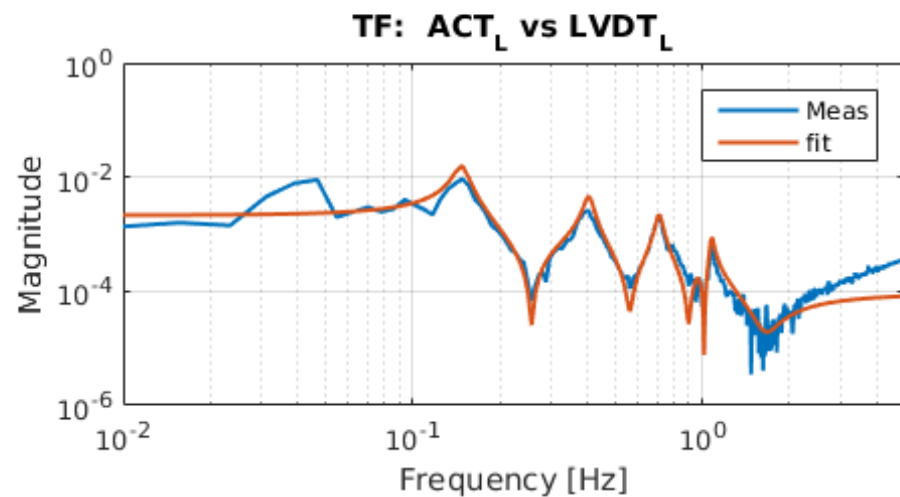


IP:T mode 0.067 Hz

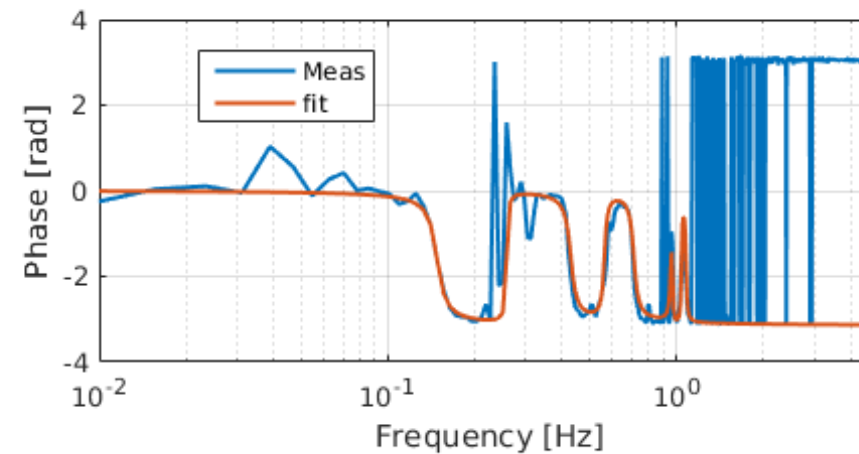
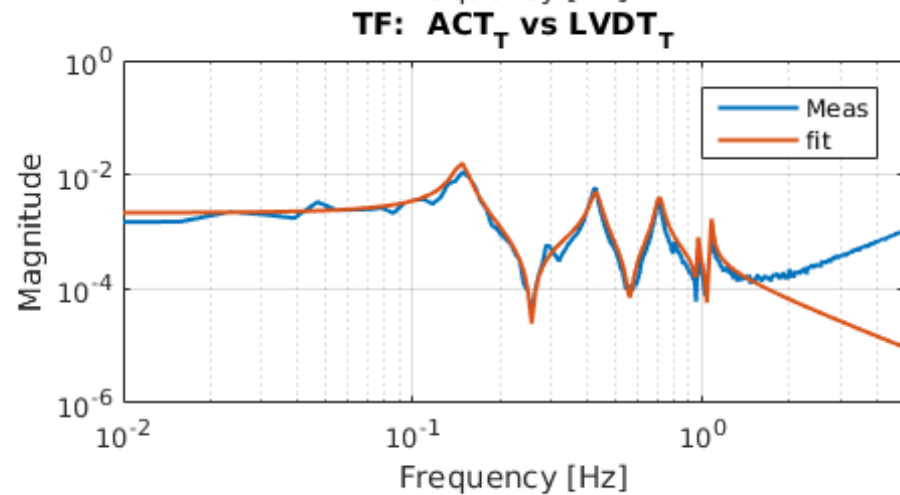


IP:Y mode 0.4 Hz

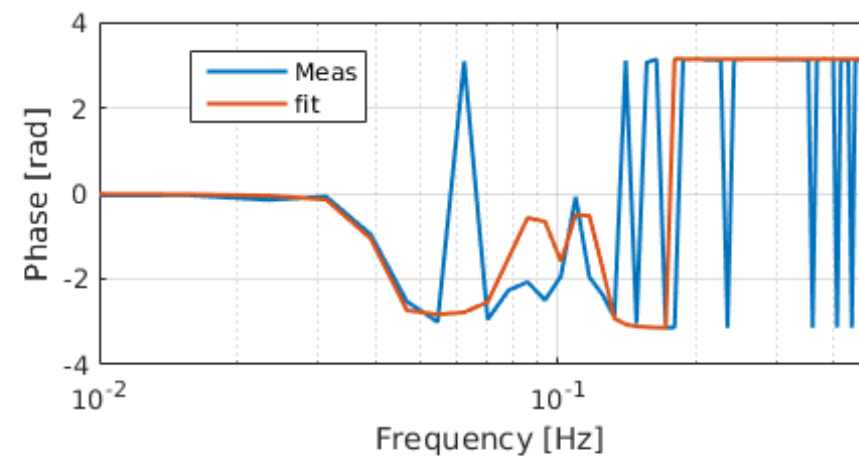
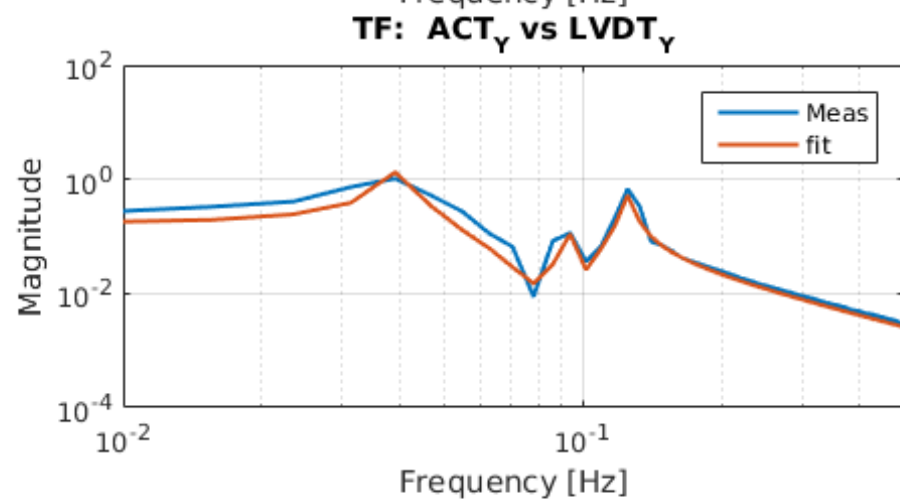
Bottom Filter (BF) mechanical transfer functions



BF: L mode 0.148 Hz



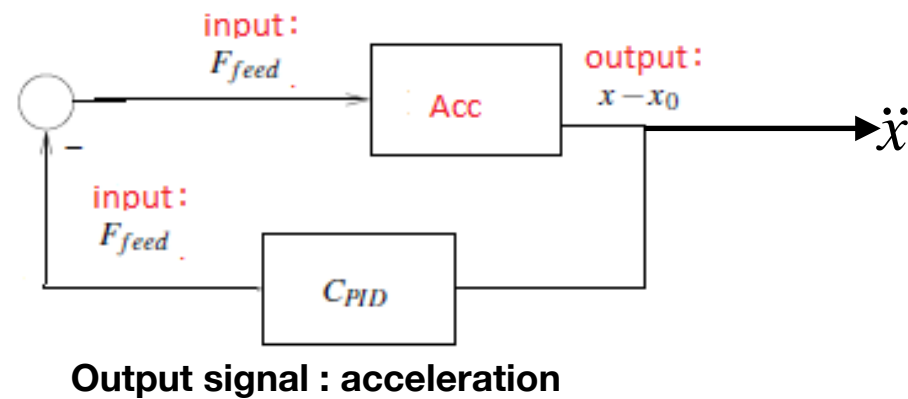
BF:T mode 0.148 Hz



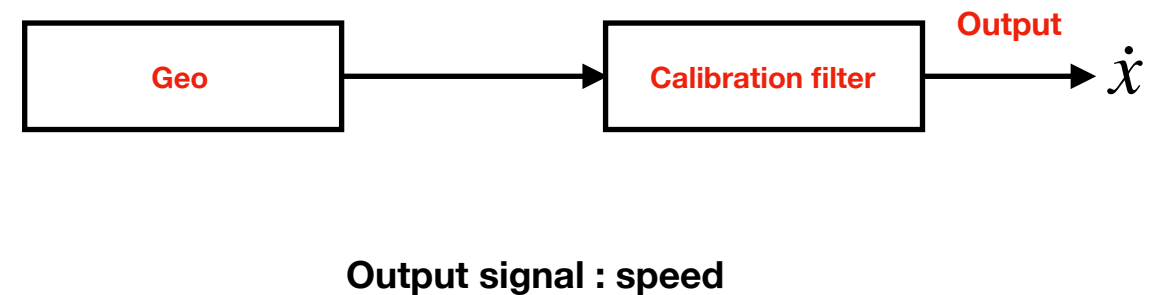
BF:Y mode 0.04 Hz

Type A: inertial sensor (I)

Input suspensions (ITMX,ITMY):
3 accelerometers



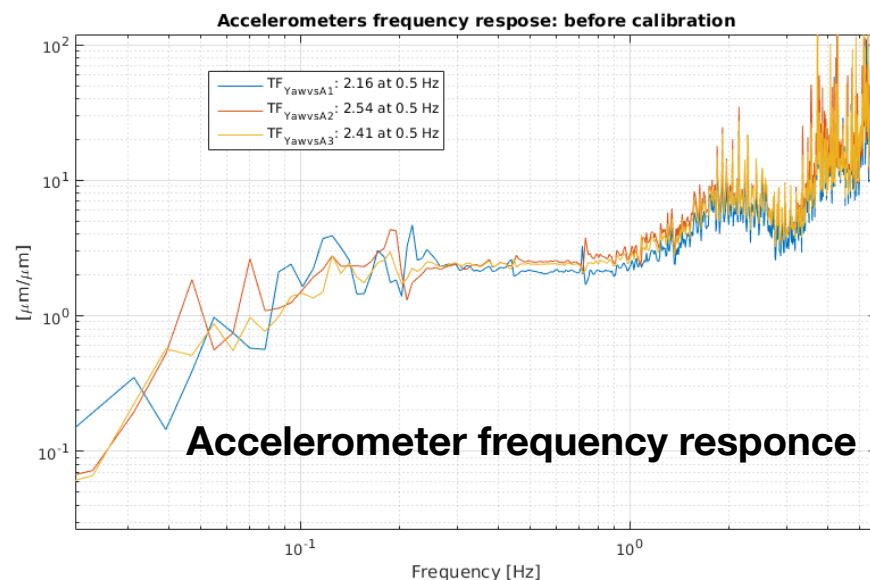
End suspensions (ETMX,ETMY):
3 Geophones



In both cases we need of the inter-calibration with the LVDT signals!

Injecting white noise along the IP Yaw degree of freedom and to measure the transfer function:

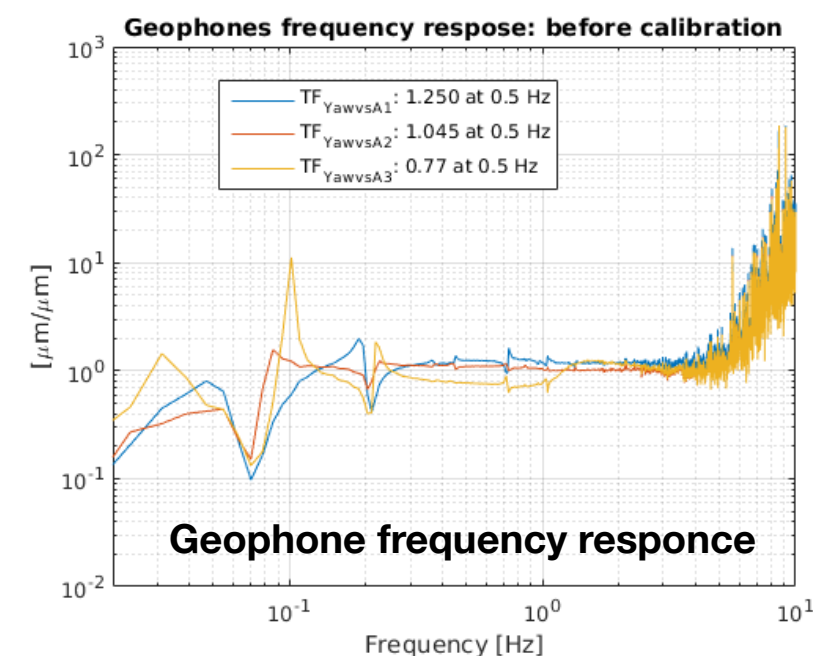
$$TF_{yaw_{acc_i}} = \frac{Yaw_{lvd_t} \cdot r}{\frac{acc_i}{\omega^2}}$$



where $i=1,2,3$ and r is the linear distance of each inertial sensor from the center of IP

Yaw is an isotropic motion: these TFs should be equals.

$$TF_{yaw_{geo_i}} = \frac{Yaw_{lvd_t} \cdot r}{geo_i}$$



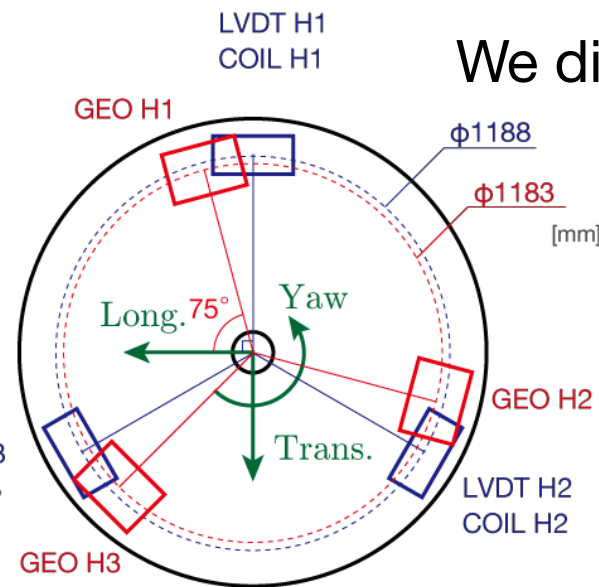
Type A: inertial sensor (II)

We diagonalize the inertial sensors in the (L,T,Y) base.

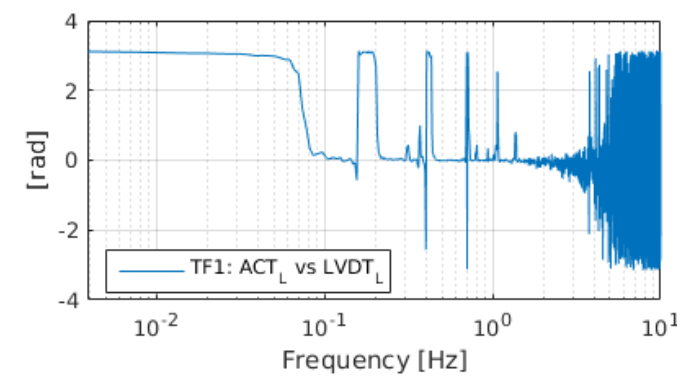
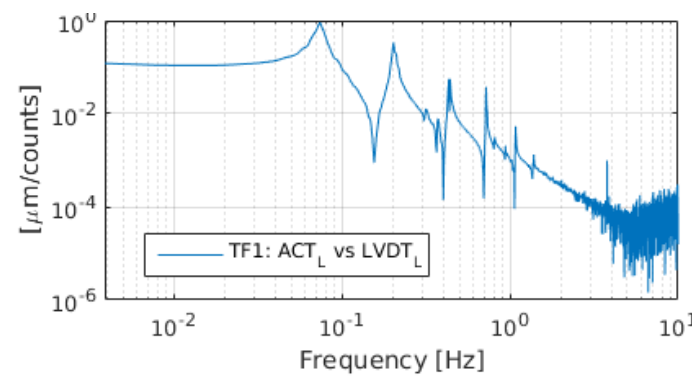
Read-out Sensing matrix

Sensors base: (H1, H2, H3) $\xrightarrow{\text{Noise injection from each diagonalized actuator (@2 Hz line)}}$ **Euler base:** (L, T, Y)

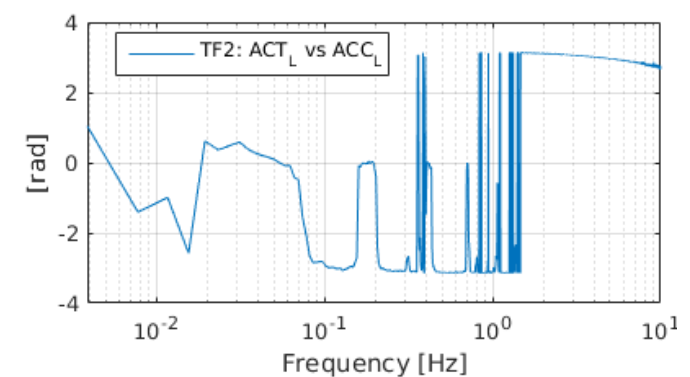
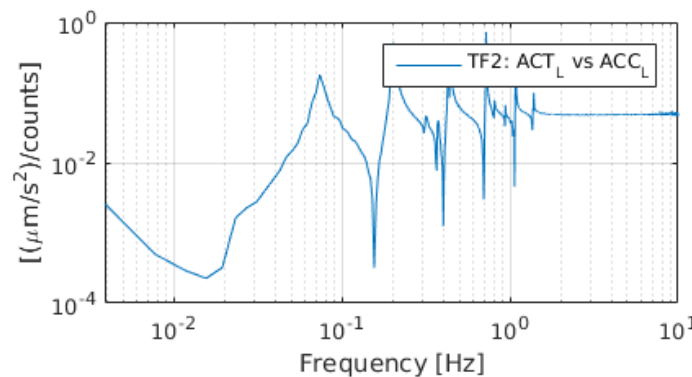
The sensor response is equalized.



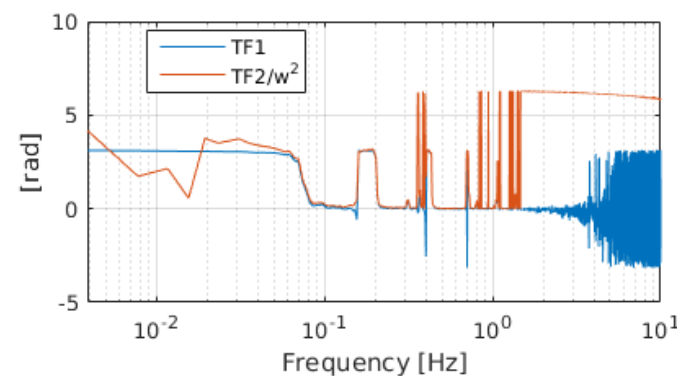
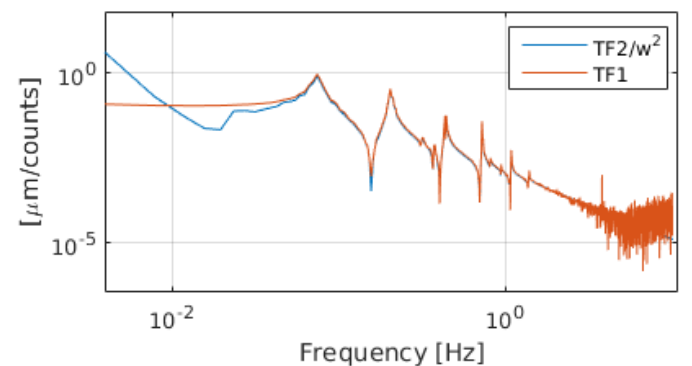
LVDT: L



ACC: L

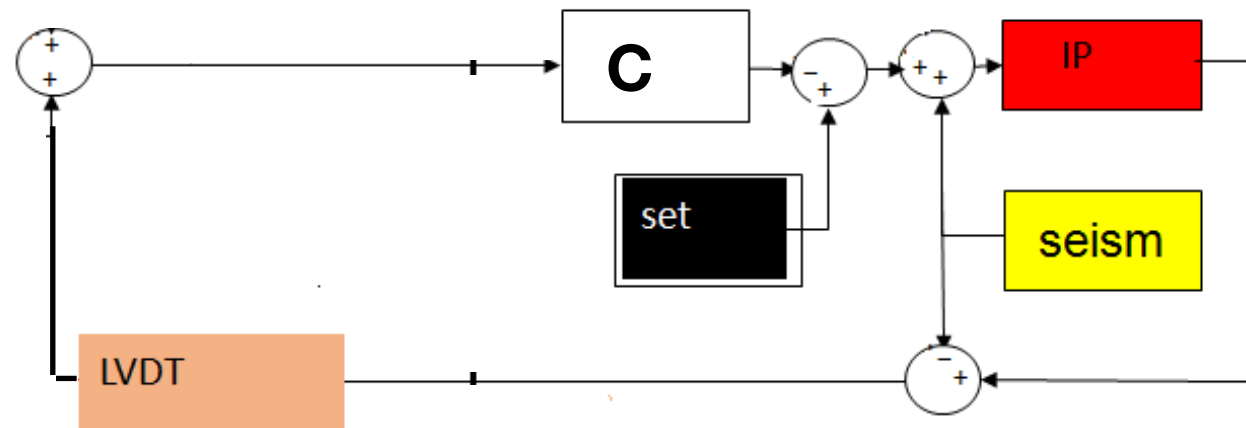


ACC & LVDT: L



Type A: Damping control

Feedback control scheme



IP= mechanical system

LVDT= is the sensor monitoring the displacement

$$x_{lvd} = x_{IP} - x_0$$

x_0 is the ground motion

C= is the damping filter

set= is the set point

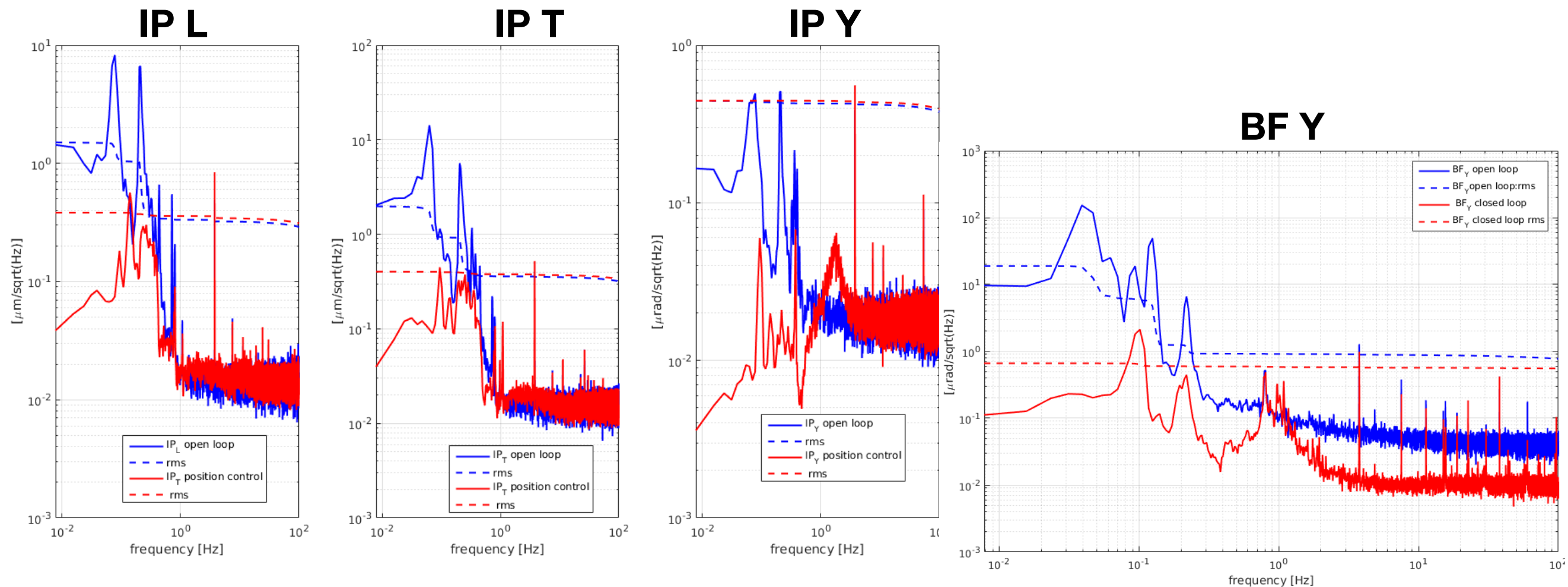
The closed loop signal is defined as

$$\tilde{S}_{iv}^{CL}(\omega) = \frac{\tilde{S}_{iv}(\omega)}{1 - \tilde{M}_i(\omega) \cdot \tilde{C}_i(\omega)}$$

In this configuration:

IP LVDT signal =
Error signal in L, T, Y

Type A: Damping control



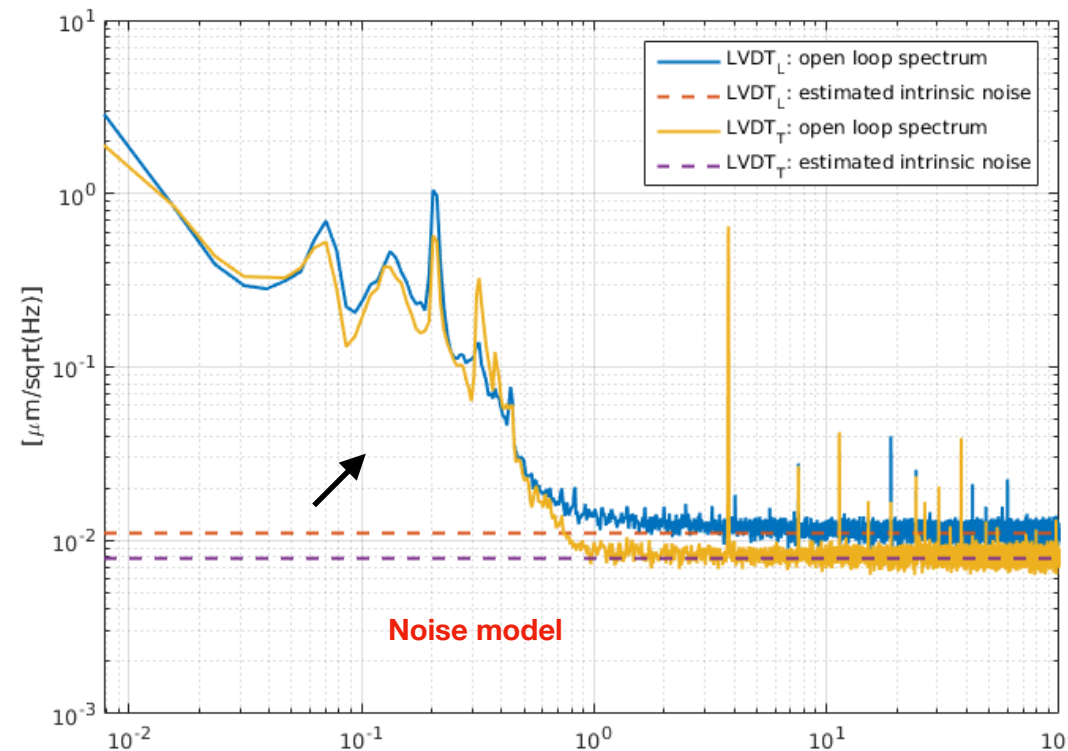
	L RMS [μm]	T RMS [μm]	Y RMS [μrad]
IP (OL)	1.5	2	0.5
IP (CL)	0.4	0.4	0.5
BF (OL)			30
BF (CL)			0.7

In this configuration we are limited by seismic noise

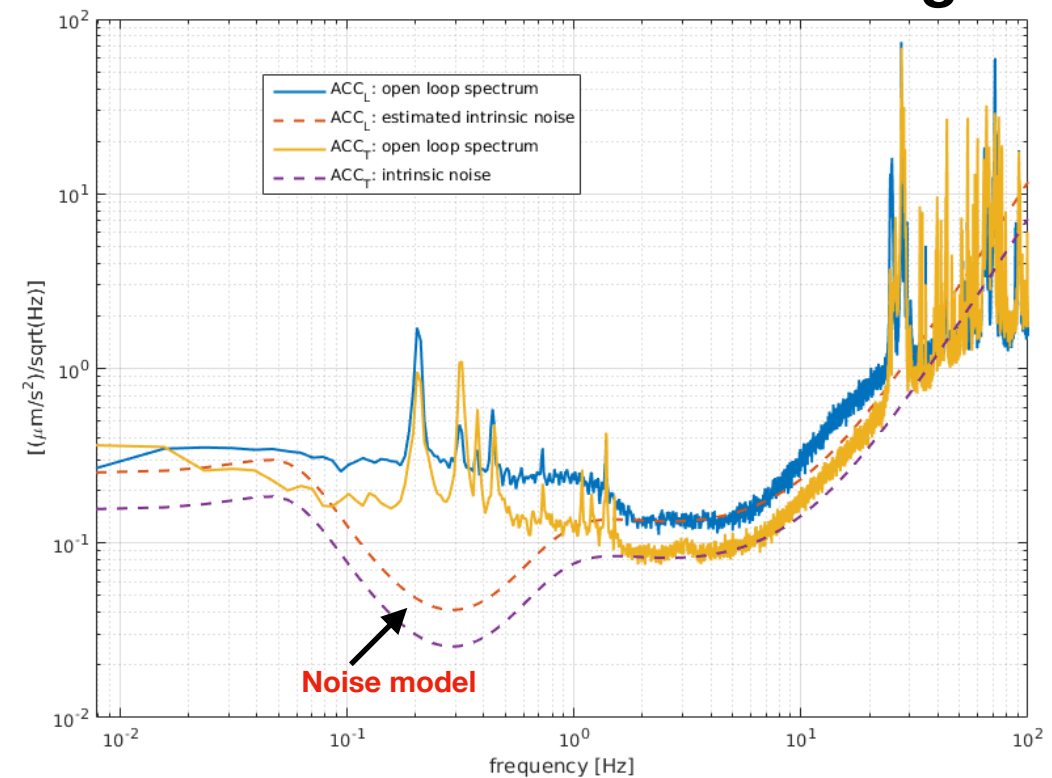
Type A: seismic noise reduction and Inertial control

Let's consider the sensors in the L,T,Y base

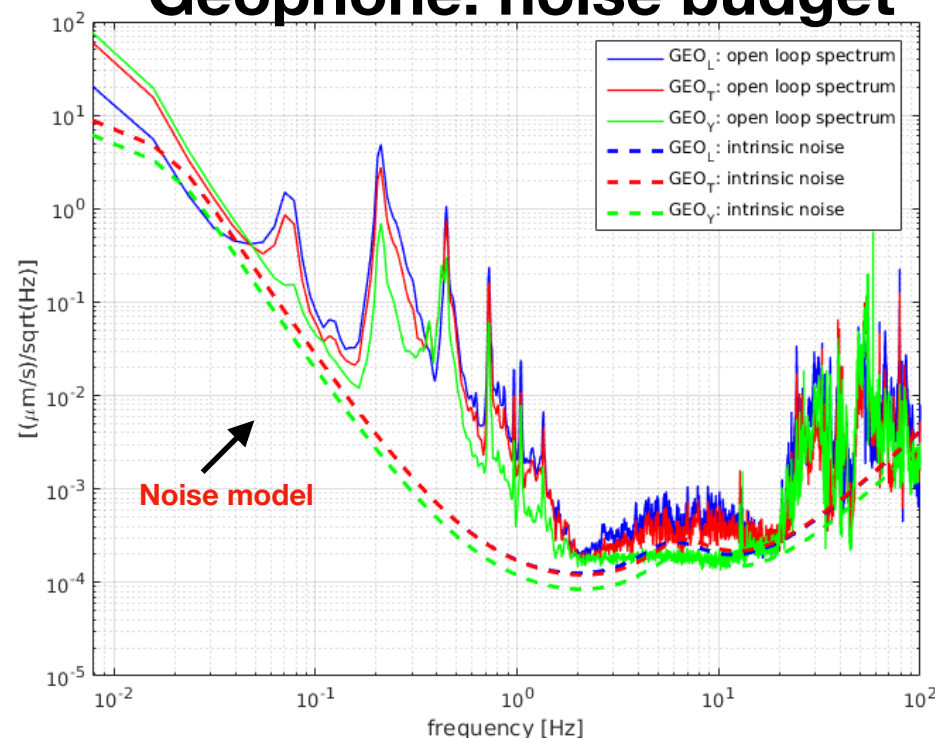
LVDT: noise budget



Accelerometer: noise budget

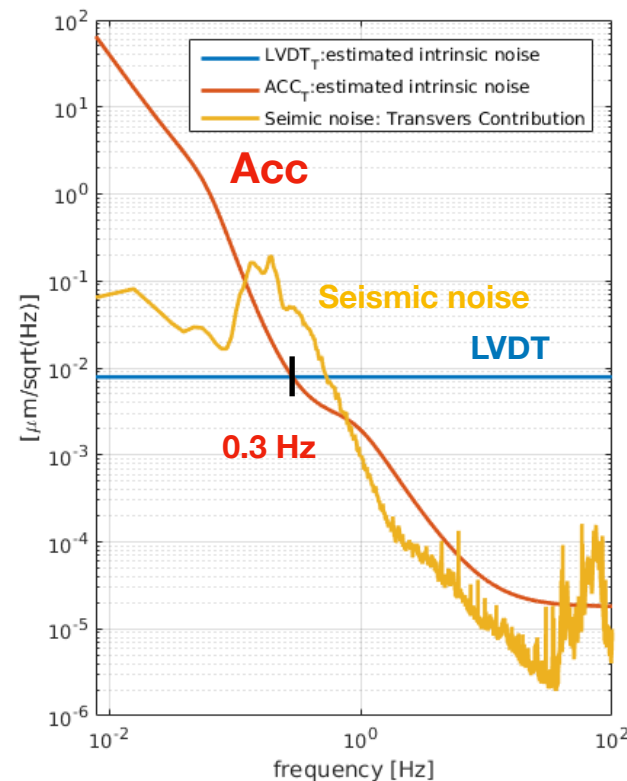
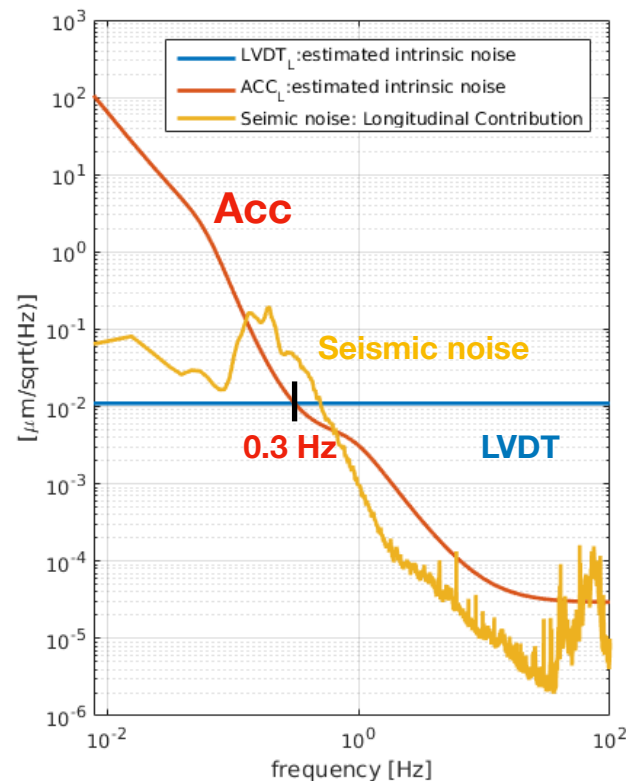


Geophone: noise budget



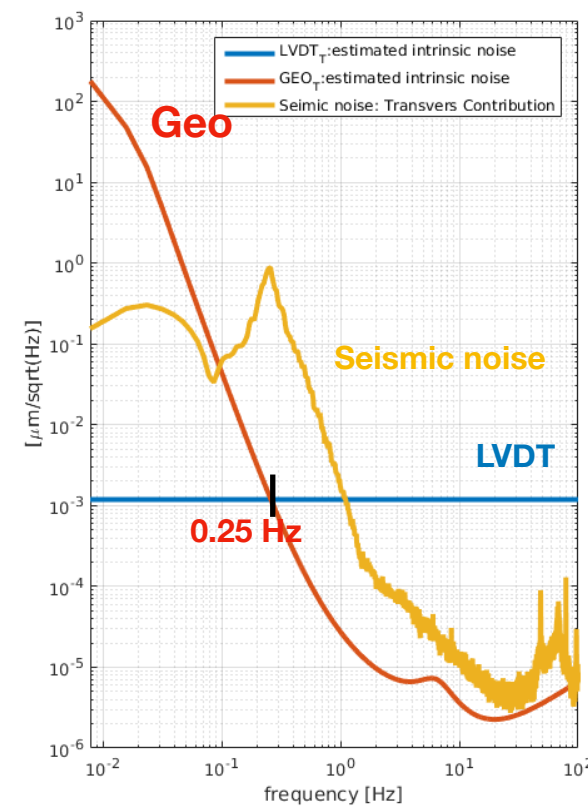
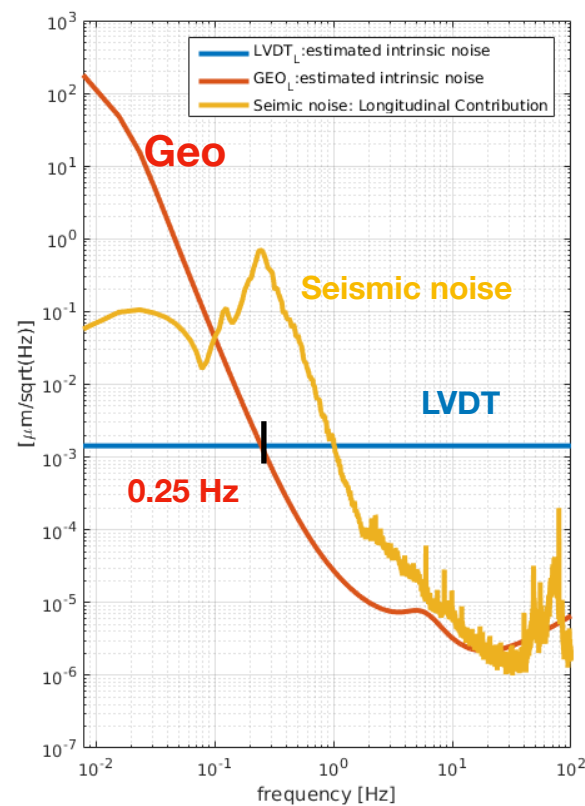
Sensors spectrum signal (LVDT, accelerometer, geophone) versus intrinsic noise (model)

Inertial control: noise budget (II)



In the range [0.1, 0.5] Hz,
the LVDT signal is spoiled
by seismic noise

Below 0.3 mHz,
the accelerometer noise is dominant



Below 0.250 mHz,
the geophone noise is dominant

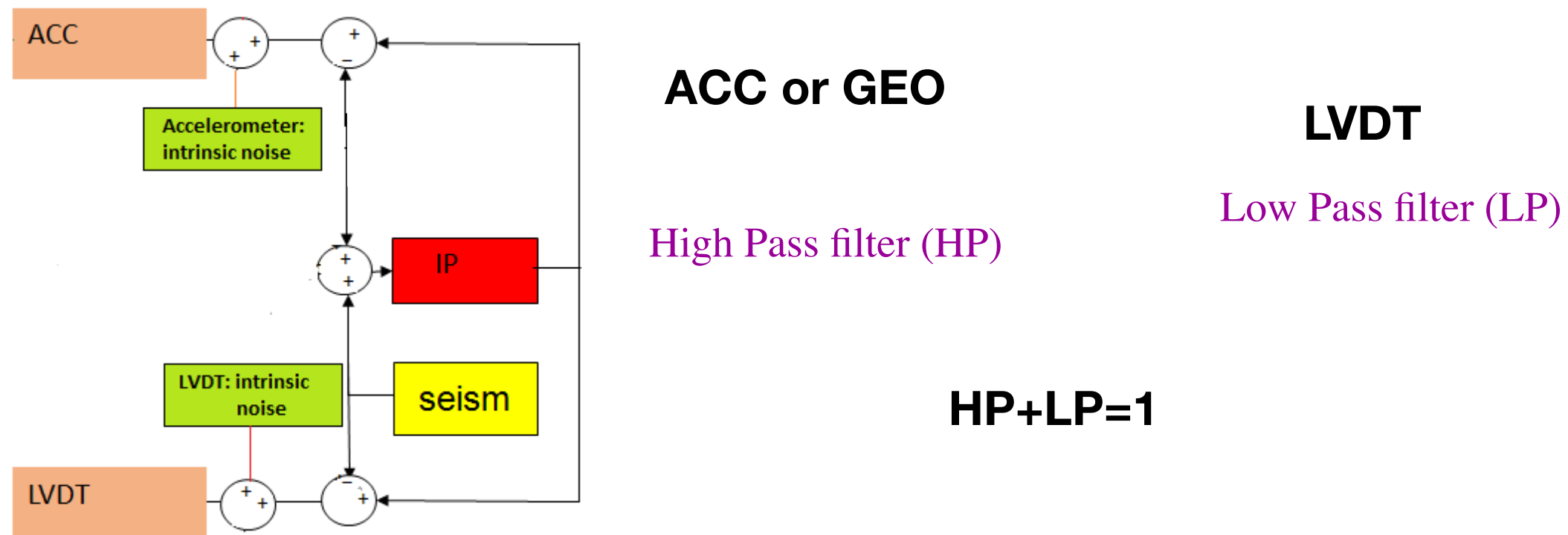
We want reduce the contribution
of the seismic noise



Blending technique

Blending technique (I)

To take the better part of both signals, the *blended virtual sensing signals*, is attained through neutral pre-filtering.



- LP filter must be shaped taking into account the background disturbance (seismic noise)
- For LP filter typical cutoff is below 100 mHz, to reduce the seismic contribution.
- For HP filter we should be careful not to reintroduce accelerometer noise.

Blended Sensor is defined as : $S(\omega) = LP(\omega) \cdot S_{LVDT}(\omega) - \omega^{-2}HP(\omega) \cdot S_{Acc}(\omega)$

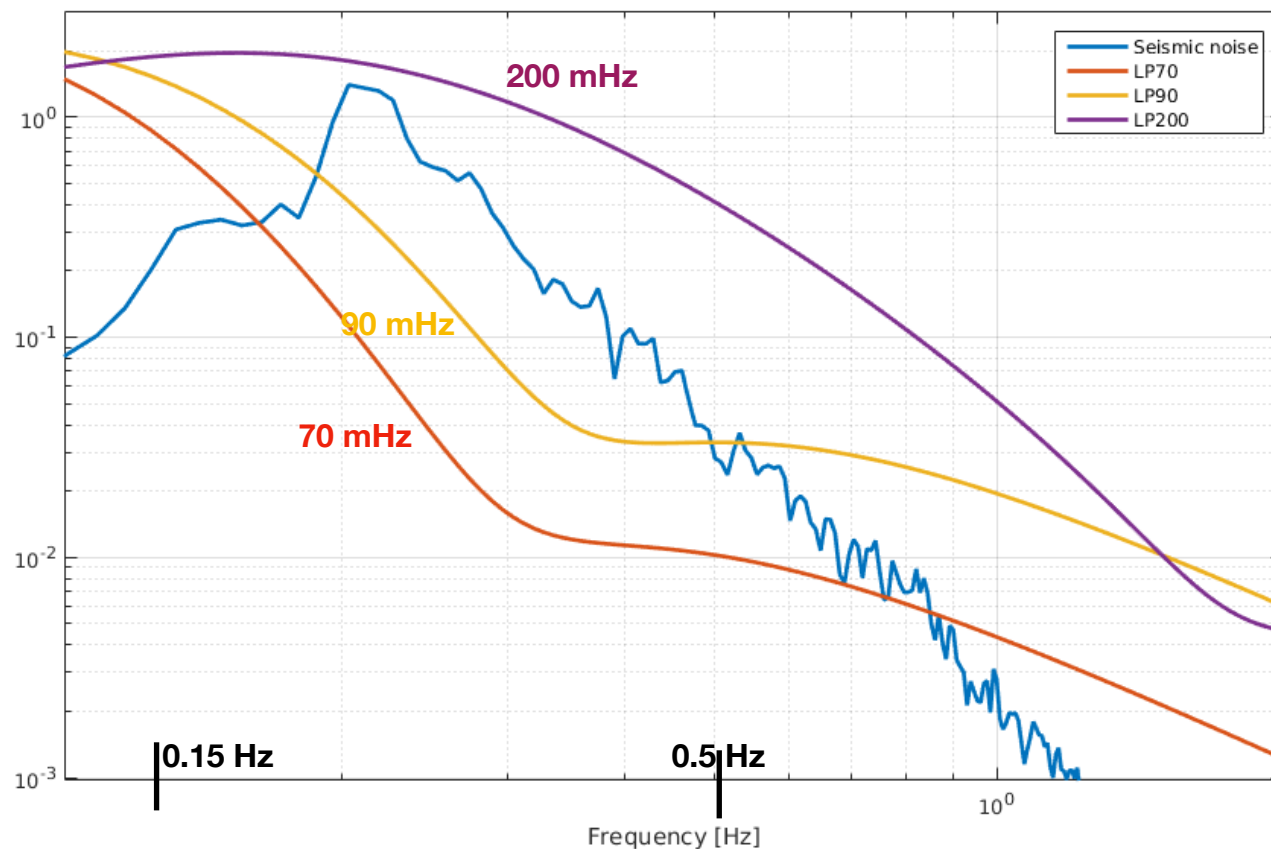
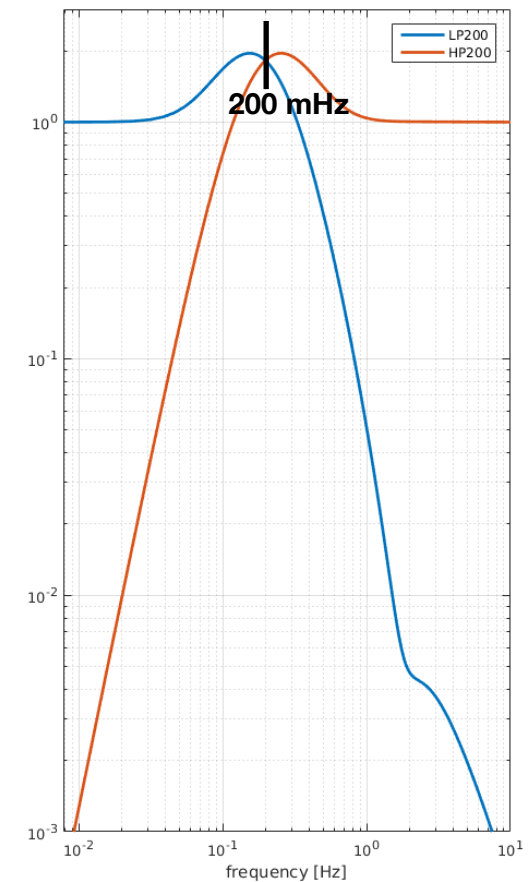
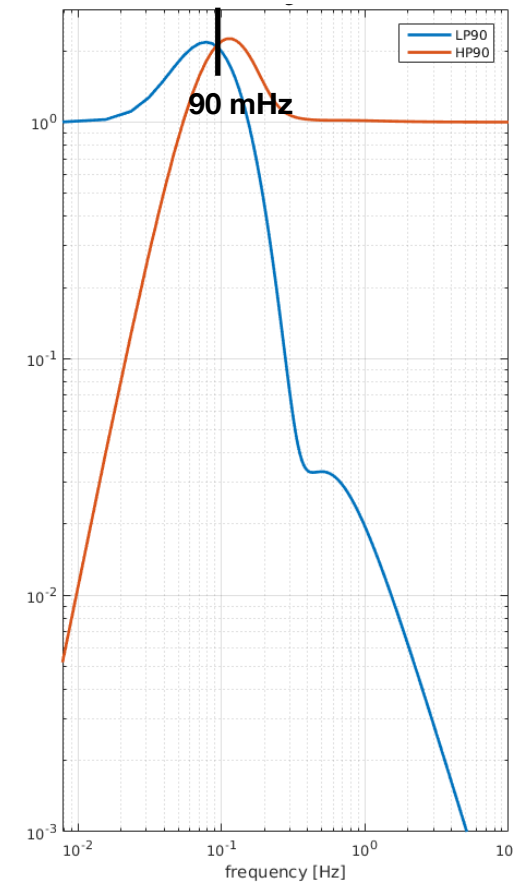
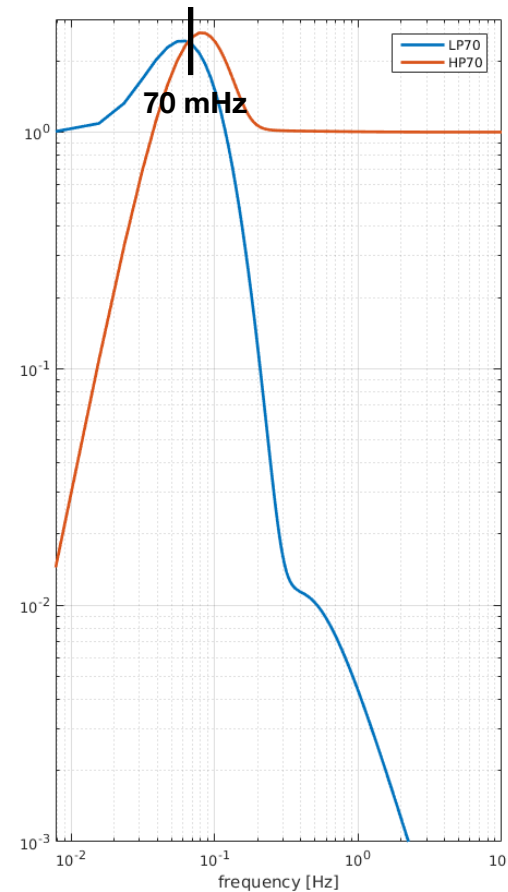
Blending technique (I)

Example of blending filters:

◆ **Blending frequency: 70 mHz**

◆ **Blending frequency: 90 mHz**

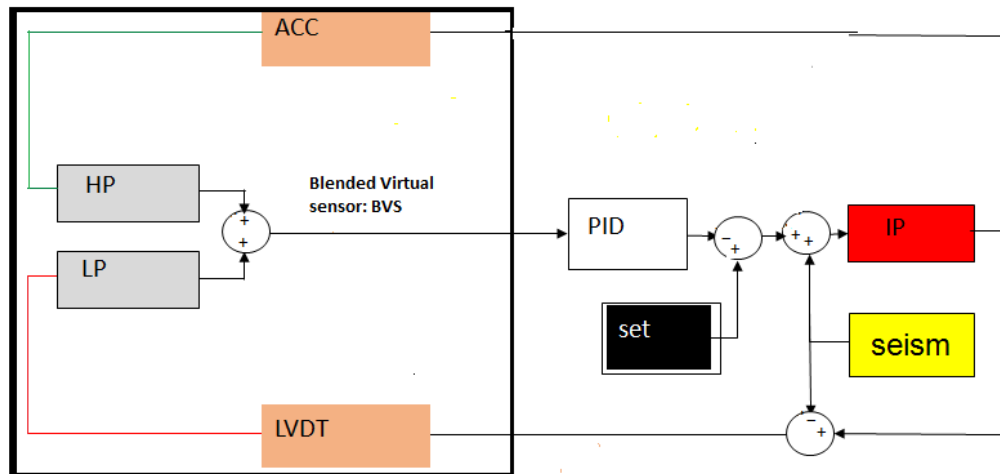
◆ **Blending frequency: 200 mHz**



Impact of each one of these strategies on the seismic noise:

The 90 mHz and 70 mHz are shaped to reduce the re-injection of seismic noise in the range [0.2 -0.5] Hz

Inertial damping: IP residual motion

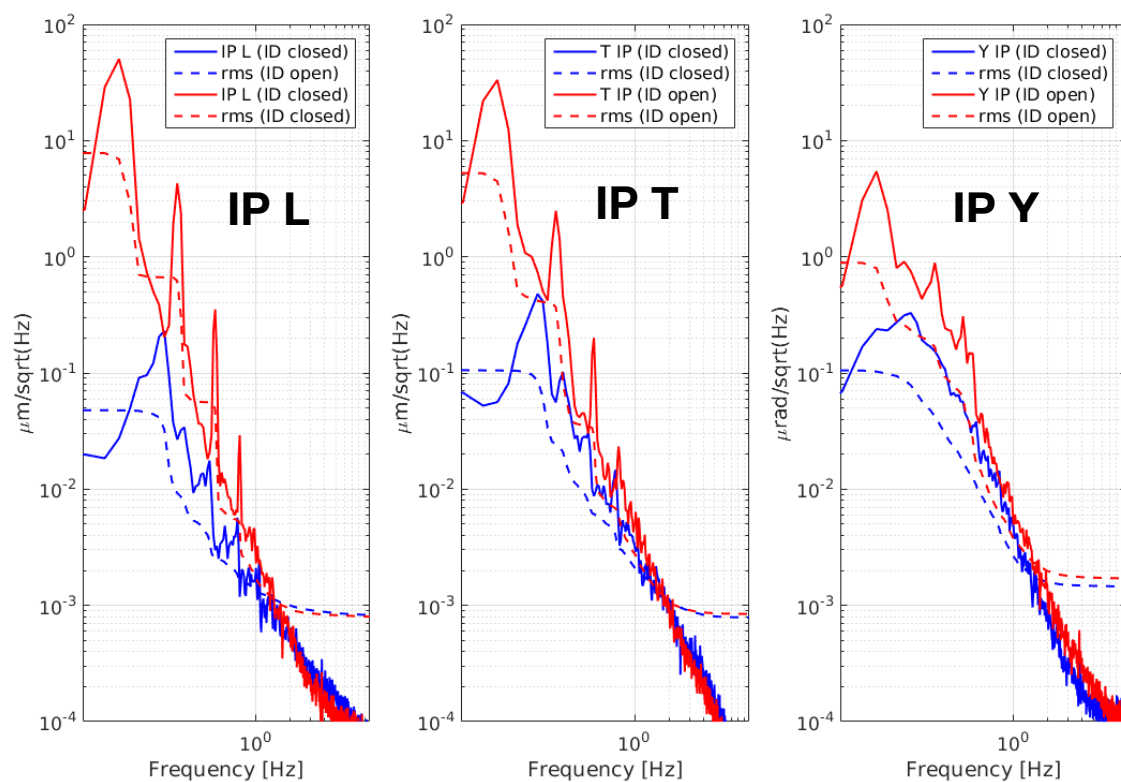


The closed loop signal is defined as

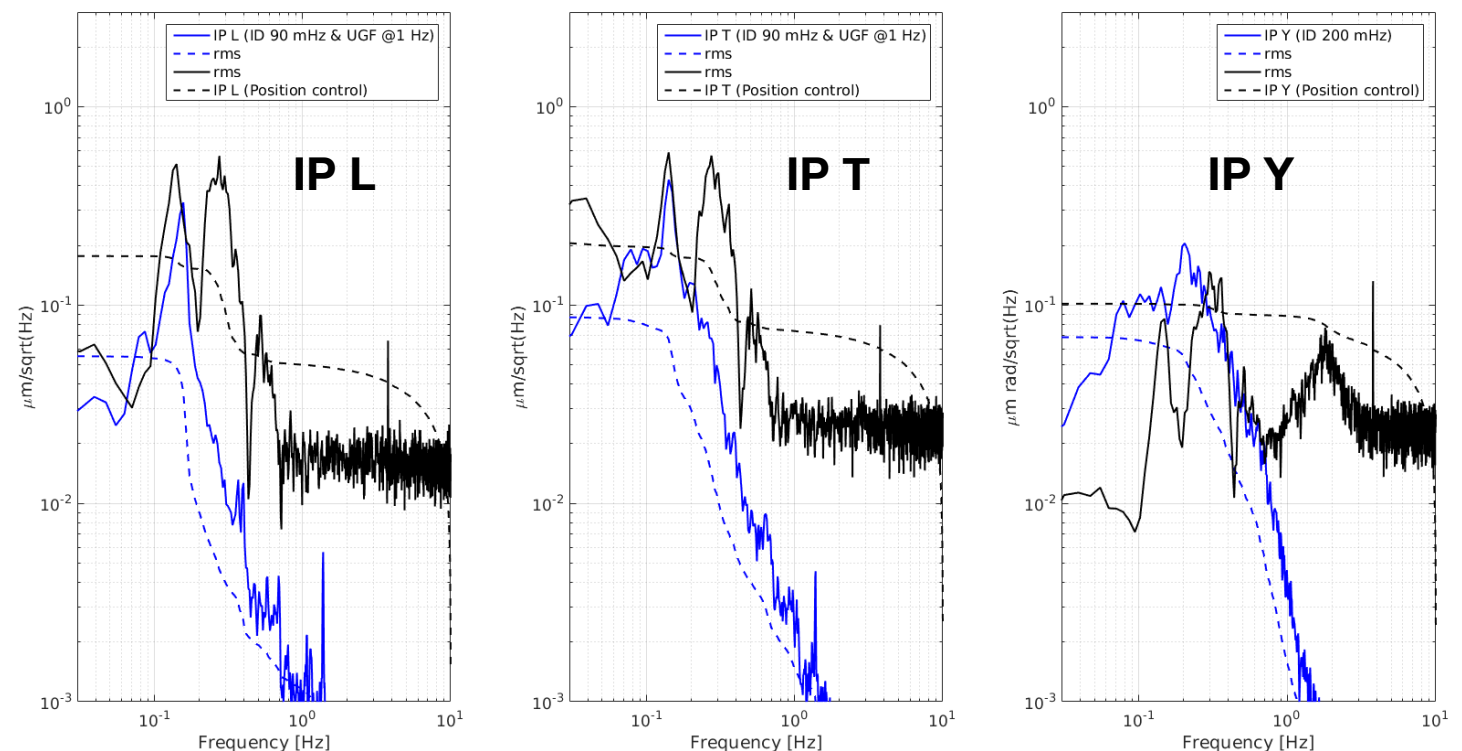
$$\tilde{S}_{iv}^{CL}(\omega) = \frac{\tilde{S}_{iv}(\omega)}{1 - \tilde{M}_i(\omega) \cdot \tilde{C}_i(\omega)}$$

IP blended signal = Error signal in L, T, Y

In this configuration the residual motion of the IP is

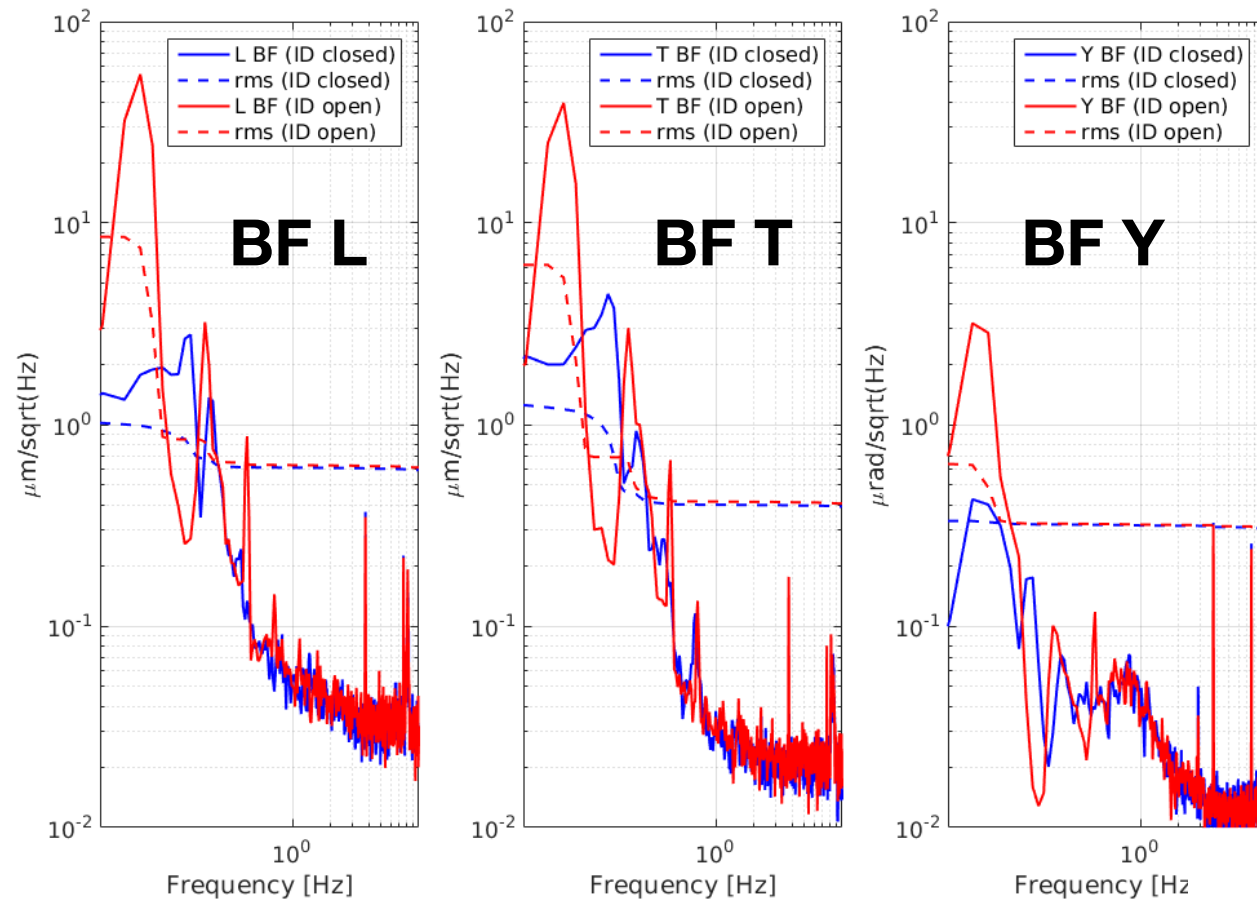


**Open loop versus closed loop
with Inertial Damping**



Closed loop: LVDT is the error signal
Closed loop: blended signal is the error signal

Inertial damping: BF & Test Mass (TM) residual motion

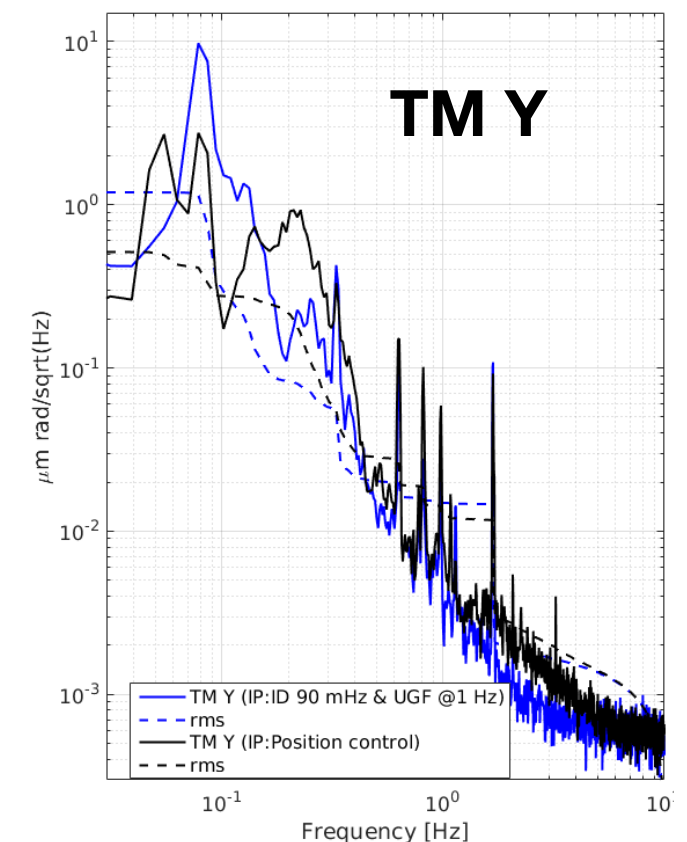
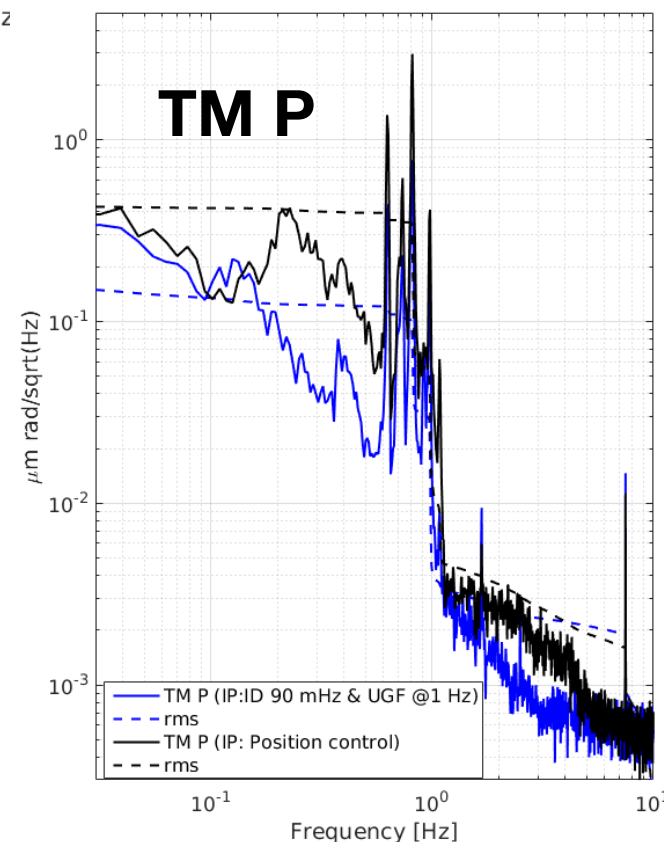


In this configuration:

- ◆ **BF L: damp off**
- ◆ **BF T: damp off**
- ◆ **BF Y: damp on**

In this configuration:

- ◆ **MN & TM P: damp off**
- ◆ **MN & TM Y: damp off**



Conclusion and next steps

- We have diagonalized sensors and actuators
- We applied the bending technique to ITMX
 - L and T blending frequency: 90 mHz
 - Yaw blending frequency: 200 mHz
- Thanks to the implementation of the inertial damping we observed a reduced motion of IP, BF and TM

	L RMS [μm]	T RMS [μm]	Y RMS [μrad]	P RMS [μrad]
IP	0,05	0,08	0,08	
BF	1	1	0,3	
TM			1	0,2

- **IP inertial damping ON**
- **YAW BF damping ON**
- **All other d.o.f NOT DAMPED**

- The test on ITMX shows that **inertial damping (ID) reduces the test mass motion more than the position control with only LVDTs**
- **We need to implement the ID on all the type A suspension also by using the geophone.**

Thanks for your attention!