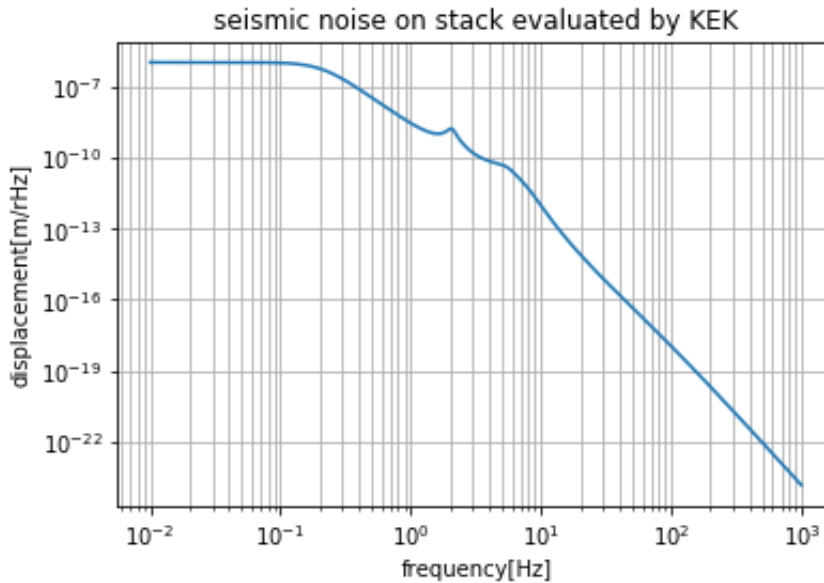


```
In [1]: import numpy as np
import matplotlib.pyplot as plt
freq1, mprHz1 = np.loadtxt("./stackKEK.dat", unpack=True)
plt.xscale("log")
plt.yscale("log")
plt.grid(which="both")
plt.xlabel(r"frequency[Hz]") # x-axis
plt.ylabel(r"displacement[m/rHz]") # y-axis
plt.title(r"seismic noise on stack evaluated by KEK")#title
plt.plot(freq1, mprHz1)
plt.show()
```



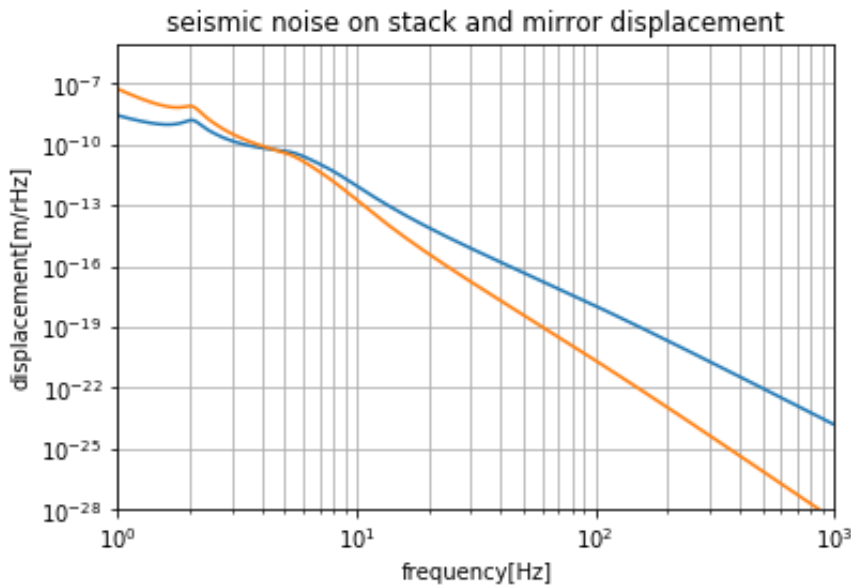
In [ ]: [Rough evaluation of the mirror angular motion due to extra static mag  
While the mirror **is** suspended by Type-C double pendulum, OSEM **is** fixed  
Then the relative displacement between the OSEM **and** the magnets on the  
**as** the seismic motion on stack measured by KEK, **if** the mirror **is** isolat  
**in** particular **in** high frequency range.

Because the OSEM has a kind of extra magnetic feature,  
the mirror **is** accelerated due to this relative motion,  
about  $k_1=0.2\text{N/mm}$  per 1 magnet; $L_5\phi^2$ .  
There are 4 magnets on the mirror, so the coupling coefficient **is**,  
 $k_4=0.8\text{[N/mm]}=800\text{[N/m]}$ .

The mirror displacement by this force **is** about  
 $ma=k_4\text{[N/m]}*x\_stack\text{[m/rHz]}$ .

Mirror mass **is** about  $m=1\text{kg}$ , then  $a=800\text{[}/\text{s}^2*\text{m/rHz]}$ .  
To make this into displacement  $x$ , divide the value by  $(2\pi*f)^2$ ,  
 $x\_ex=x\_stack*800/(2\pi*f)^2\text{[m/rHz]}$

```
In [2]: plt.xscale("log")
plt.yscale("log")
plt.grid(which="both")
plt.xlabel(r"frequency[Hz]") # x-axis
plt.ylabel(r"displacement[m/rHz]") # y-axis
plt.title(r"seismic noise on stack and mirror displacement")#title
plt.plot(freq1, mprHz1)
mprHz2=mprHz1*800/(2*np.pi*freq1)/(2*np.pi*freq1)
plt.plot(freq1, mprHz2)
plt.xlim([1,1000])
plt.ylim([1e-28, 1e-5])
plt.show()
```



Blue line shows the original stack motion.

Orange line shows excited motion by magnetic feature.

At low frequency region, the assumption of the equation is not valid.

```
In [ ]: If there is 10% imbalance of the mirror horizontal motion x_stack,
and convert it into angular motion by dividing it by the mirror diameter.
angular motion noise due to extra static magnetic feature, x_a
is evaluated as x_a=x_stack[m/rHz]*0.1(assumed coupling)/0.1[m]=x_stack
```

```
In [ ]: Other way to estimate the angular motion is to take moment of inertia
```

```
Iz=M/12*(3r^2+L^2)
=1[kg]/12*(3*5[cm^2]+6[cm^2])=9.25[kg.cm^2]

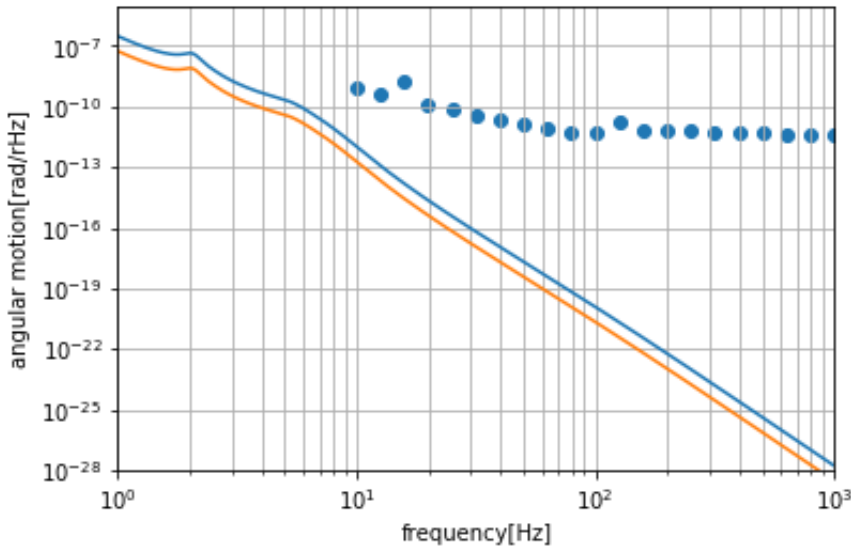
r*F=5[cm]*k1[N/mm]*4*x_stack*0.1(assumed imbalance)
=5*0.2*4*0.1*10*s_stack=4*x_stack[N.m/rHz]

radprHz=r*F/Iz/(2pi*f)^2
=4*x_stack/9.25/(2pi*f)^2
=4444*x_stack/(2pi*f)^2[rad/rHz]
```

```

In [3]: radprHz=mprHz1*4444/(2*np.pi*freq1)/(2*np.pi*freq1)
plt.xscale("log")
plt.yscale("log")
plt.grid(which="both")
plt.xlabel(r"frequency[Hz]") # x-axis
plt.ylabel(r"angular motion[rad/rHz]") # y-axis
plt.scatter(freq1, radprHz)
hor_req, ver_req, freq_req = np.loadtxt("./typeCreq.dat", unpack=True,
plt.plot(freq1, radprHz)
plt.plot(freq1, mprHz2)
plt.scatter(freq_req, ver_req)
plt.xlim([1, 1000])
plt.ylim([1e-28, 1e-5])
plt.show()

```



Blue dots show required upper limit of the mirror angular motion calculated by Somiya-san.  
Blue line shows the angular motion estimated by using moment of inertia.  
Orange line shows the angular motion estimated from 10% coupling from horizontal motion.  
Both estimations are well below the requirement over 10Hz.