

# Prospects for improving the sensitivity of KAGRA gravitational wave detector

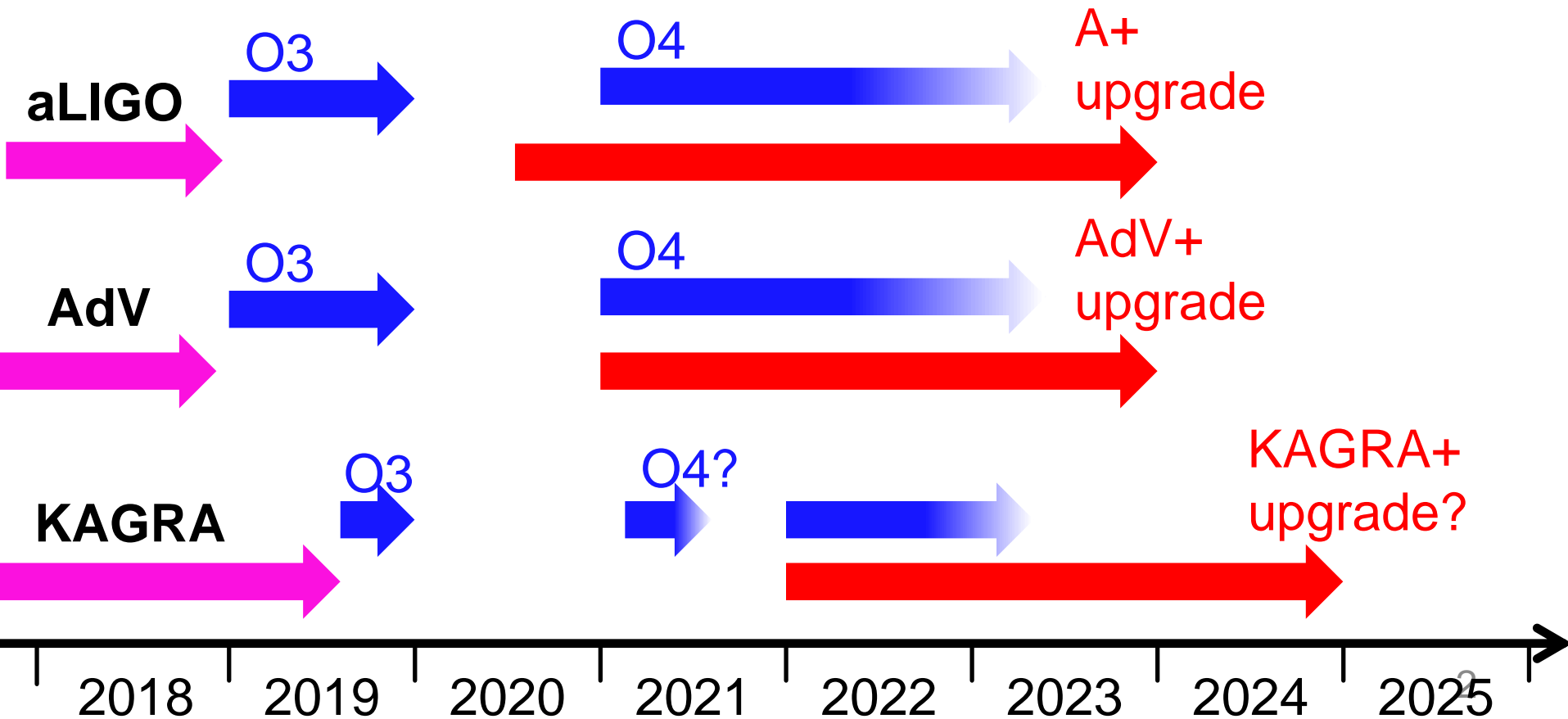
Yuta Michimura

Department of Physics, University of Tokyo

Masaki Ando, Enomoto, Yutaro Enomoto; Haino, Sadakazu; Hayama, Kazuhiro; Hirose, Eiichi; Itoh, Yousuke; Kinugawa, Tomoya; Komori, Kentaro; Leonardi, Matteo; Mio, Norikatsu; Nagano, Koji; Nakano, Hiroyuki; Nishizawa, Atsushi; Sago, Norichika; Shibata, Masaru; Shinkai, Hisaaki; Takeda, Hiroki; Tanaka, Takahiro; Tanioka, Satoshi; Wei, Li-Wei; Yamamoto, Kazuhiro

# Upgrading Current GW Detectors

- Gravitational wave astronomy has begun
- Sensitivity improvements allow **more detections** and **more precise** source parameter estimation



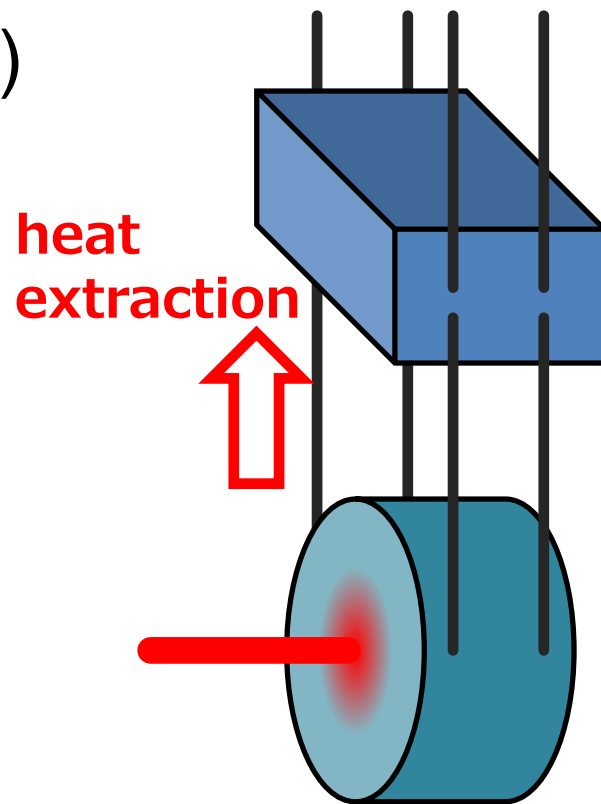
# Upgrading KAGRA is Tricky

- Only **cryogenic** interferometer among 2G
- Not trivial to do both
  - high power (**400 kW** on mirror)
  - low temperature (**20 K**)
- Sapphire fibers to extract heat
  - thinner and longer
  - for thermal noise reduction



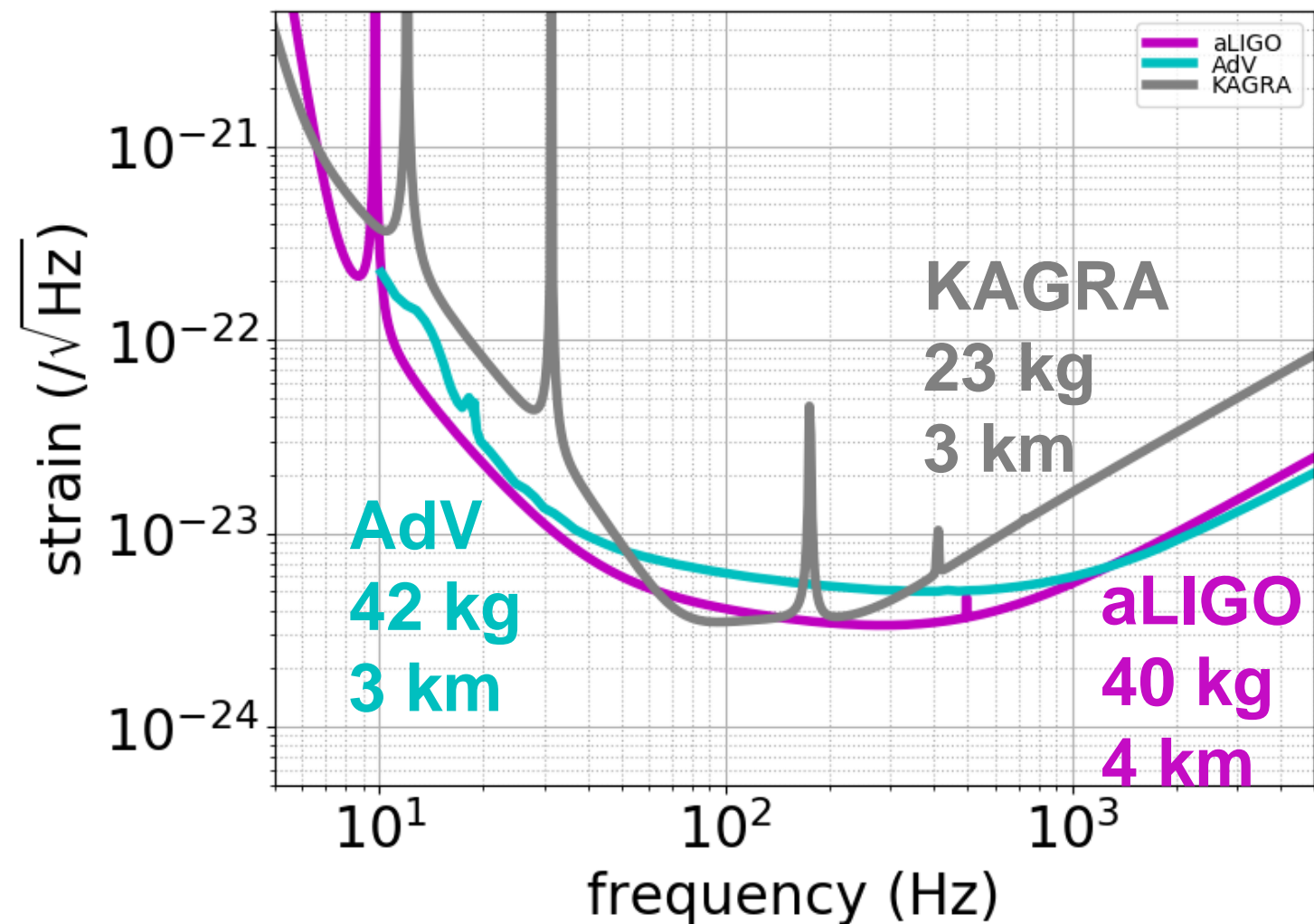
**Dilemma**

thicker and shorter  
for heat extraction



# 2G Sensitivity Comparison

- Not good at low freq. because of **thick and short** fiber (35 cm,  $\phi 1.6$  mm) to extract heat, and **lower mass**

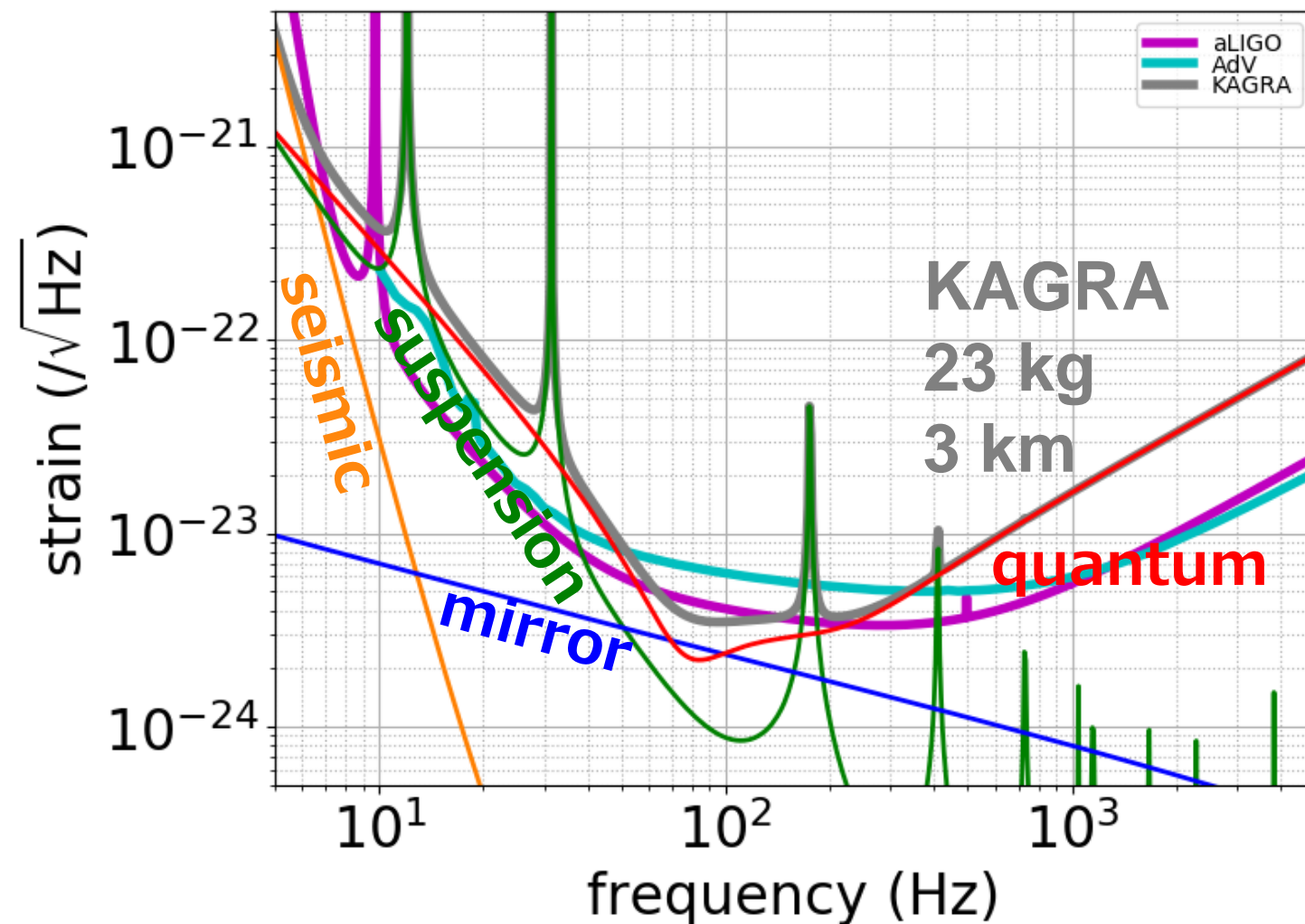


23 kg was the largest available sapphire mirror

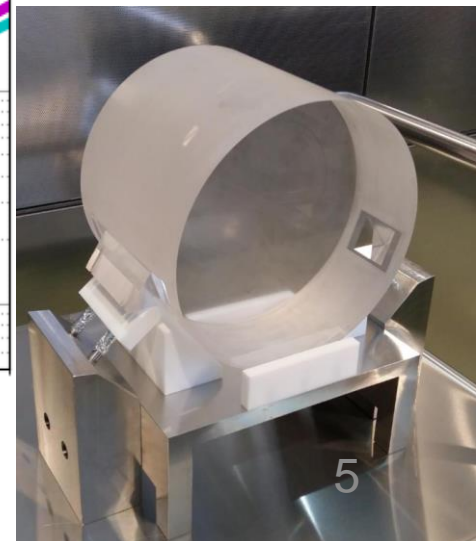


# 2G Sensitivity Comparison

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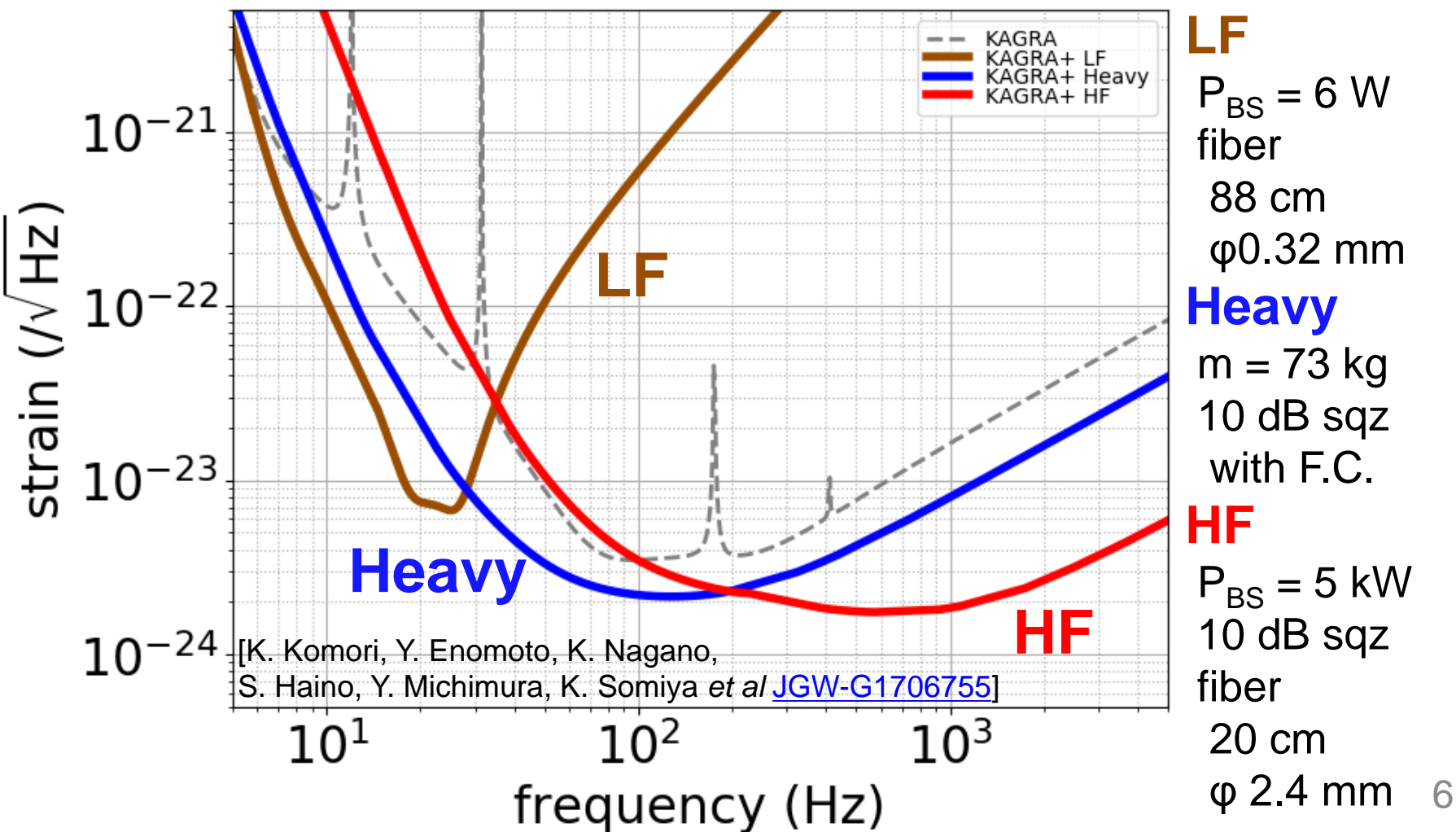


23 kg was the largest available sapphire mirror



# 3 KAGRA+ Concepts to Start With

- Low power to focus on **low frequency**, high power to focus on **high frequency**, and **heavier mass**



# Science Case Study

- Although **LF** has the best inspiral range for heavy BBH ( $\sim 100M_{\text{sun}}$ ), narrow band was **not favorable**

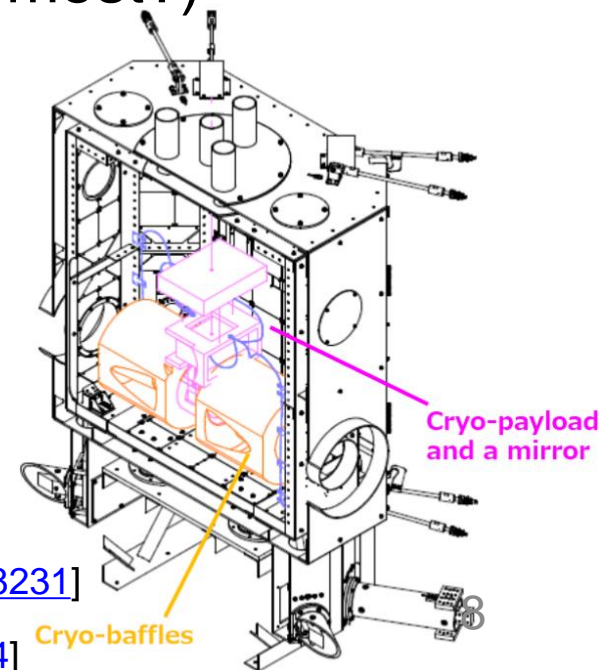
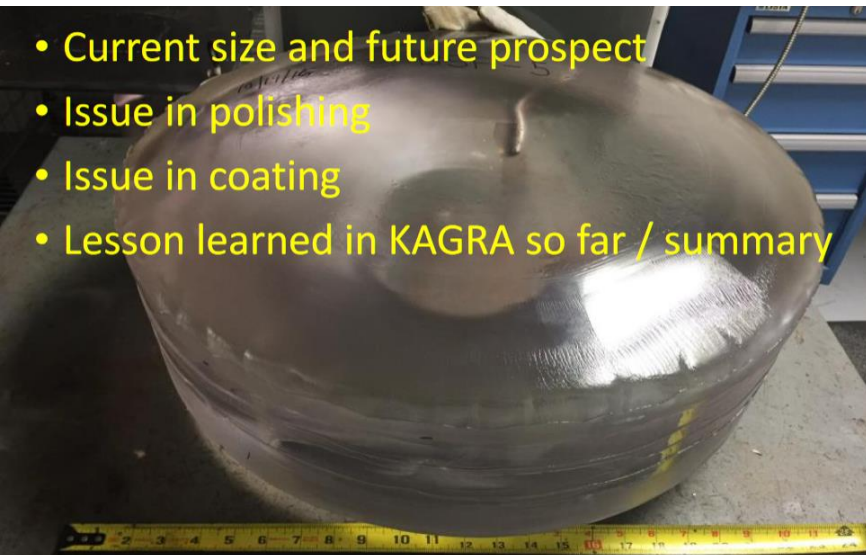
	bKAGRA	LF	Heavy	HF
test of GR with BH ringdown	×	×	△	○
existence of IMBH from hierarchical growth	△	△	○	△
existence of stellar-mass BBH from popIII	×	×	×	×
sky localization for BBH (identifying host galaxy)	△	×	○	○
pulsar ellipticity	×	×	△	○
NS equation of state	×	×	△	○

[Based on inputs from K. Hayama, Y. Itoh, T. Kinugawa, H. Nakano, A. Nishizawa, N. Sago, M. Shibata, H. Shinkai, T. Tanaka, *et al* [JGW-G1707125](#)]

# Feasibility Study: Heavier Mirror

- **Larger sapphire** bulk available, but requires R&D for polishing and coating, **needs time and money**
  - $\phi$  55 cm x t 30 cm (**~280 kg**) mirror would be possible in the future
  - Current one ( $\phi$  22 cm x t 15 cm, 23 kg) more than 1 year to polish, \$0.6M / mirror
  - Current cryostat is quite full (**40 kg** at most?)

- Current size and future prospect
- Issue in polishing
- Issue in coating
- Lesson learned in KAGRA so far / summary



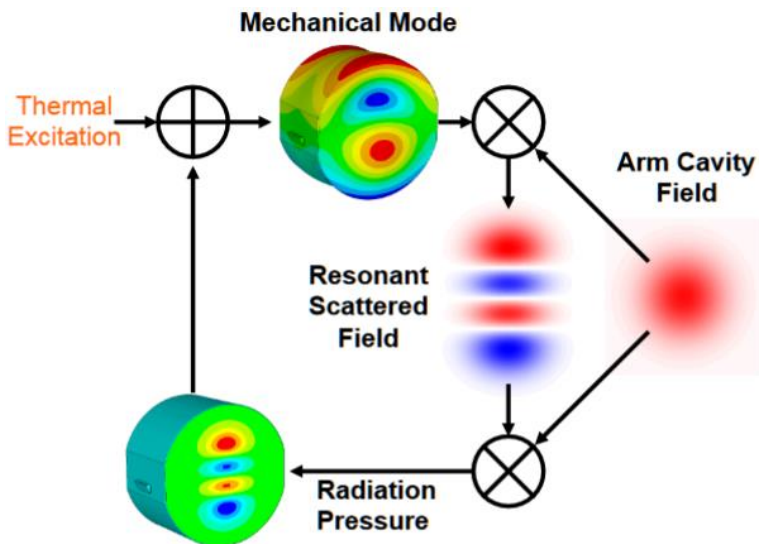
[K. Somiya, [JGW-G1808231](#)]

[E. Hirose [JGW-G1707484](#)]

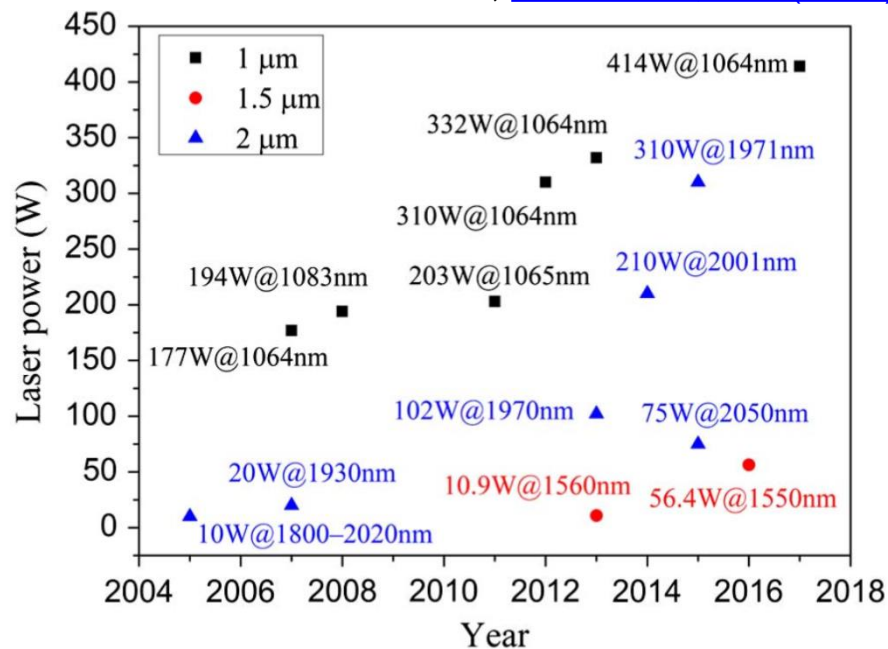


# Feasibility Study: High Power

- Higher power laser source at **400 W** would be available, but operation is **tough**
  - thermal compensation
  - parametric instability
  - radiation pressure induced instability etc...
- Could be OK with cryogenic sapphire?



S. Fu *et al*, [JOSA B 34, A49 \(2017\)](#)

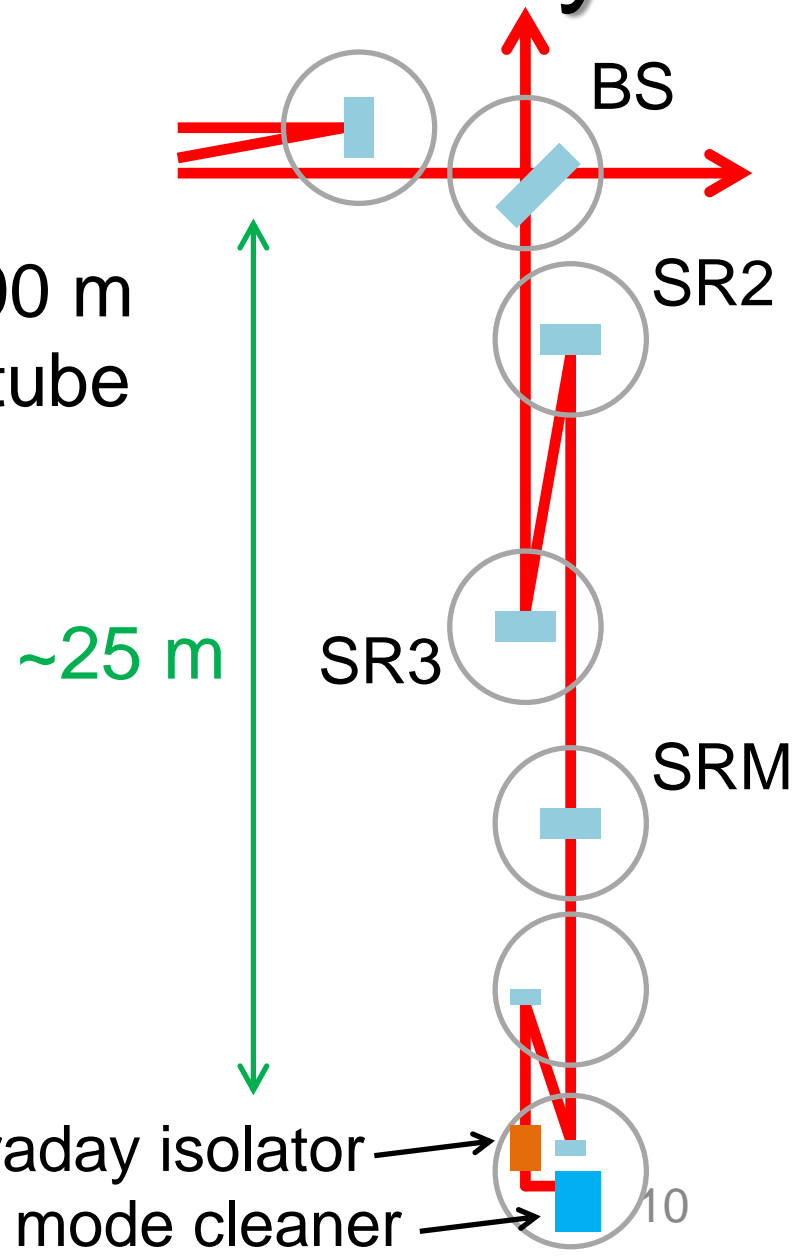
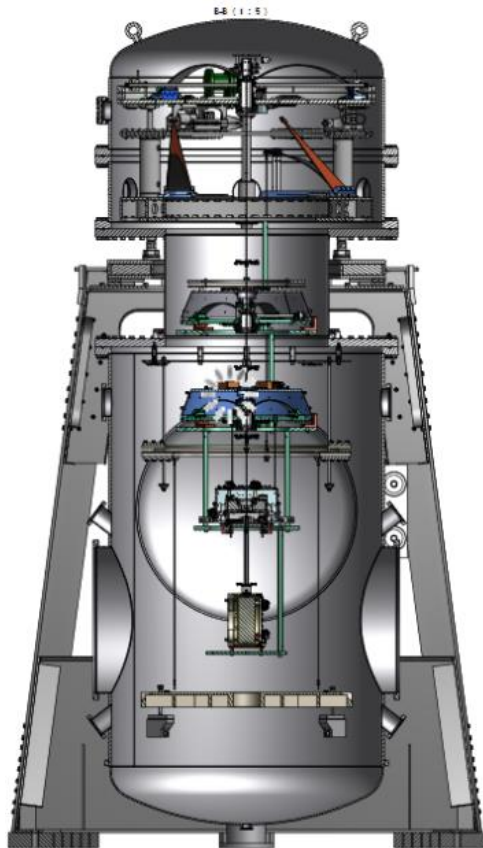


M. Evans *et al*, [PRL 114, 161102 \(2016\)](#)

**Fig. 7.** Output power evolution of CW single-frequency amplifiers in all-fiber format operating in 1, 1.5, and 2  $\mu\text{m}$  regions.

# Feasibility Study: Filter Cavity

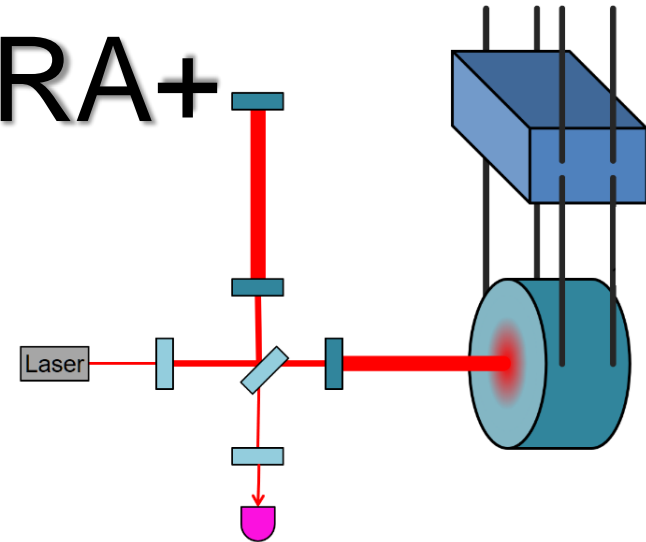
- One core optic per tank, not very crowded
- **~30 m** could be OK, but  $>100$  m would require new vacuum tube



output faraday isolator →  
output mode cleaner →

# Near Term KAGRA+

- Within ~5 years, ~\$5M



- Candidates would be

A. 40 kg mirror with better coating (>\$4M?)  
and new sapphire fibers (\$1M?)

(use existing cryostat and Type-A tower)

B. 400 W laser (\$3M?) with squeezing (\$1M?)

and new sapphire fibers (\$1M?)

C. Frequency dependent squeezing (\$3M?)

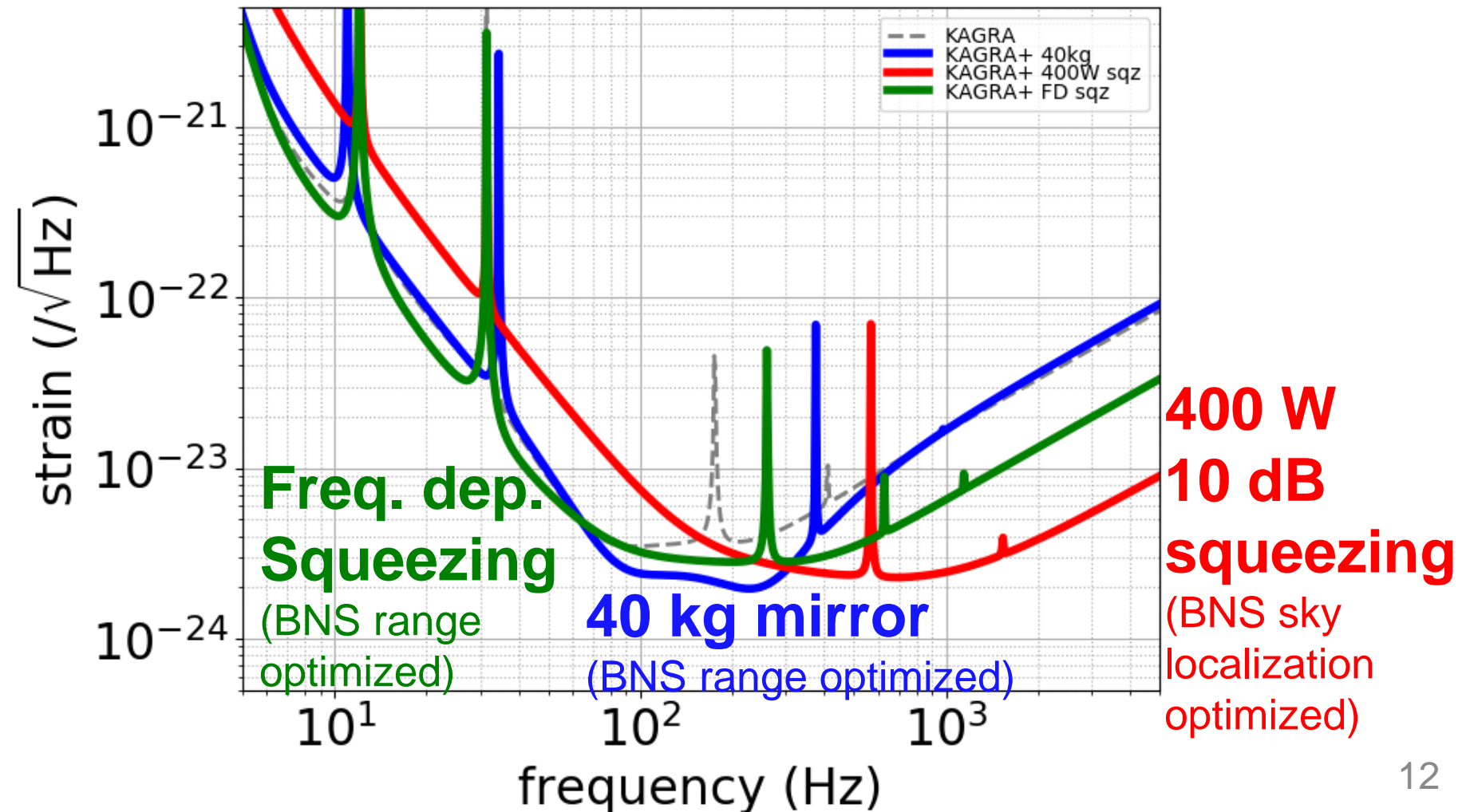
and new sapphire fibers (\$1M?)

- Sensitivity optimization with particle swarm

Y. Michimura et al, [Phys. Rev. D 97, 122003 \(2018\)](#)

# Near Term Candidates

- Within ~5 years, ~\$5M



# Summary of Near Term Plans

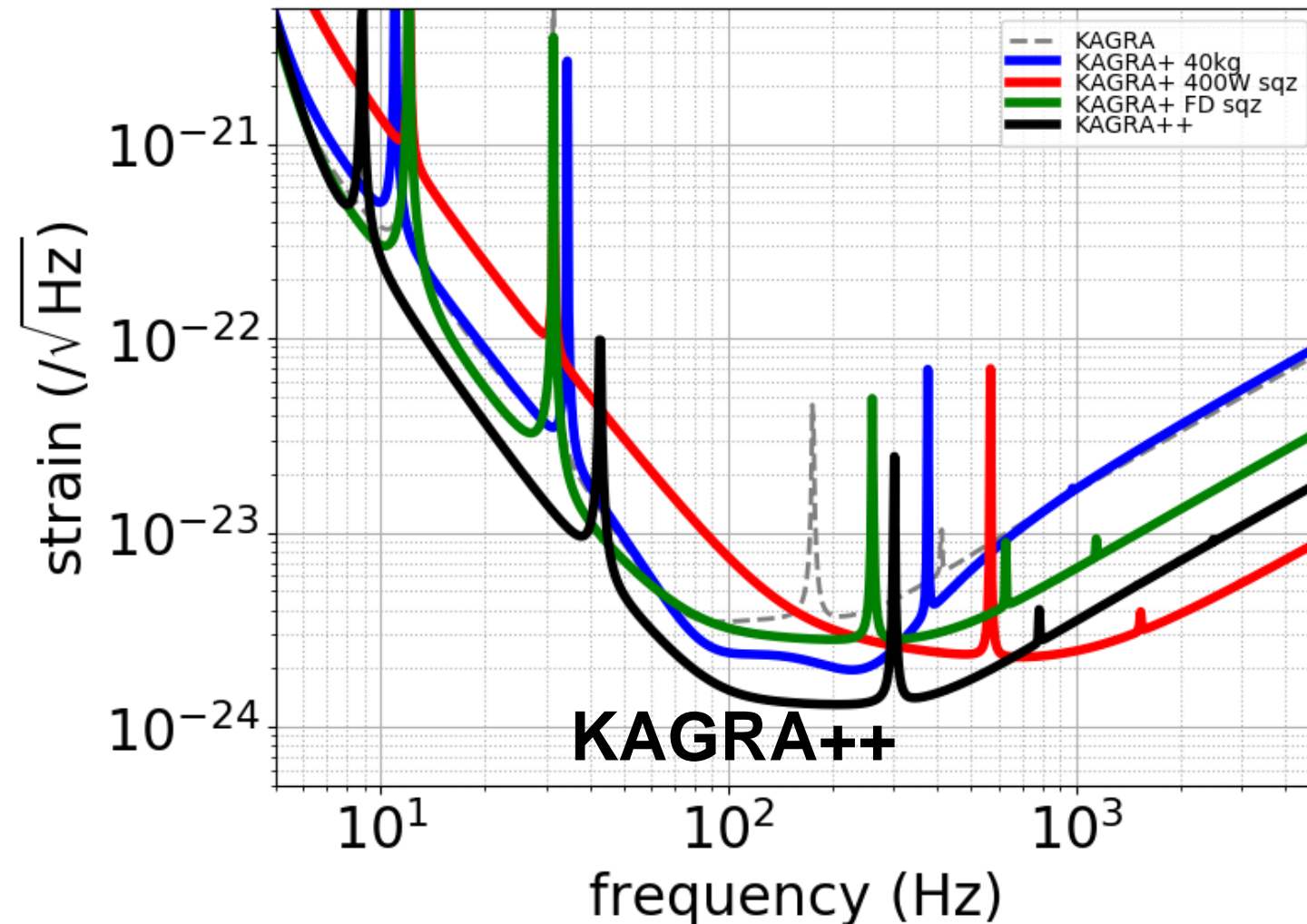
- **A.** New mirror takes time to fabricate
- **B.** High power operation is tough
- **C.** Does it fit in the facility?



	Inspiral range (Mpc)			BNS localize (deg <sup>2</sup> )
	BBH100	BBH30	BNS	
bKAGRA	353	1095	153	0.183
<b>A. 40 kg mirror</b>	339	1096	<b>213</b>	0.151
<b>B. 400 W laser sqz</b>	117	314	123	<b>0.114</b>
<b>C. Freq. dep. sqz</b>	<b>470</b>	<b>1177</b>	181	0.135

# Longer Term Candidate

- 100 kg mirror with 1/2 coating thermal, 320 W input, 10 dB squeezing with 100 m filter cavity

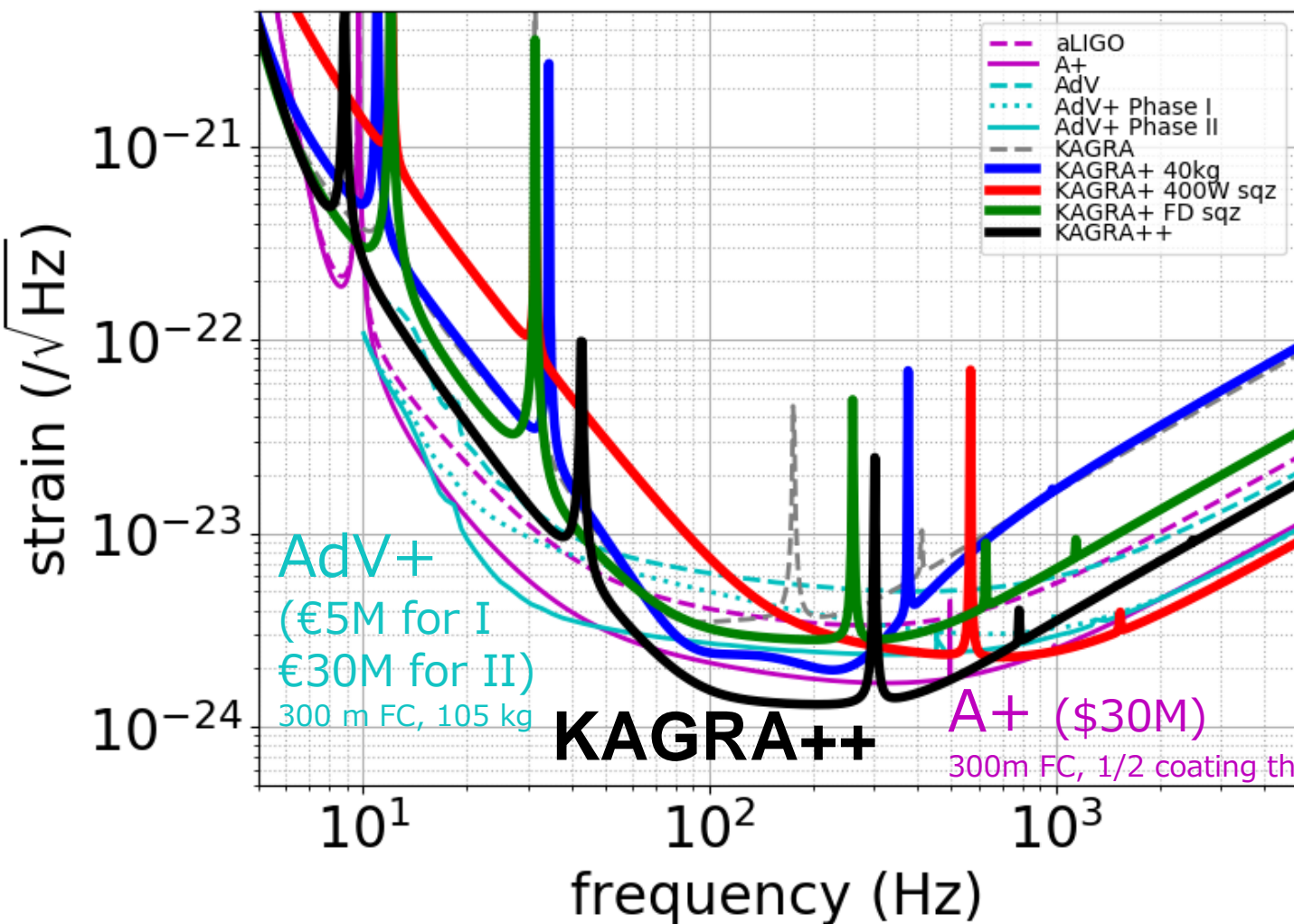


BNS range  
reaches  
**355 Mpc**

Within  
~ 10 years  
~ \$20M?

# Comparison between 2G and 2G+

- **A+**: 325 Mpc  
**AdV+ Phase I**: 160 Mpc, **Phase II**: 300 Mpc



aLIGO curve from  
[LIGO-T1800044](https://arxiv.org/abs/1804.07333)  
(updated ver)

A+ curve from  
[LIGO-T1800042](https://arxiv.org/abs/1804.07333)

AdV and AdV+ curves  
from  
[VIR-0325B-18](https://arxiv.org/abs/1804.07333)

KAGRA curve from  
[JGW-T1707038](https://arxiv.org/abs/1707.03808)



# Possible Upgrade Strategy

- Still **under discussion** among KAGRA collaboration

Filter cavity R&D



Mirror upgrade

Heavier mirror R&D, fabrication



Filter cavity

Coating R&D

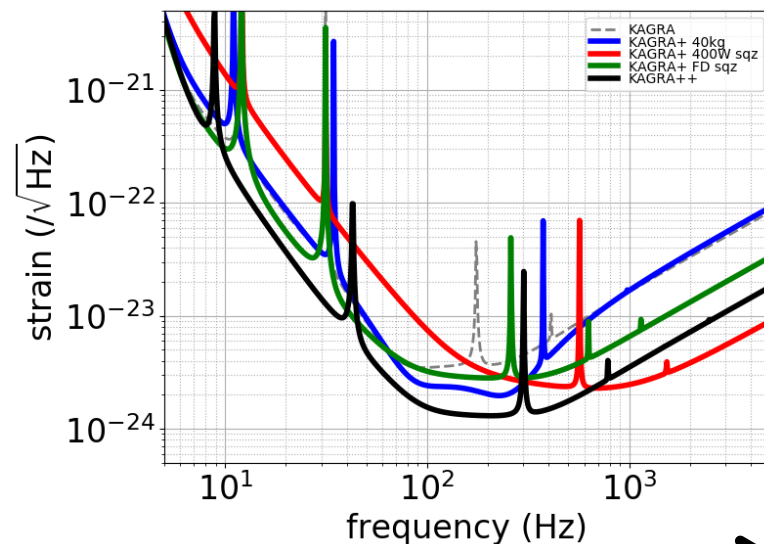


Higher power upgrade?

Higher power R&D



Realize KAGRA

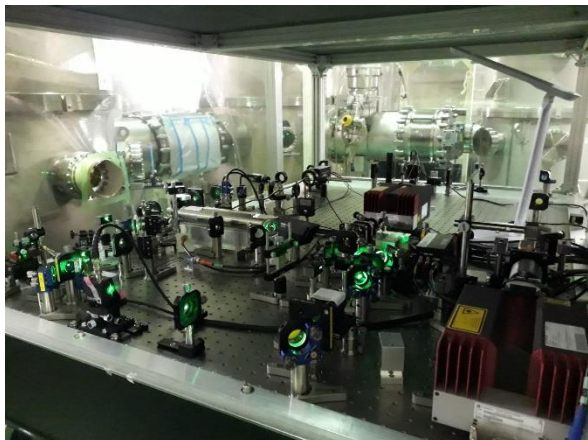


2018 | 2019 | 2020 | 2021 | 2022 | 2023 | 2024 | 2025 | 2026 | 2027 | 2028 | 16



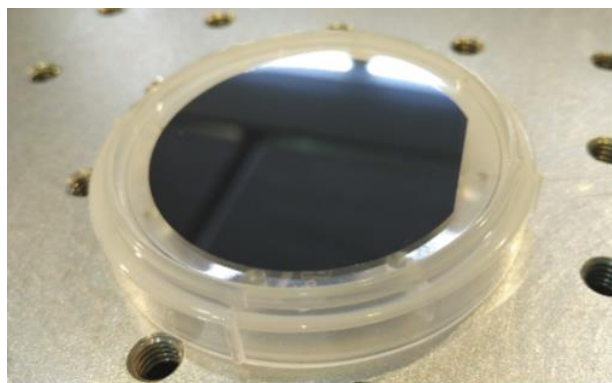
# R&D Activities for Upgrades

- 300 m filter cavity experiment at TAMA300  
E. Capocasa *et al*, [PRD 93 082004 \(2016\)](#) and [arXiv:1806.10506](#)

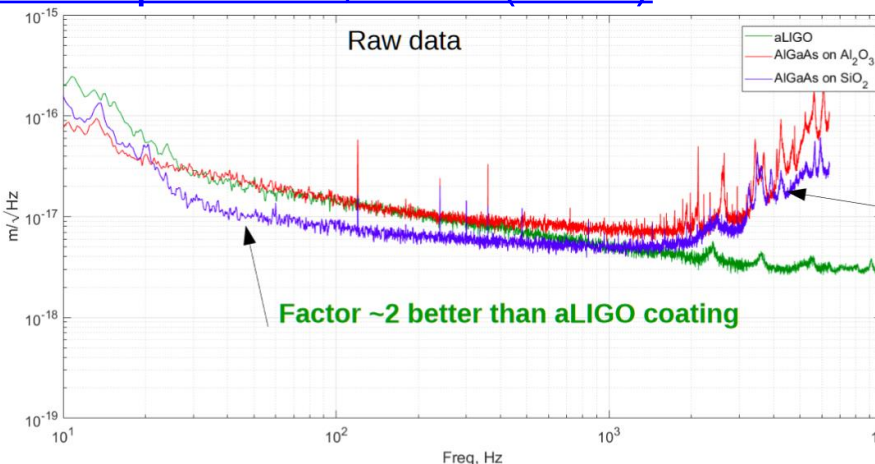


[M. Leonardi *et al*,  
[JGW-G1808310](#)]

- Characterization of crystalline coating on sapphire  
M. Marchio *et al*, [Optics Express 26, 6114 \(2018\)](#)



2 inches diameter



[M. Marchio *et al*,  
[JGW-G1808310](#)]

# R&D Activities for Upgrades

- Coating thermal noise experiment at cryogenic temperatures
- Quantum radiation pressure noise experiment with mg-scale mirror and bar

N. Matsumoto, K. Komori *et al*,  
[PRA 92, 033825 \(2015\)](#)

- Demonstration of parametric signal amplification

K. Somiya *et al*,  
[Phys. Lett. A 380, 521 \(2016\)](#)

..... and more



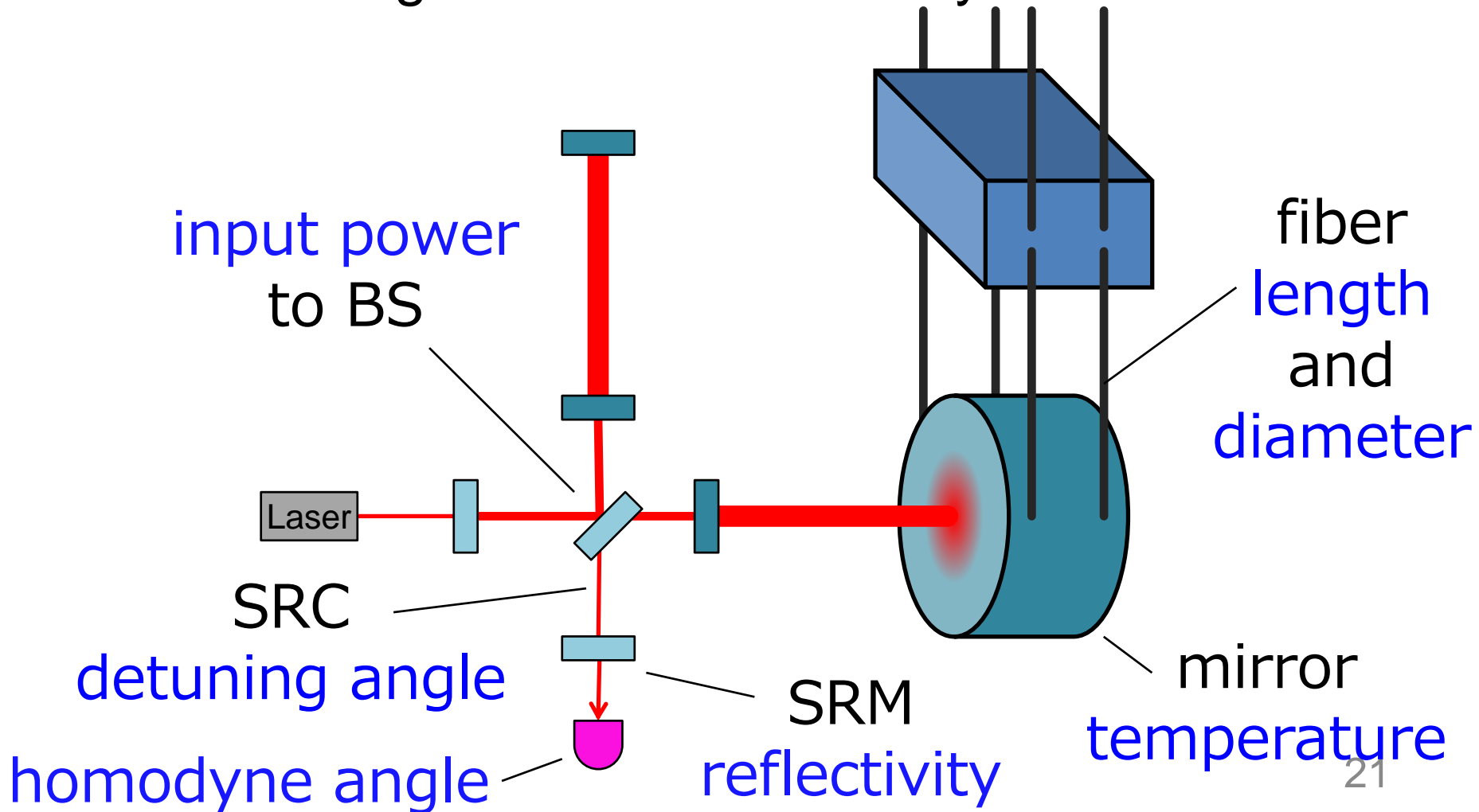
# Summary

- Study of **KAGRA upgrade** aiming for realization in ~2024 has started last year
- **Cryogenic** detectors have unique potential to improve the sensitivity
- Based on scientific target and technical feasibility, we have studied **realistic** near term upgrade plans
  - heavier mirror
  - higher power
  - frequency dependent squeezing
- **Further upgrade possible** by combining all the techniques, with more time and money
- Strategy **under discussion** in KAGRA collaboration
- Quite active **R&D** is on going

# Supplementary Slides

# Parameters of Interest

- 7 parameters are relatively **easy to be retuned**
- Search range based on feasibility



# Particle Swarm Optimization

- Particles search the parameter space based on **own best** position and **entire swarm's best** known position

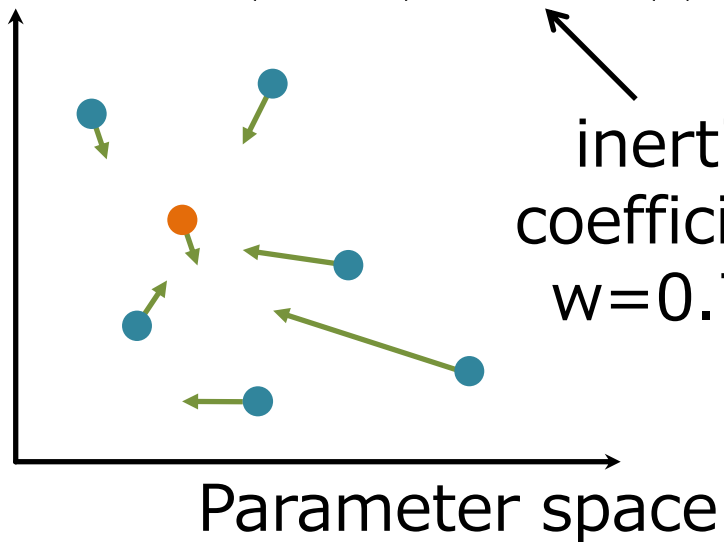
$$x_k(t+1) = x_k(t) + v_k(t)$$

personal best position so far      global best position so far

$$v_k(t+1) = wv_k(t) + c_1r_1(\hat{x}_k - x_k(t)) + c_2r_2(\hat{x}_g - x_k(t))$$

inertia coefficient  
 $w=0.72$





acceleration coefficient  $c=1.19$   
random number  $r \in [0,1]$



[Kennedy & Eberhart \(1995\)](#)

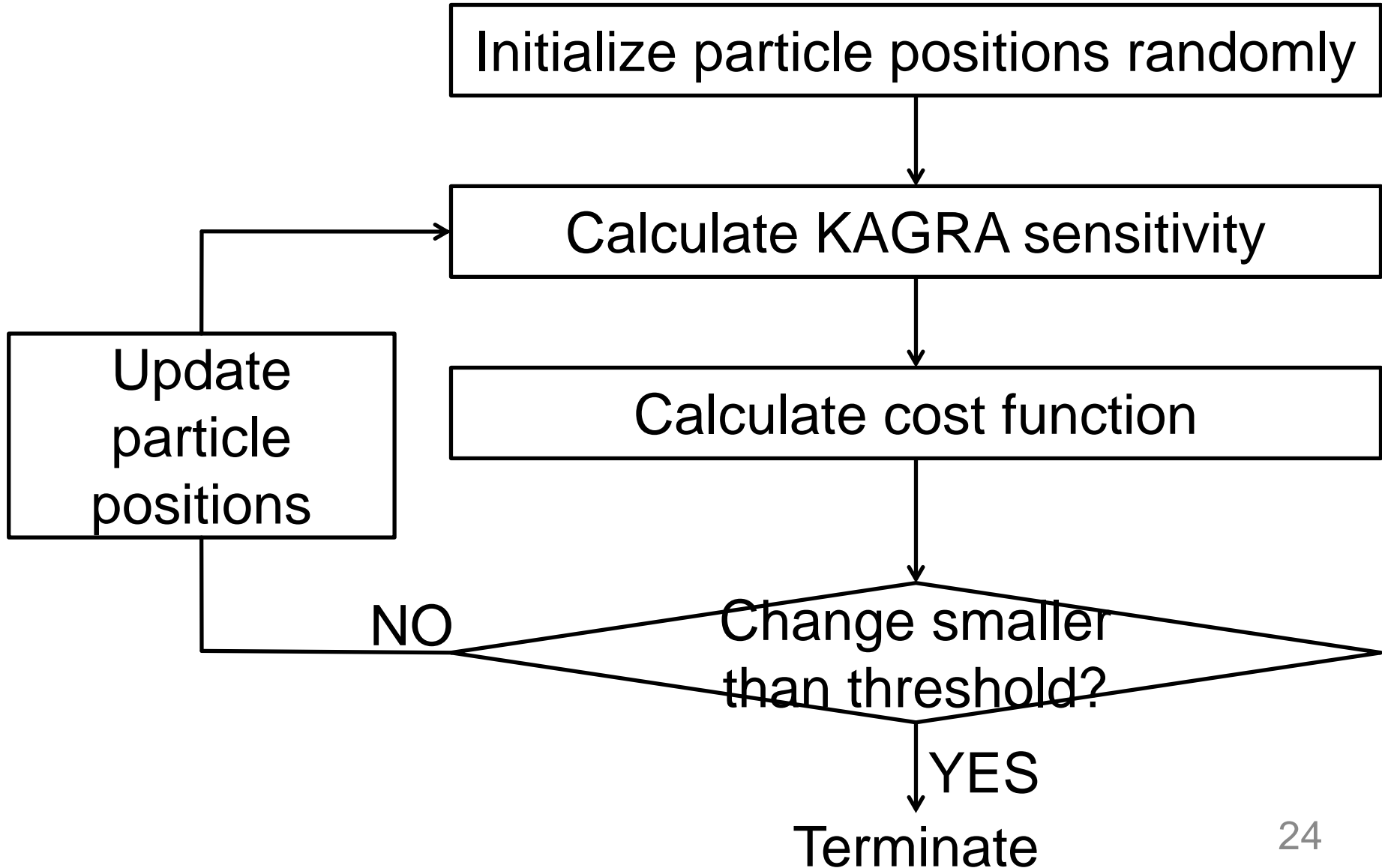
values for  $w$  and  $c$  are from [Standard PSO 2006](#)

# Pros and Cons of PSO

- **Fast** even for highly **multidimensional** parameter space   
uses entire swarm's information to search
- Requires **small number of design variables** and **little prior information**   
basically only swarm size and termination criterion  
prior information is only search range
- **No guarantee** for convergence to global maximum   
stochastic method
- Do not give **error** of the parameters   
no direct information on stability of the solution

→ Sounds great for detector design

# PSO Algorithm





# Swarm Size Determination

- **Probability of convergence**: ratio of PSO trials resulted within 0.1 Mpc or  $10^{-3}$  deg<sup>2</sup>
- Increased swarm size until probability of convergence is larger than **90%**

number of params	3	5	7
number of particles	10	20	200
number of iterations	$52 \pm 13$	$73 \pm 16$	$60 \pm 18$
probability of convergence	98 %	96 %	91 %

\* From 100 PSO trials

# IFO Parameter Search Range

	Lower bound	Upper bound	KAGRA Default	Precision
Detuning angle [deg]	86.5 (or 60) *	90	86.5	0.1
Homodyne angle [deg]	90	180	135.1	3
Mirror temperature [K]	20	30	22	0.09
Power attenuation	0.01	1	1	0.02
SRM reflectivity	0.5	1	0.92 (85%)	6e-4
Wire length [cm]	20	100	35	0.02
Wire safety factor	3	30	12.57 (0.8 mm)	0.07

\* Considering SRC nonlinearity, maximum detuning is 3.5 deg  
(see Y. Aso+ [CQG 29, 124008](#))

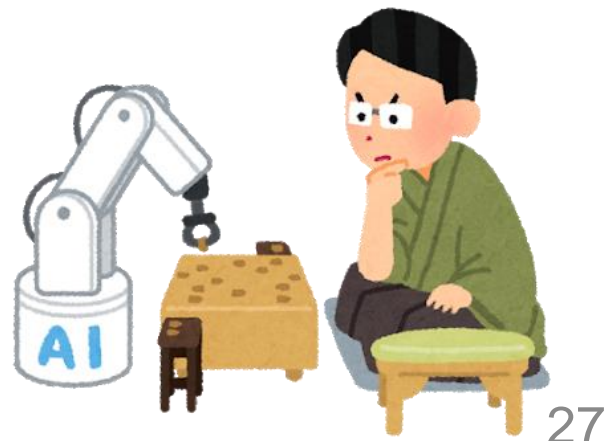
- *Reflecting wall* boundary:  
 $x=x_{\max}, v=-v$  if  $x>x_{\max}$   
 $x=x_{\min}, v=-v$  if  $x<x_{\min}$

step size which changes  
BNS inspiral range by 0.1 Mpc



# Other Optimization Methods

- Simulated annealing  
tuning cooling schedule is troublesome
- Genetic algorithm  
too many design variables
- Markov chain Monte Carlo  
tend to be dependent on prior distribution  
gives error from posterior distribution  
takes time
- Machine learning  
if the problem well-modeled,  
you don't need ML



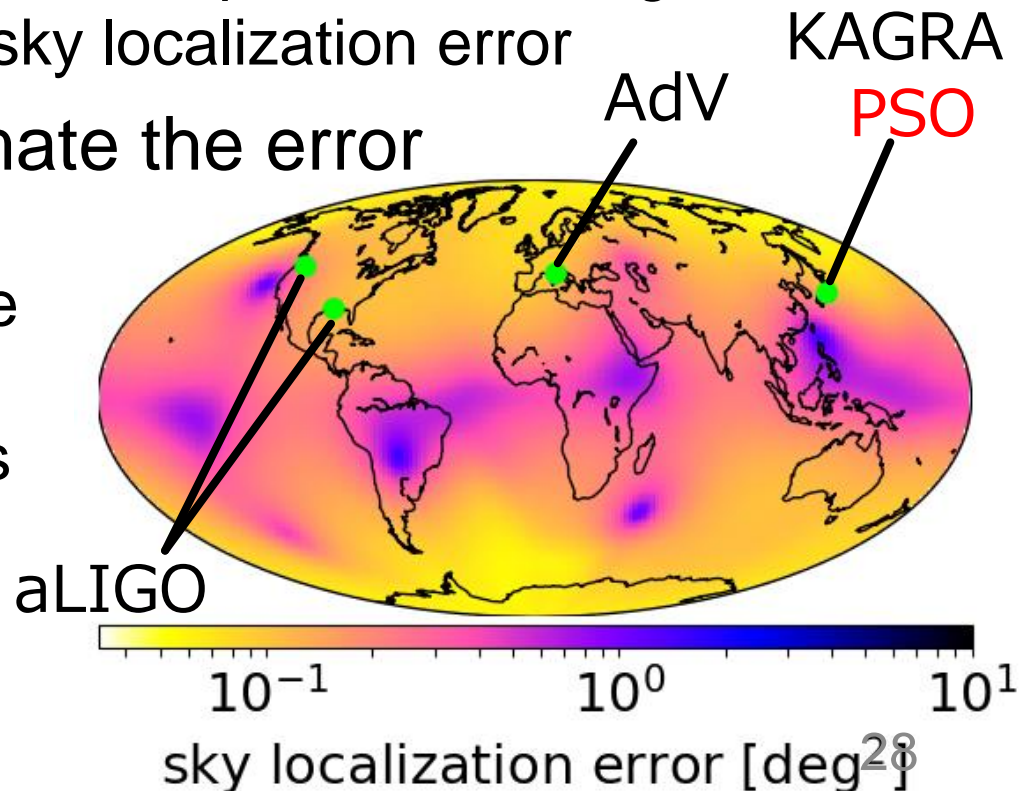
# Sky Localization Optimization

- Cost function:
  - **sky localization** of **GW170817**-like binary
    - 1.25-1.5 Msun at 40 Mpc, inclination 28 deg
    - zero spins, no precession
    - **108 sets** of sky location and polarization angle to derive median of sky localization error

- **Fisher matrix** to estimate the error

- inspiral waveform to
  - 3.0 PN in amplitude
  - 3.5 PN in phase
- 11 binary parameters

- **HLVK** global network



# Fisher Matrix Analysis

- Fisher matrix

$$\Gamma_{ij} = 4\Re \int_{f_{\min}}^{f_{\max}} \sum_k \frac{\partial h_k^*(f)}{\partial \lambda^i} \frac{\partial h_k(f)}{\partial \lambda^j} \frac{df}{S_{n,k}(f)}$$

- Covariance

$$\sqrt{\langle (\delta \lambda^i \delta \lambda^j) \rangle} = \sqrt{(\Gamma^{-1})^{ij}}$$

- 11 binary parameters considered

**mc**: chirp mass

**eta**: symmetric mass ratio

**tc**, **phic**: time and phase for coalescence

**dL**: luminosity distance

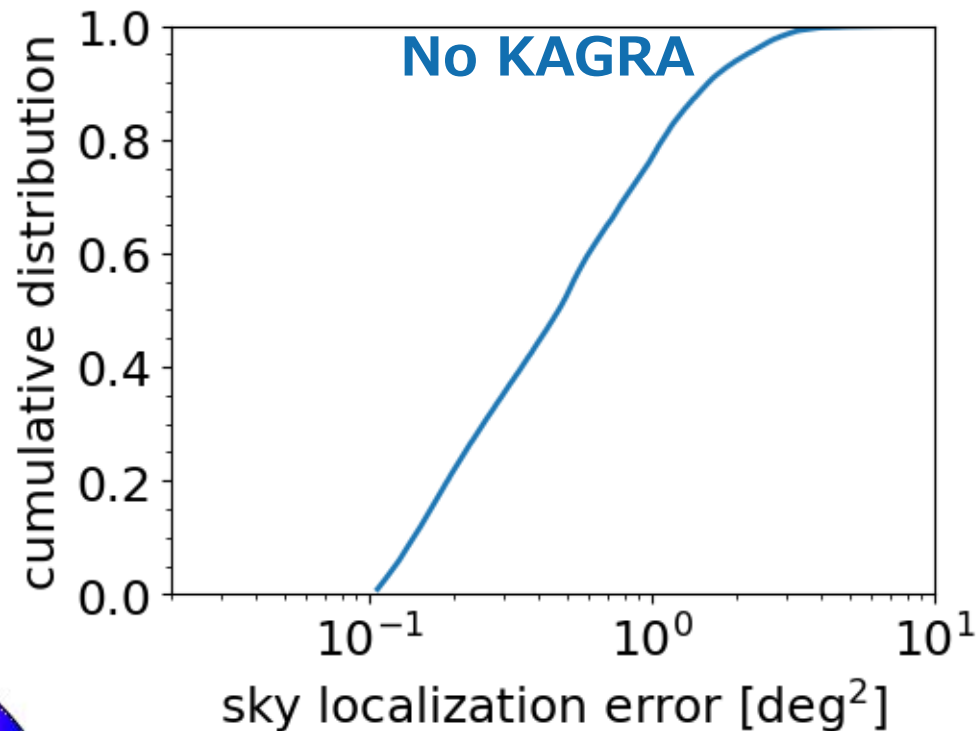
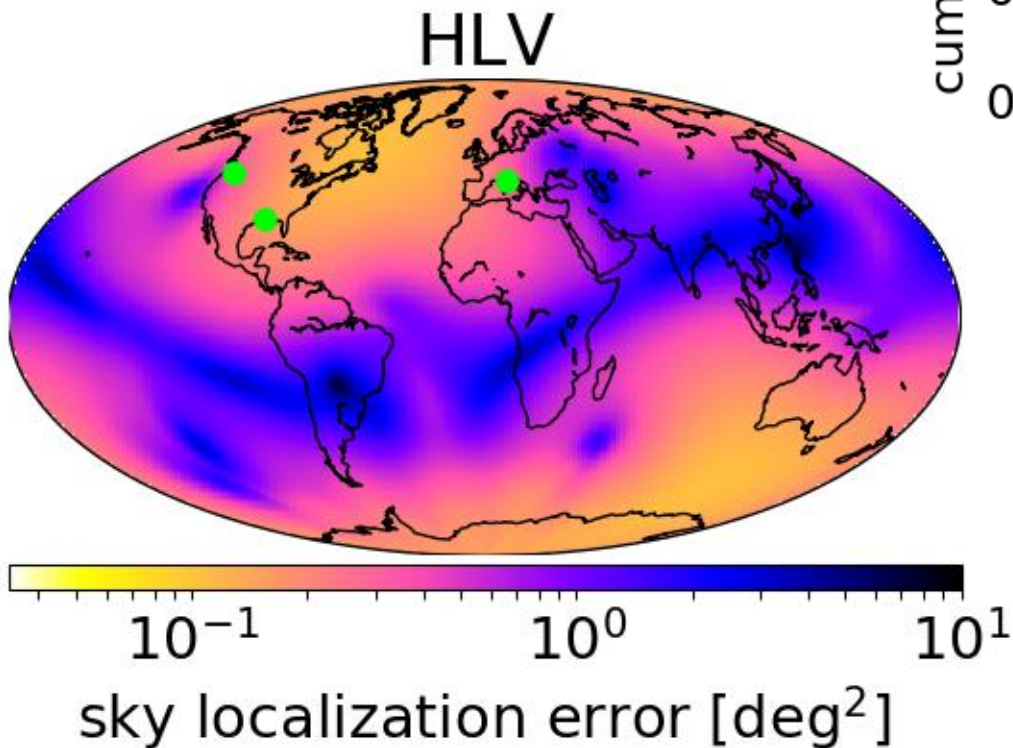
**chis**, **chia**: symmetric/asymmetric spin  $\chi_{s/a} = (\chi_1 \pm \chi_2)/2$

**thetas**, **phis**: colatitude / longitude of source

**cthetai**: inclination angle

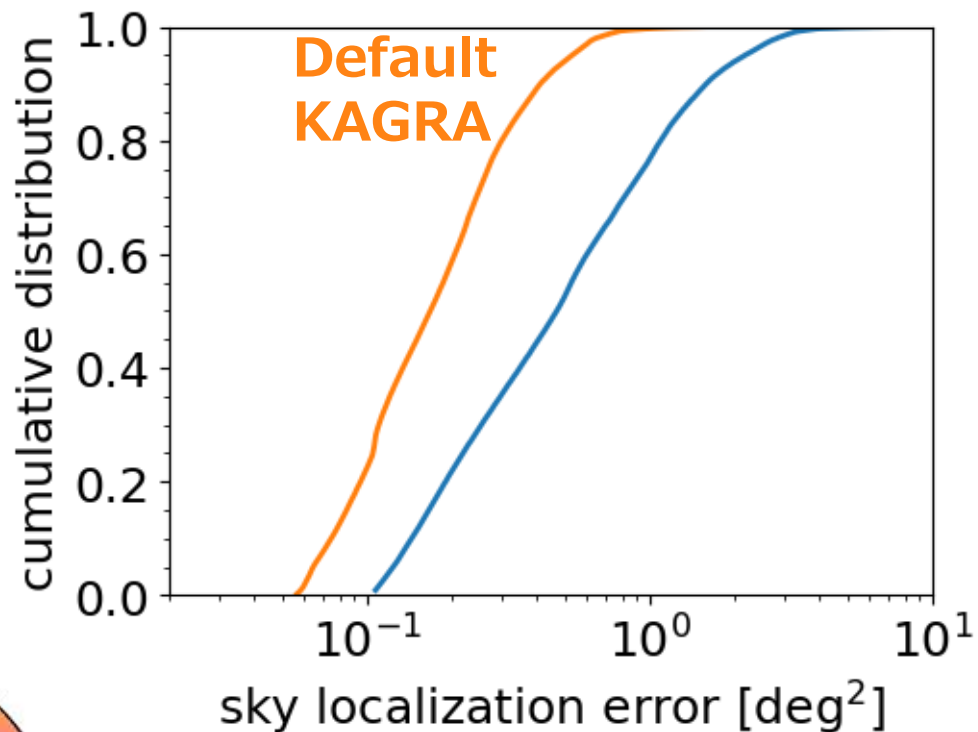
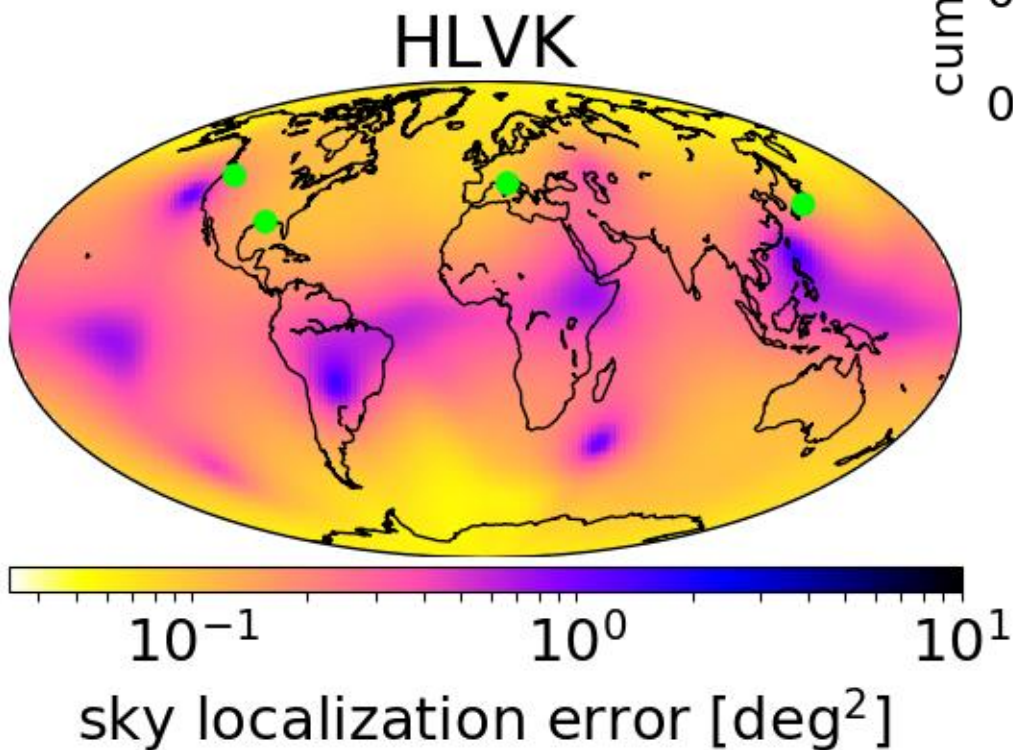
**psip**: polarization angle

# Sky Localization with HLV



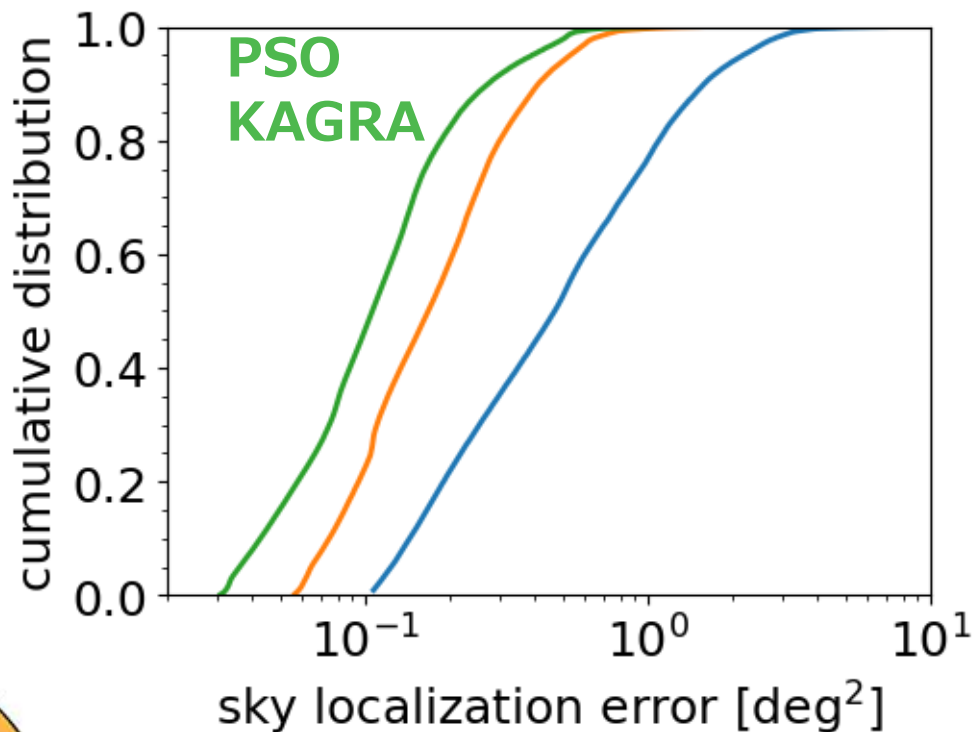
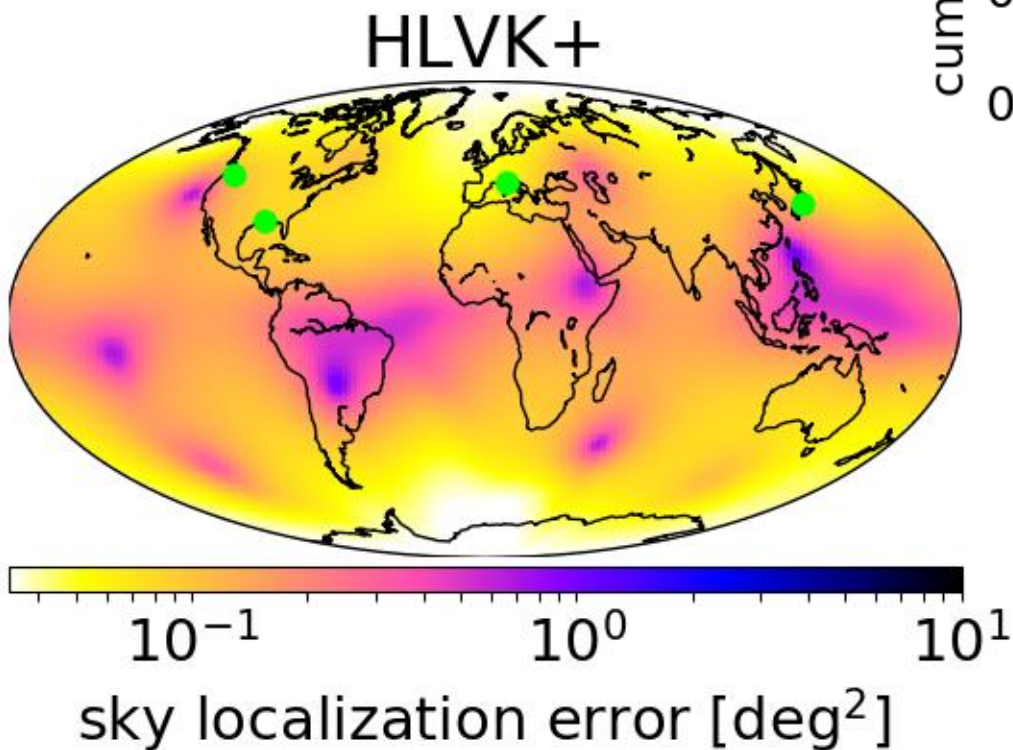
	median
HLV	0.472 deg <sup>2</sup>
HLVK	
HLVK+	

# Sky Localization with HLVK



	median
HLV	0.472 deg <sup>2</sup>
HLVK	0.168 deg <sup>2</sup>
HLVK+	

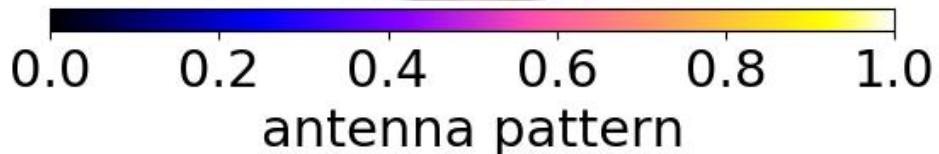
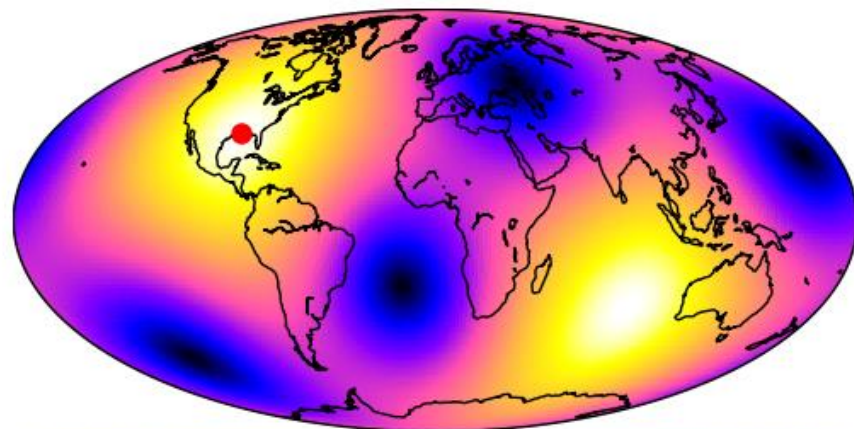
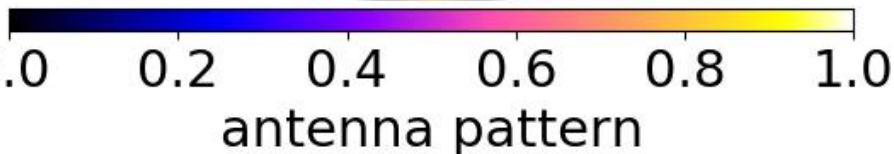
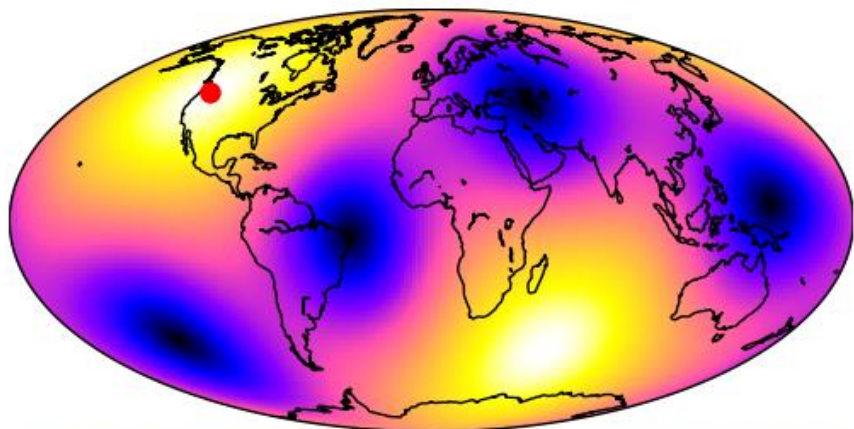
# Sky Localization with HLVK+



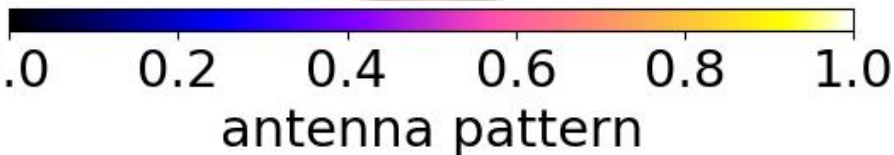
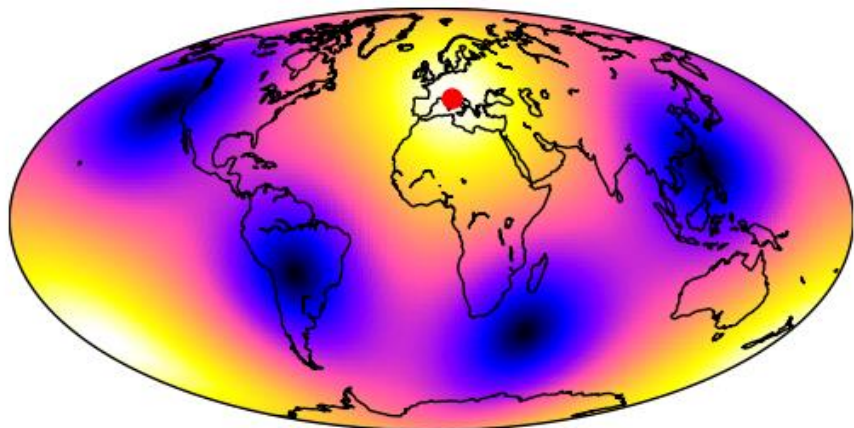
	median
HLV	0.472 $\text{deg}^2$
HLVK	0.168 $\text{deg}^2$
HLVK+	0.107 $\text{deg}^2$



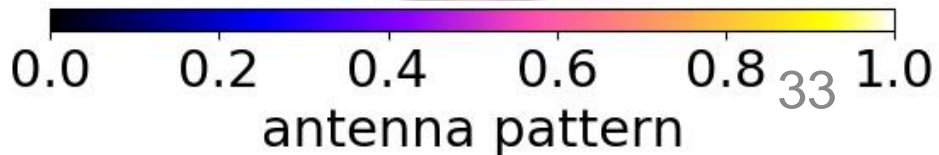
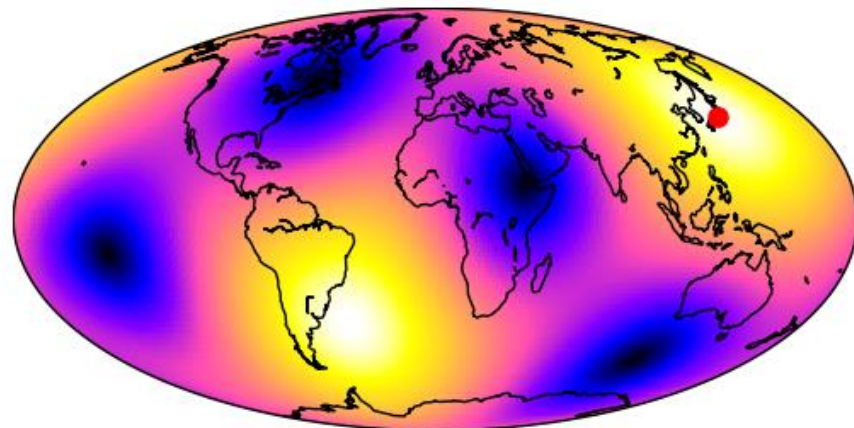
# H Antenna Pattern L



V



K



# 2G/2G+ Parameter Comparison

	<b>KAGRA</b>	<b>AdVirgo</b>	<b>aLIGO</b>	<b>A+</b>	<b>Voyager</b>
Arm length [km]	3	3	4	4	4
Mirror mass [kg]	23	42	40	80	200
Mirror material	Sapphire	Silica	Silica	Silica	Silicon
Mirror temp [K]	22	295	295	295	123
Sus fiber	35cm Sap.	70cm SiO <sub>2</sub>	60cm SiO <sub>2</sub>	60cm SiO <sub>2</sub>	60cm Si
Fiber type	Fiber	Fiber	Fiber	Fiber	Ribbon
Input power [W]	67	125	125	125	140
Arm power [kW]	340	700	710	1150	3000
Wavelength [nm]	1064	1064	1064	1064	2000
Beam size [cm]	3.5 / 3.5	4.9 / 5.8	5.5 / 6.2	5.5 / 6.2	5.8 / 6.2
SQZ factor	0	0	0	6	8
F. C. length [m]	none	none	none	16	300

# KAGRA Detailed Parameters

K. Komori *et al.*, [JGW-T1707038](#)

- **Optical parameters**
  - Mirror transmission: 0.4 % for ITM, 10 % for PRM, 15.36 % for SRM
  - Power at BS: 674 W
  - Detune phase: 3.5 deg (DRSE case)
  - Homodyne phase: 135.1 deg (DRSE case)
- **Sapphire mirror parameters**
  - TM size: 220 mm dia., 150 mm thick
  - TM mass: 22.8 kg
  - TM temperature: 22 K
  - Beam radius at ITM: 3.5 cm
  - Beam radius at ETM: 3.5 cm
  - Q of mirror substrate:  $1e8$
  - Coating: tantala/silica
  - Coating loss angle:  $3e-4$  for silica,  $5e-4$  for tantala
  - Number of layers: 22 for ITM, 40 for ETM
  - Coating absorption: 0.5 ppm
  - Substrate absorption: 50 ppm/cm
- **Suspension parameters**
  - TM-IM fiber: 35 cm long, 1.6 mm dia.
  - IM temperature: 16 K
  - Heat extraction: 5800 W/m/K at 20 K
  - Loss angle:  $5e-6/2e-7/7e-7$  for CuBe fiber/sapphire fiber/sapphire blade
- **Inspirial range calculation**
  - SNR=8,  $f_{min}=10$  Hz, sky average constant 0.442478
- Seismic noise curve includes vertical coupling, vibration from heatlinks and Newtonian noise from surface and bulk

# KAGRA Cryopayload

Provided by T. Ushiba and T. Miyamoto

Platform  
(SUS, 65 kg)

Marionette  
(SUS, 22.5 kg)

Intermediate Mass  
(SUS, 20.1 kg,  
16 K)

Test Mass  
(Sapphire, 23 kg,  
22 K)

3 CuBe blade springs

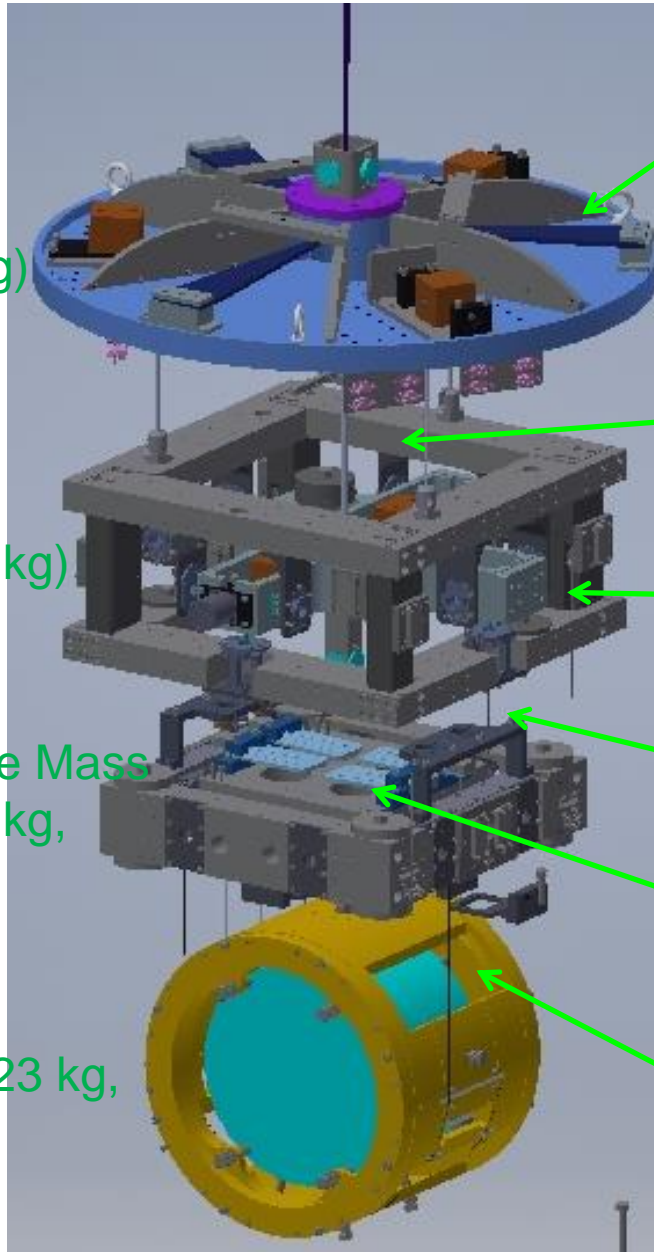
MN suspended by 1 Maraging steel fiber  
(35 cm long, 2-7mm dia.)  
MRM suspended by 3 CuBe fibers

Heat link attached to MN

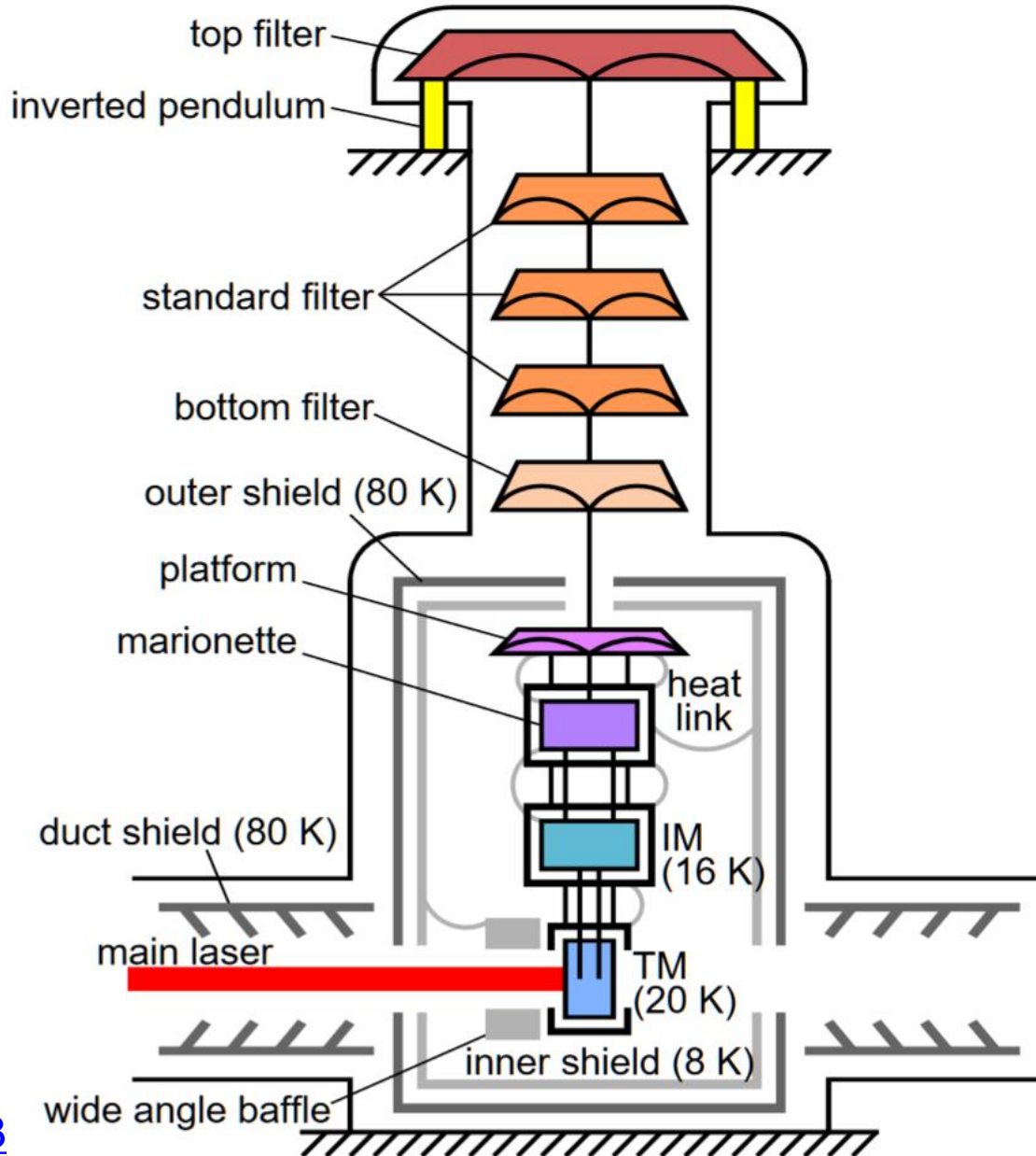
IM suspended by 4 CuBe fibers  
(24 cm long, 0.6 mm dia)  
IRM suspended by 4 CuBe fibers

4 sapphire blades

TM suspended by 4 sapphire fibers  
(35 cm long, 1.6 mm dia.)  
RM suspended by 4 CuBe fibers

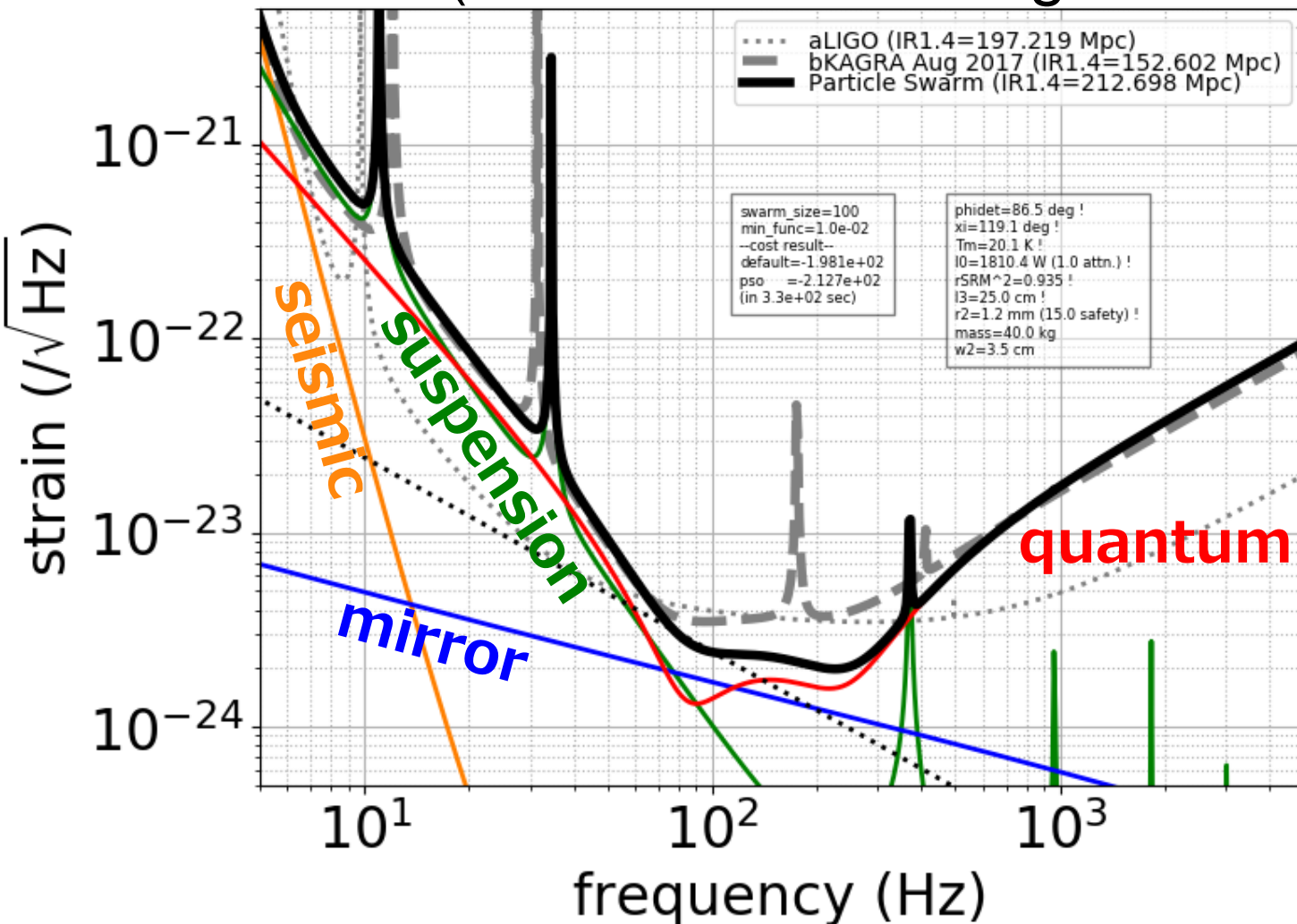


# KAGRA Cryostat Schematic



# Plan A: 40 kg Mirror

- Also assumes factor of 2 coating loss angle reduction (no beam size change assumed)

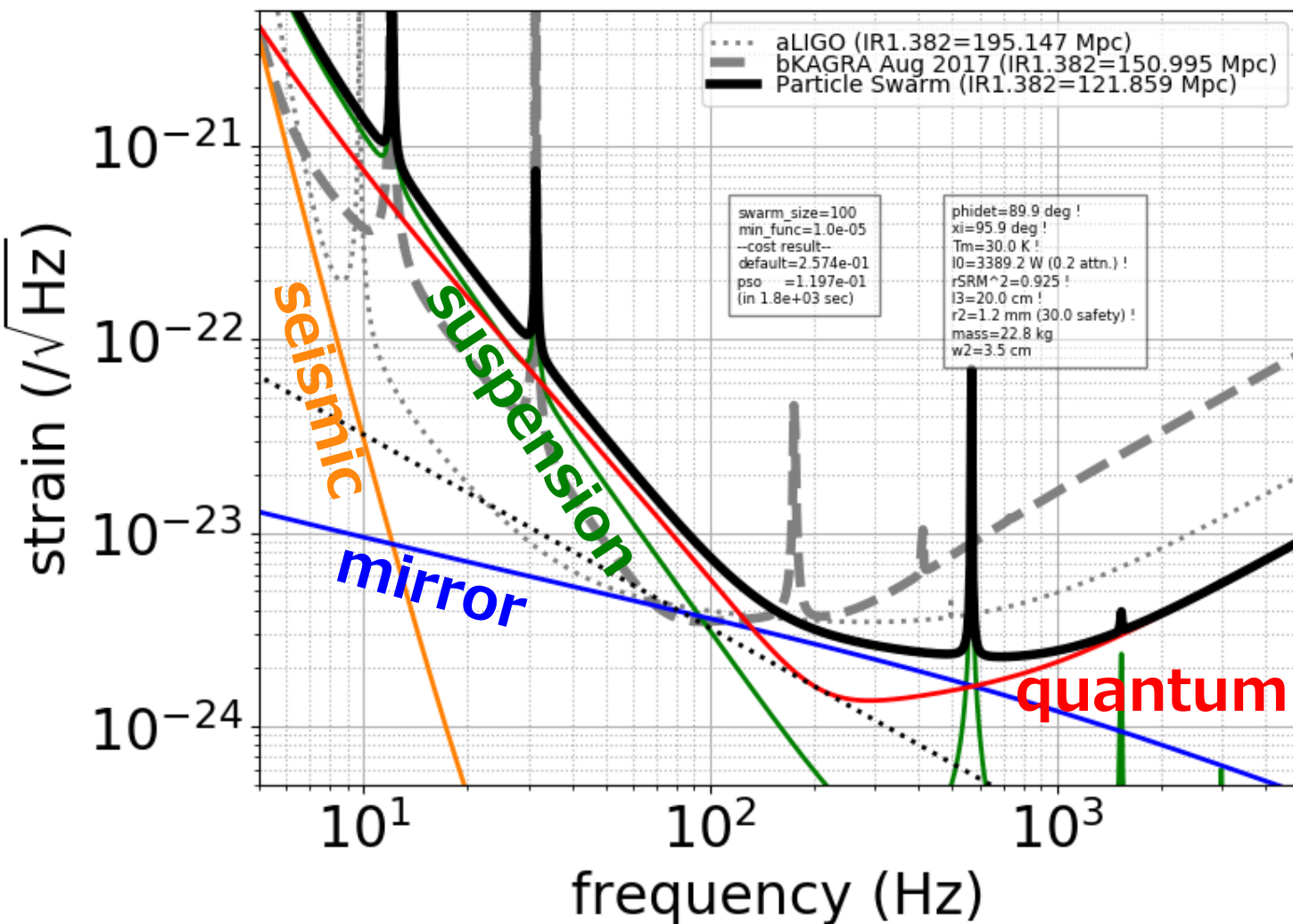


Good for mid frequency improvement  
 → BNS range optimized

T=20.1 K  
 181 W input  
 thicker fiber  
 25.0 cm  
 φ1.2 mm  
 (thicker to allow for higher power)

# Plan B: 400 W Laser with SQZ

- Assumes 10dB input SQZ

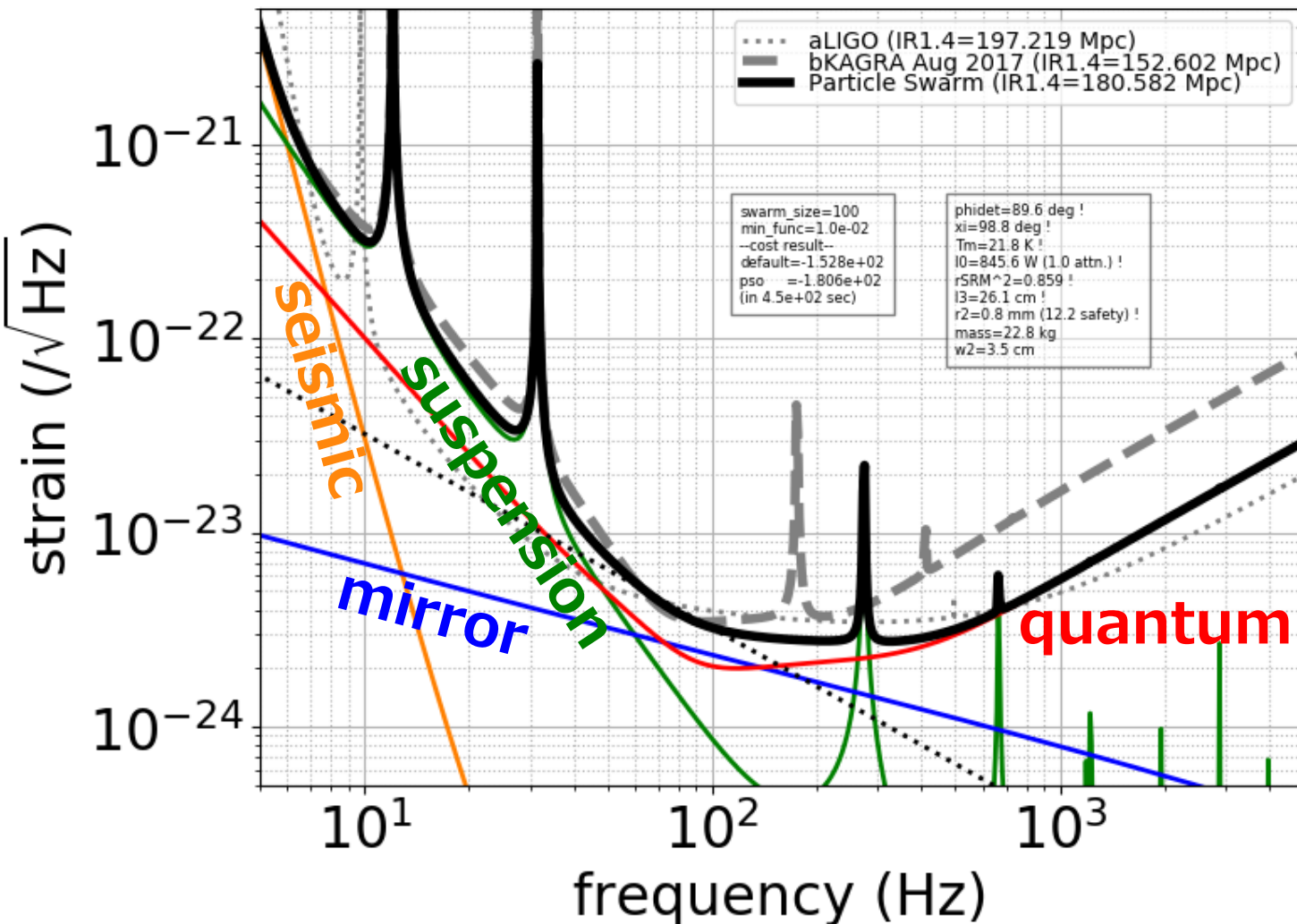


Good for high frequency improvement  
 → BNS range optimized

**T=29.8 K**  
 330 W input  
**shorter and thicker** fiber  
 20.1 cm  
 $\phi$ 1.2 mm  
 (high power with high temperature)

# Plan C: Freq. Dependent SQZ

- Assumes 10dB input SQZ and 100 m filter cavity



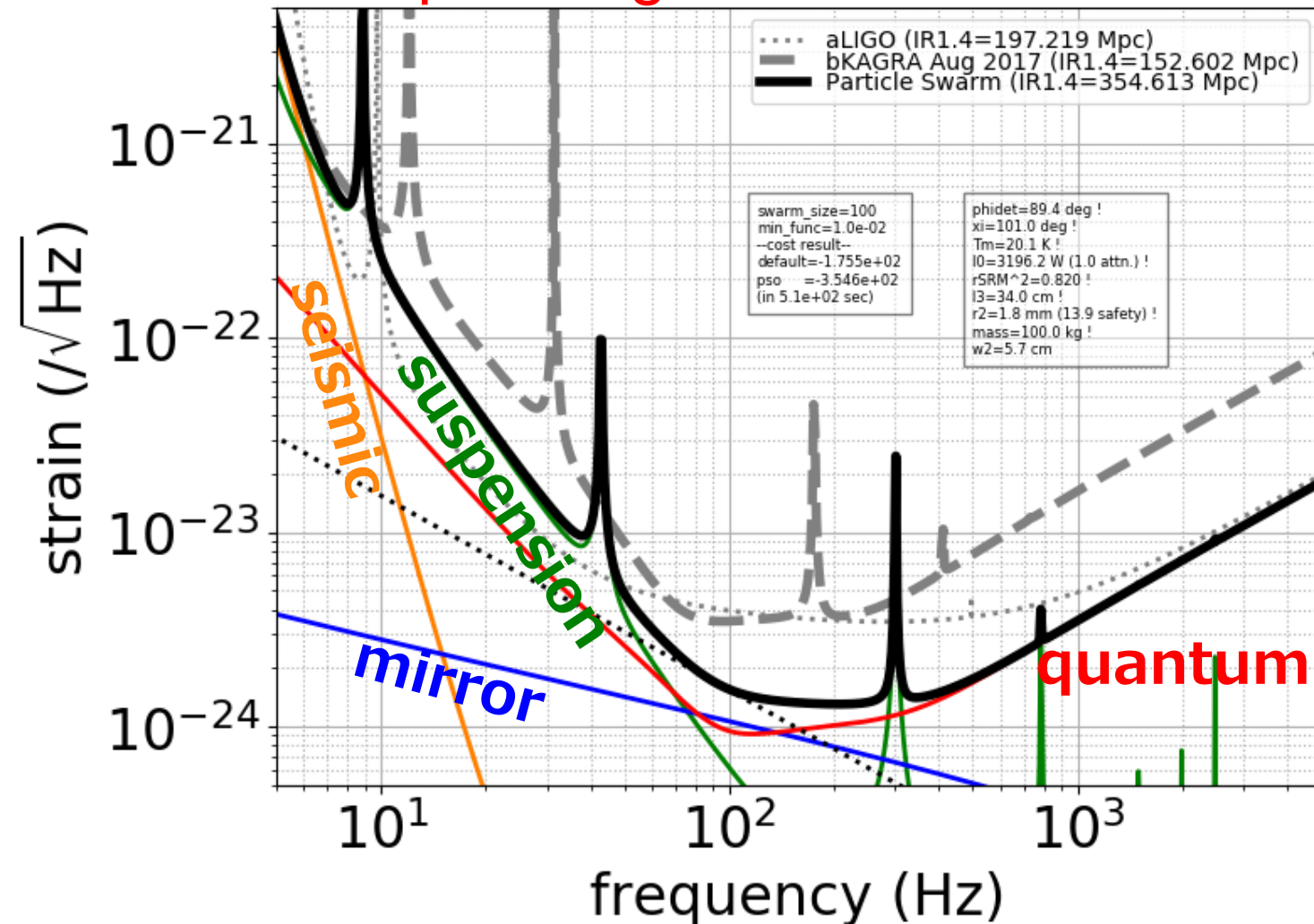
Broadband improvement  
→ BNS range optimized

T=21.8 K  
85 W input  
thinner fiber  
26.1 cm  
φ0.8 mm  
(SQZ helps to ease fiber requirement)



# Longer Term Candidate

- 100 kg mirror with 1/2 coating thermal, 320 W input, 10 dB squeezing with 100 m filter cavity



Broadband improvement  
→ BNS range optimized

T=20.1 K  
320 W input  
longer fiber  
34.9 cm  
φ1.8 mm

# Very Rough Estimates

- New mirrors: **\$3M**
- Sapphire fiber replacement: **\$1M**
- Cryopayload replacement: **\$4M**
- Type-A tower replacement: **\$2M**
- Frequency independent squeezing: **\$1M**
- Frequency dependent squeezing: **\$3M**
- 400 W laser and high power input optics: **\$3M**
- Recycling mirror replacement (for larger beam): **\$1M**
- SRM replacement: **\$0.1M**