

Re-considering bKAGRA EOM layout

May 2017

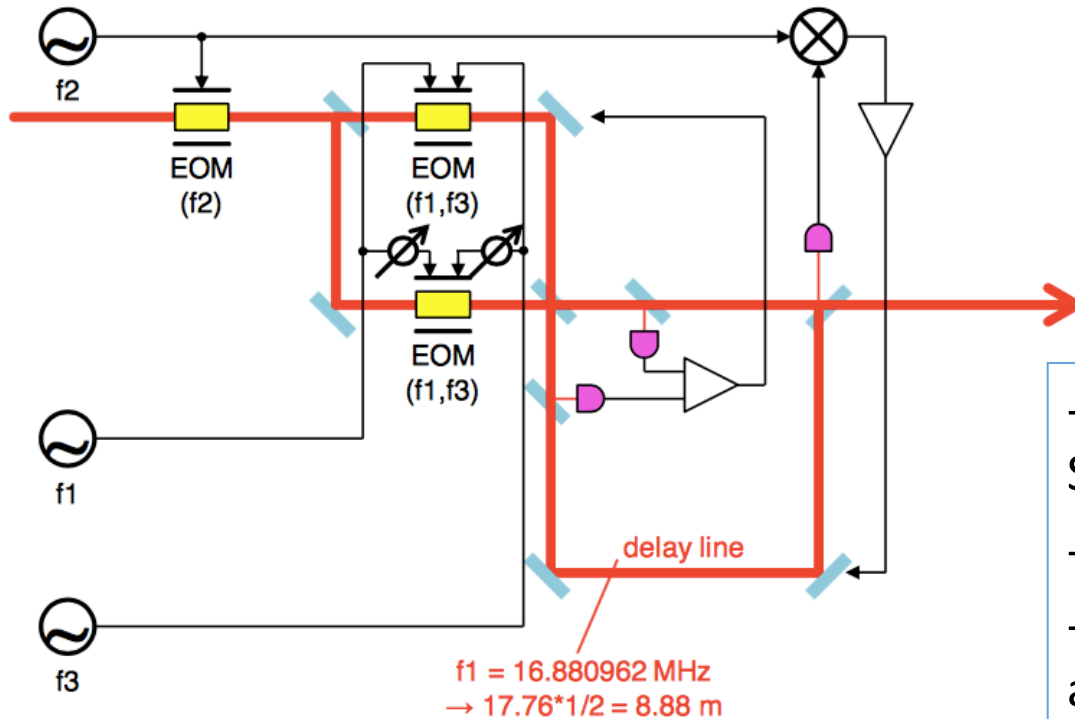
Yutaro Enomoto

default plan

JGW-D1503189-v3

Layout 3

- Simpler, but loses some f3 AM



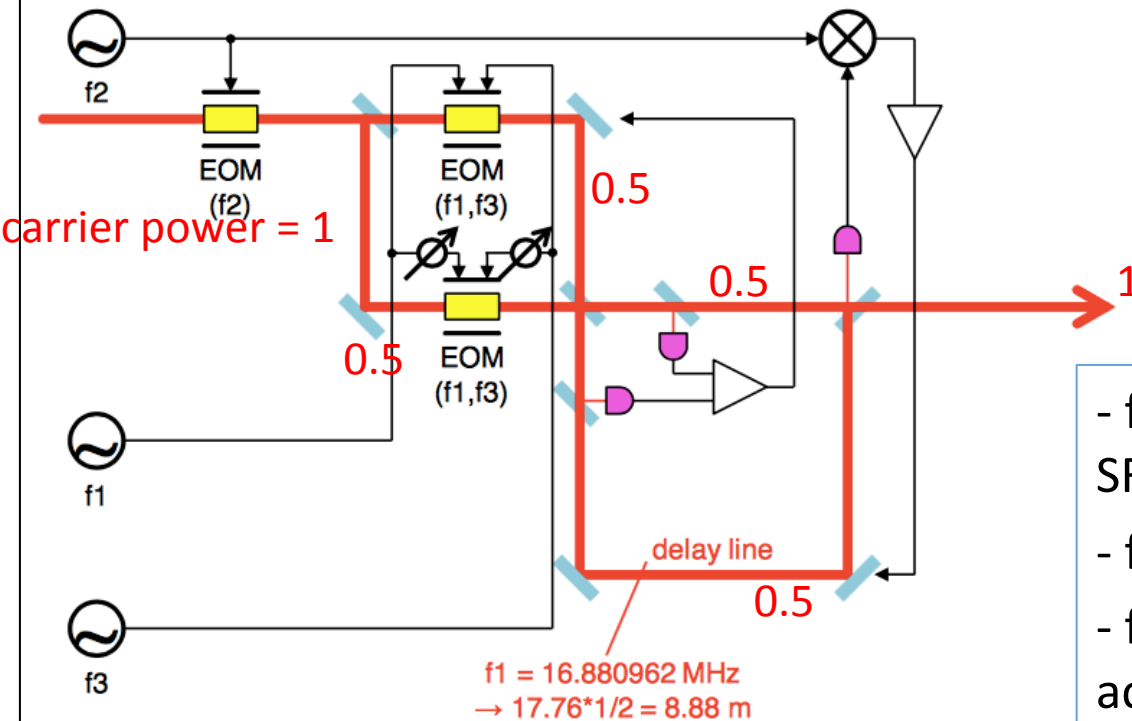
- f1: PM and AM (depending on SRC detuning)
- f2: PM only
- f3: AM only (used only for lock acquisition phase)

default plan

JGW-D1503189-v3

Layout 3

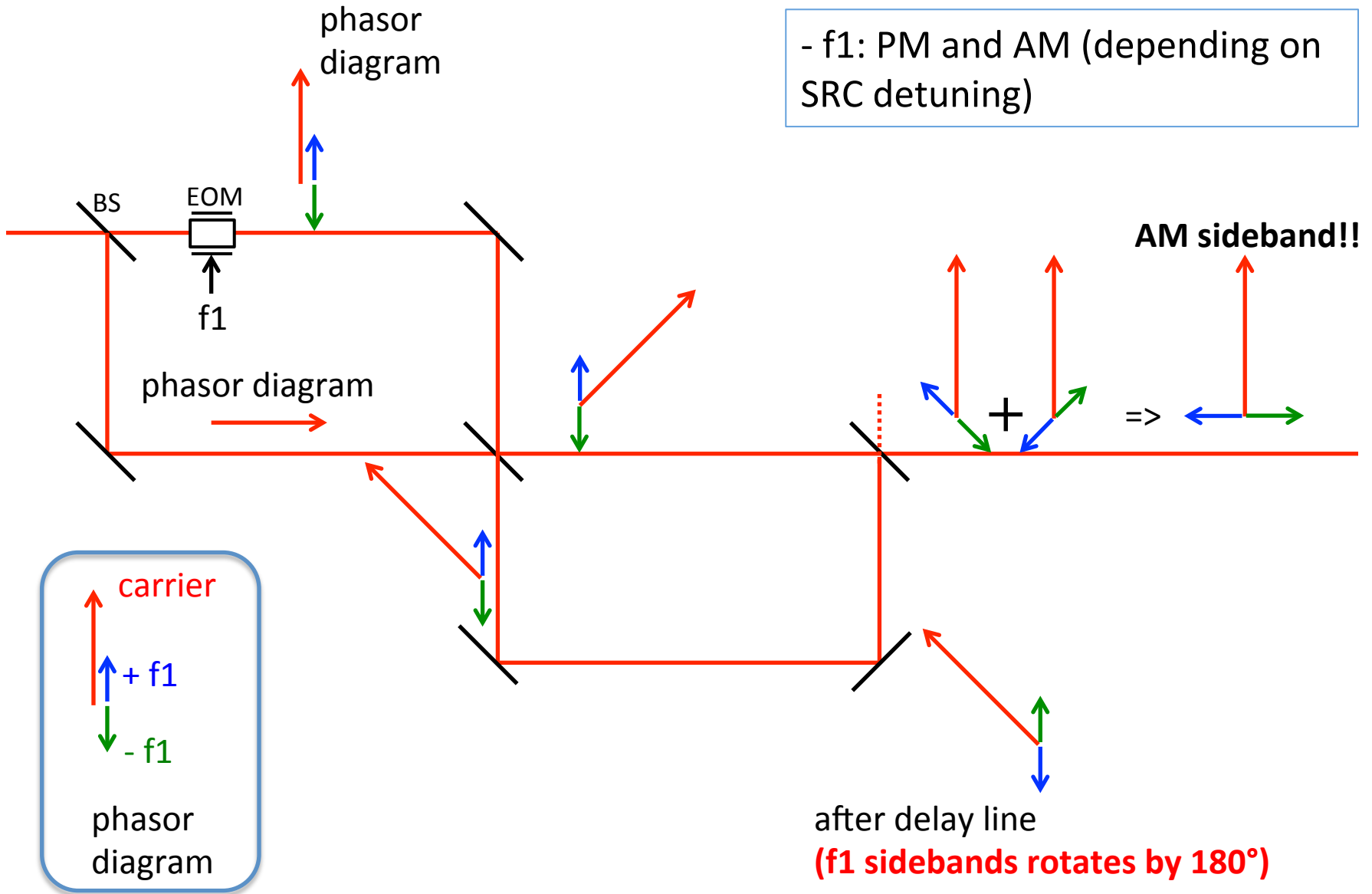
- Simpler, but loses some f3 AM



- f1: PM and AM (depending on SRC detuning)
- f2: PM only
- f3: AM only (used only for lock acquisition phase)

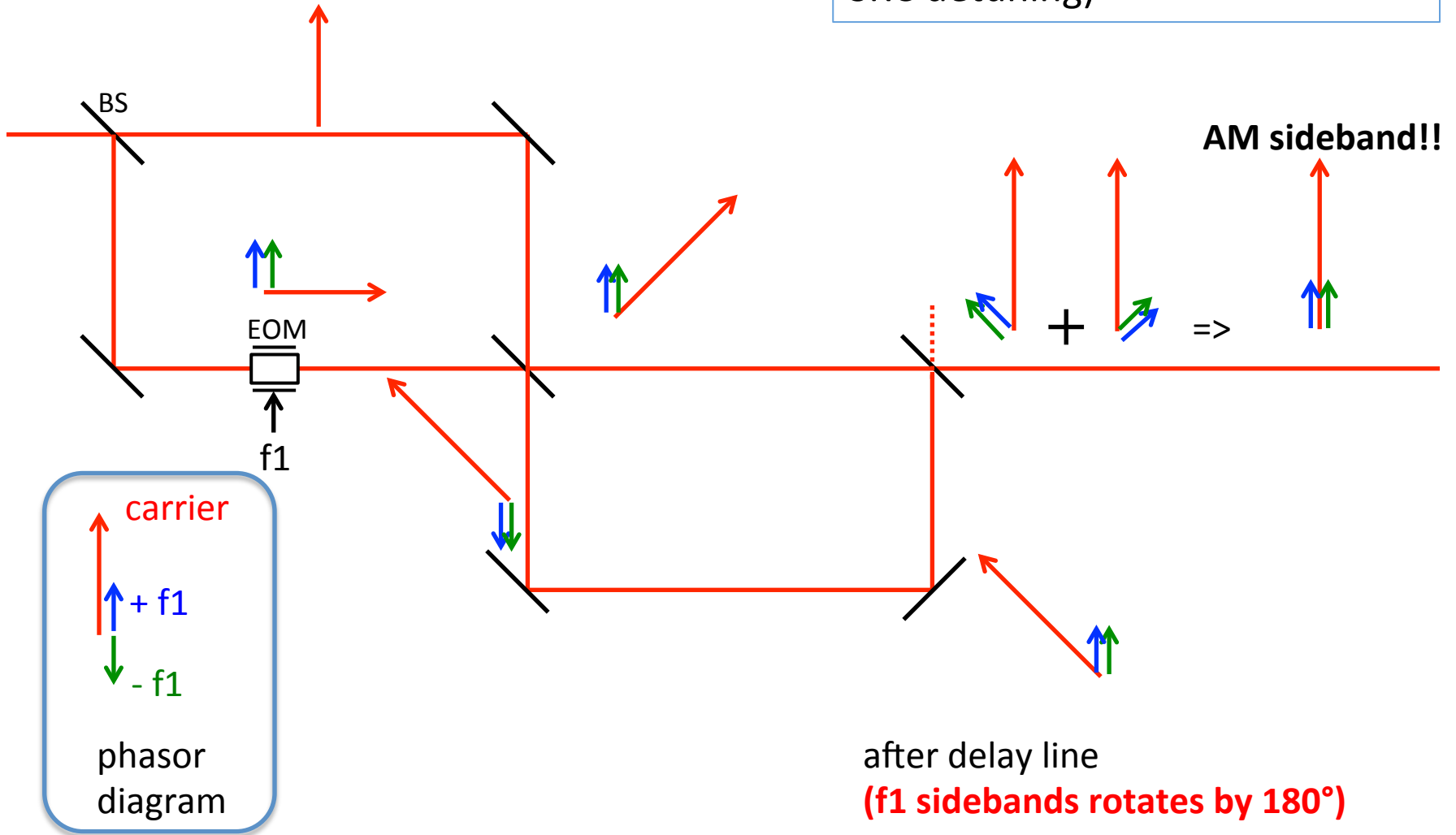
= Let us focus on f_1 =

- f_1 : PM and AM (depending on SRC detuning)



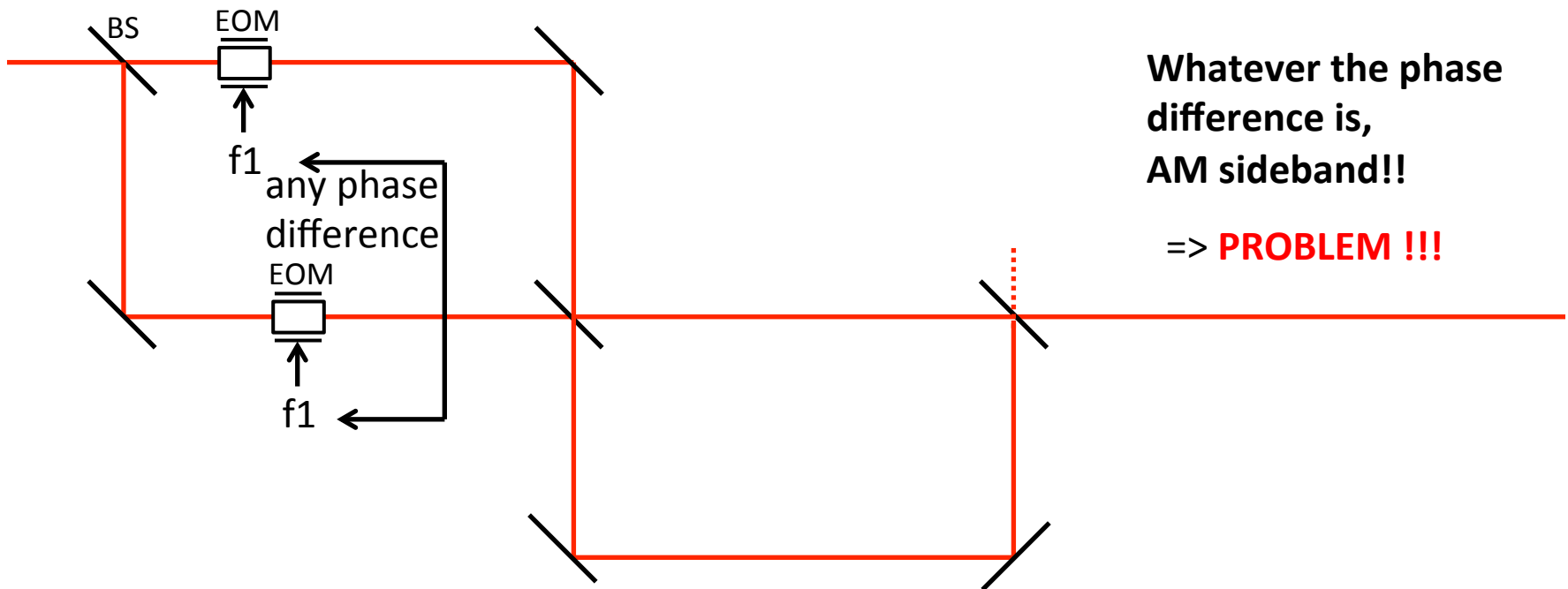
= Let us focus on f_1 =

- f_1 : PM and AM (depending on SRC detuning)



= Let us focus on f1 =

- f1: PM and AM (depending on SRC detuning)



Whatever the phase difference is,
AM sideband!!

=> **PROBLEM !!!**

after delay line

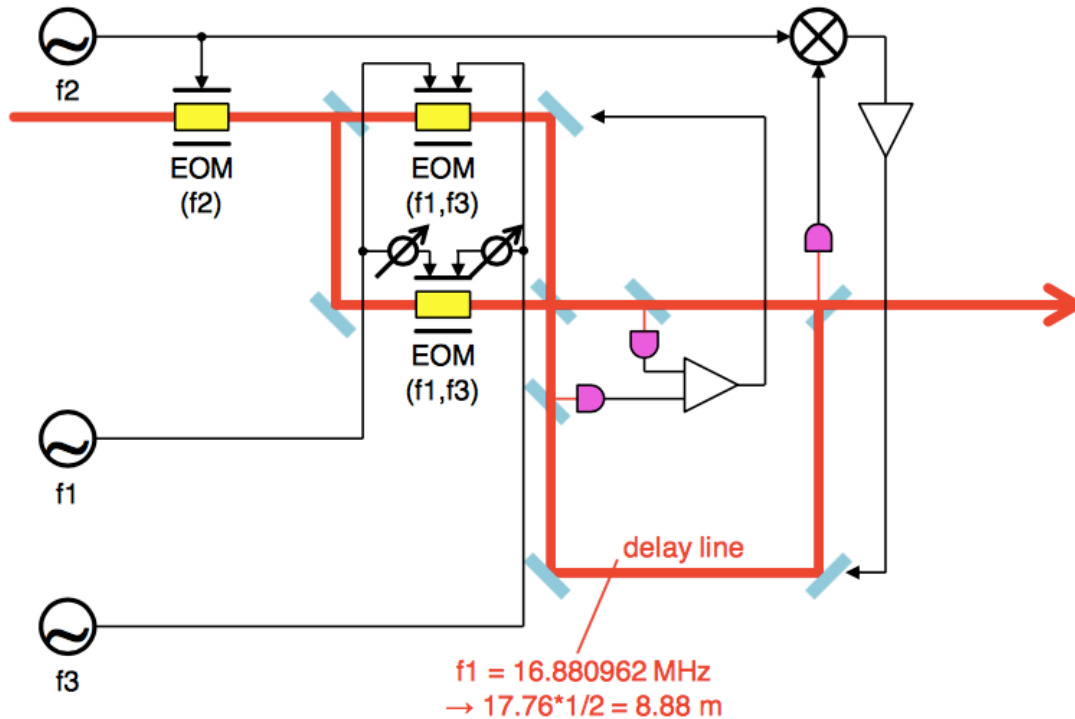
(f1 sidebands rotates by 180°)

alternative plan

JGW-D1503189-v3

Layout 3

- Simpler, but loses some f3 AM

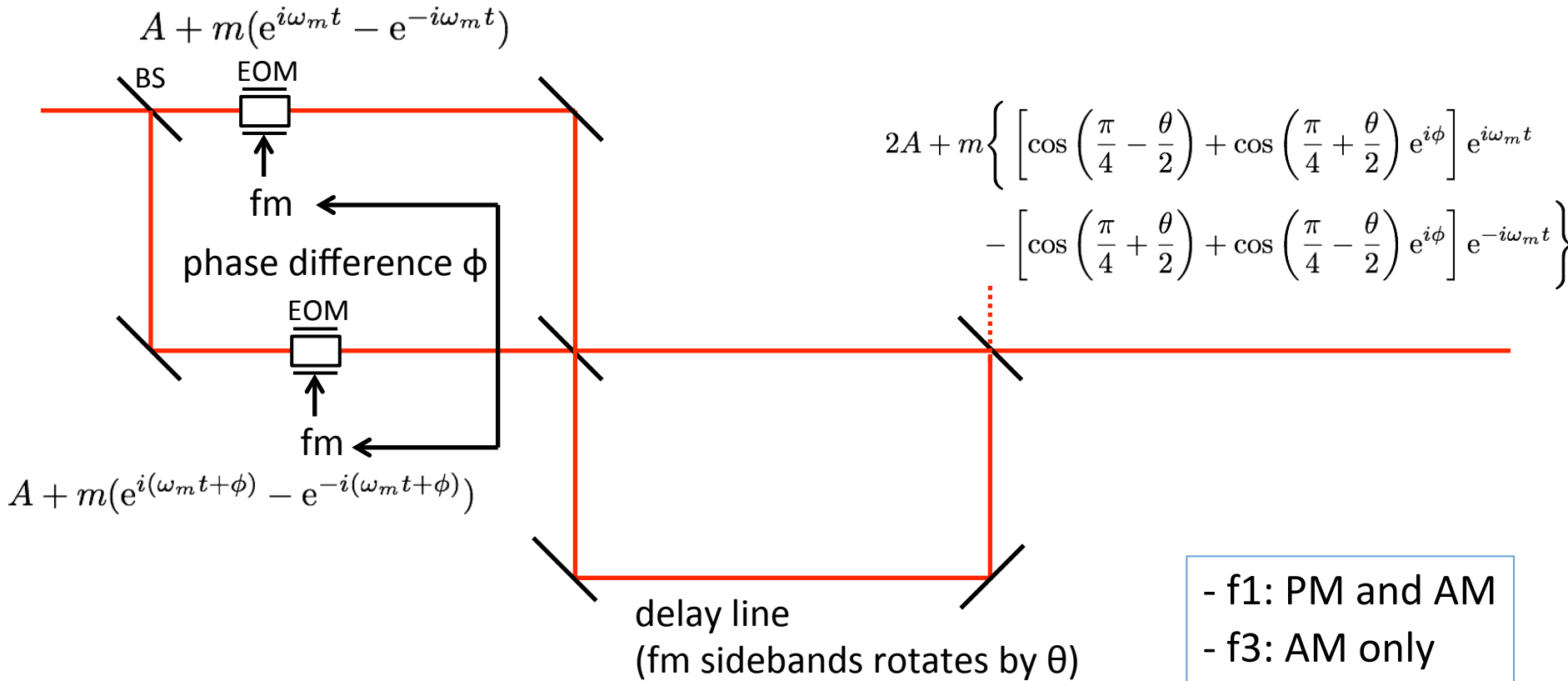


$f1 = 16.880962 \text{ MHz}$
 $\rightarrow 17.76 \cdot 1/2 = 8.88 \text{ m}$

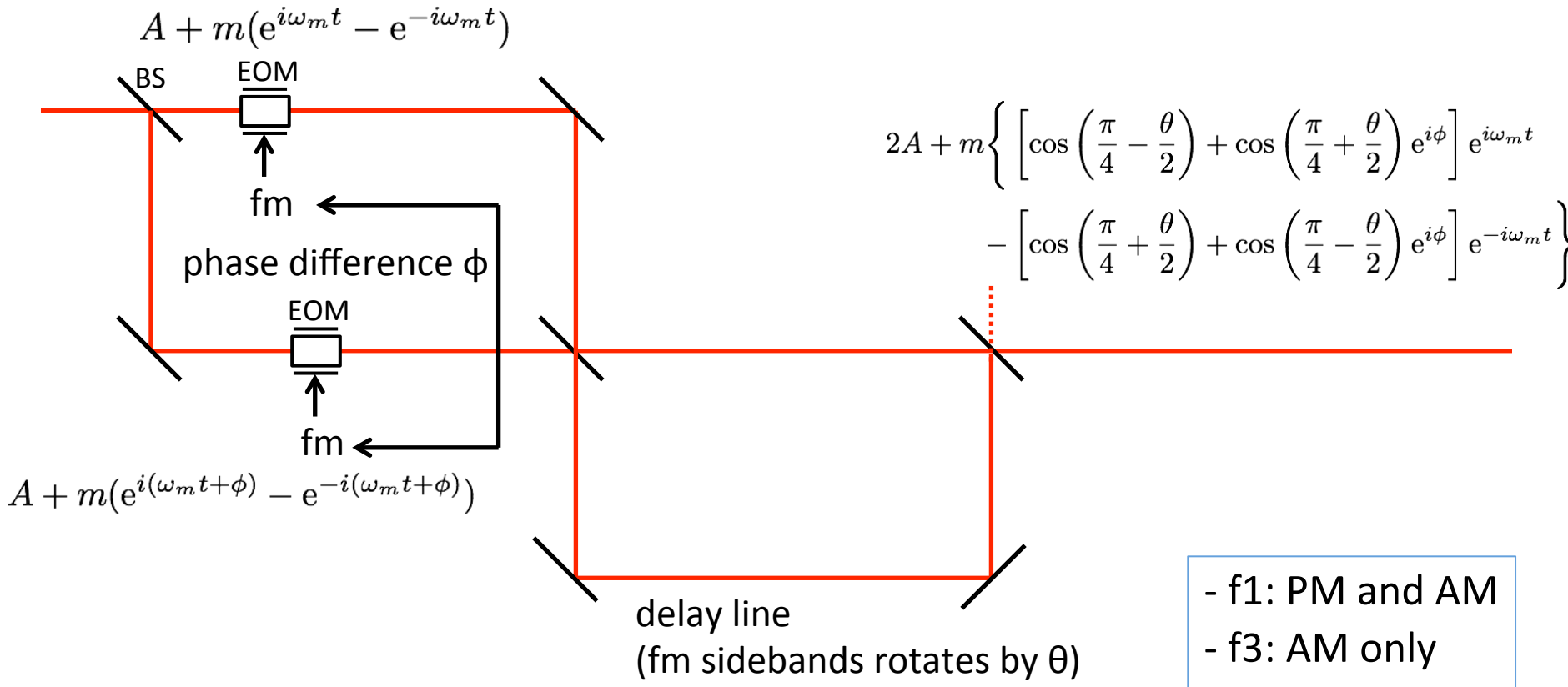
=> change to 2.66 m

- f1: PM and AM (depending on SRC detuning)
- f2: PM only
- f3: AM only (used only for lock acquisition phase)

alternative plan



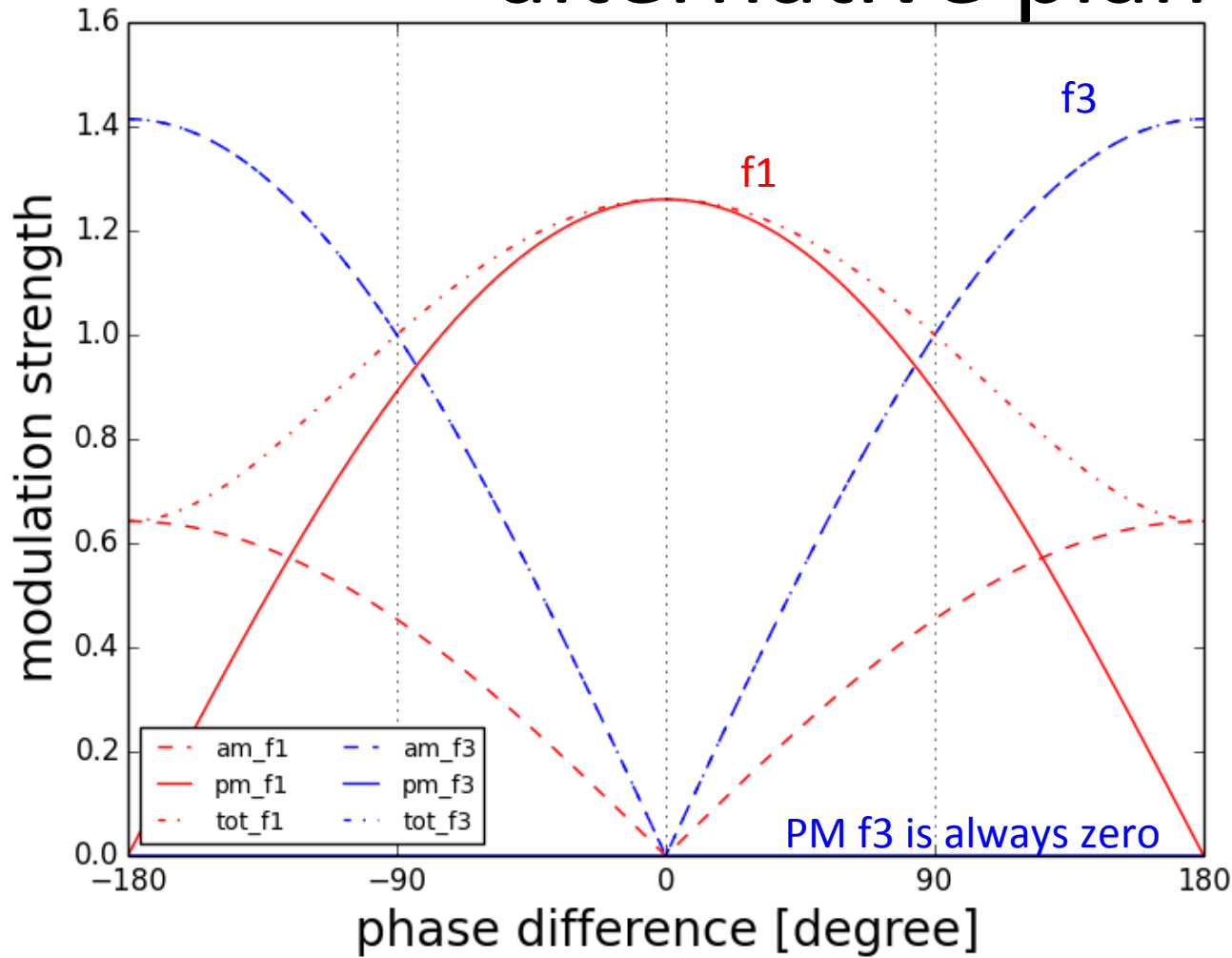
alternative plan



delay line 2.66 m --> $\theta(f_1) = 54^\circ$ --> combination of PM and AM (next page)

$\theta(f_3) = 180^\circ$ --> AM only ($\phi=180^\circ$ is preferable)

alternative plan

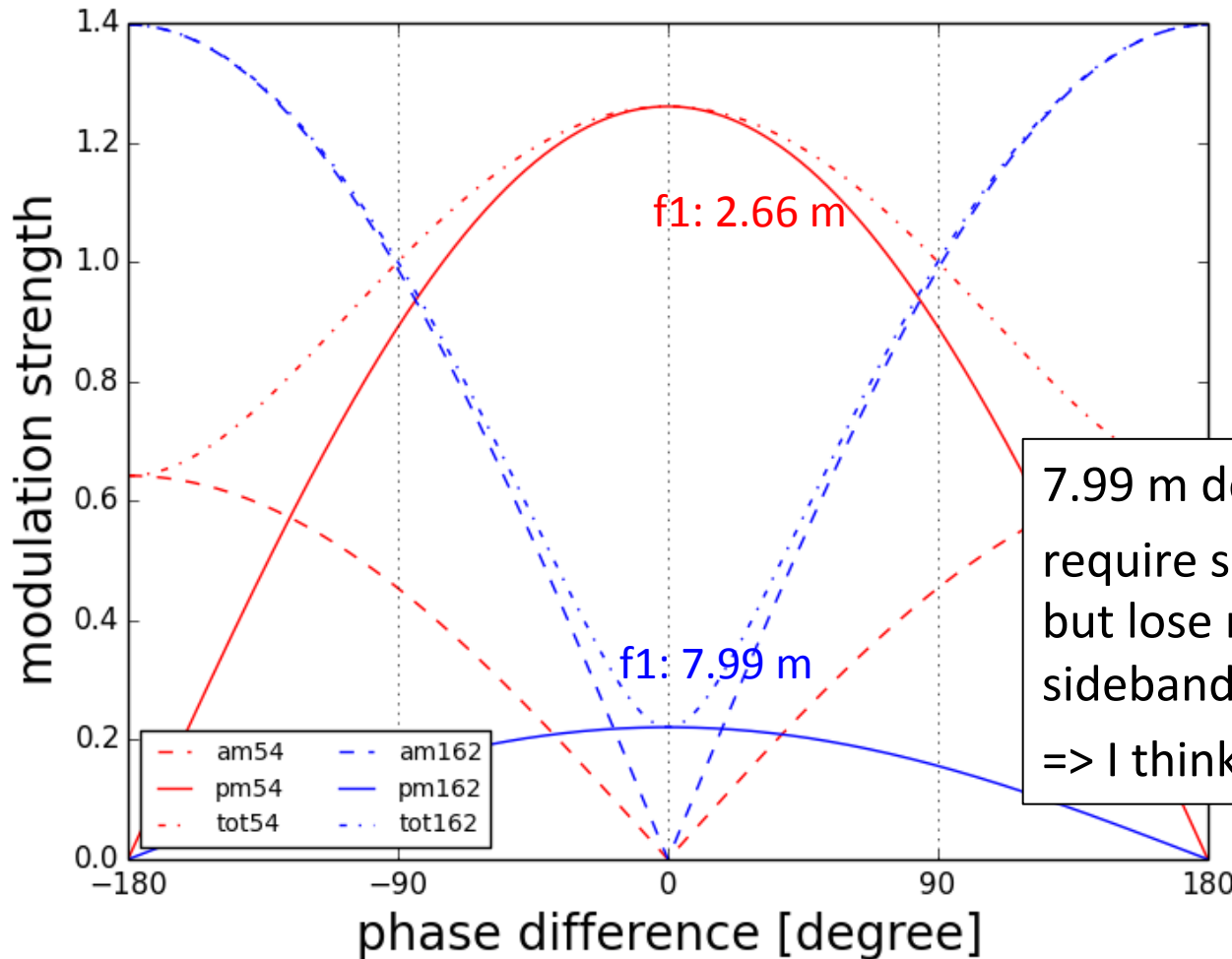


- f1: PM and AM
- f3: AM only

delay line 2.66 m --> $\theta(f_1) = 54^\circ$
 $\theta(f_3) = 180^\circ$

$$2A + m \left\{ \left[\cos\left(\frac{\pi}{4} - \frac{\theta}{2}\right) + \cos\left(\frac{\pi}{4} + \frac{\theta}{2}\right) e^{i\phi} \right] e^{i\omega_m t} - \left[\cos\left(\frac{\pi}{4} + \frac{\theta}{2}\right) + \cos\left(\frac{\pi}{4} - \frac{\theta}{2}\right) e^{i\phi} \right] e^{-i\omega_m t} \right\}$$

2.66 m vs. 7.99 m



7.99 m delay line is also OK.
 require smaller changes of design,
 but lose much more power of f1
 sideband to create AM at f1
 => I think 2.66 m is better.

- f1: PM and AM
 - f3: AM only

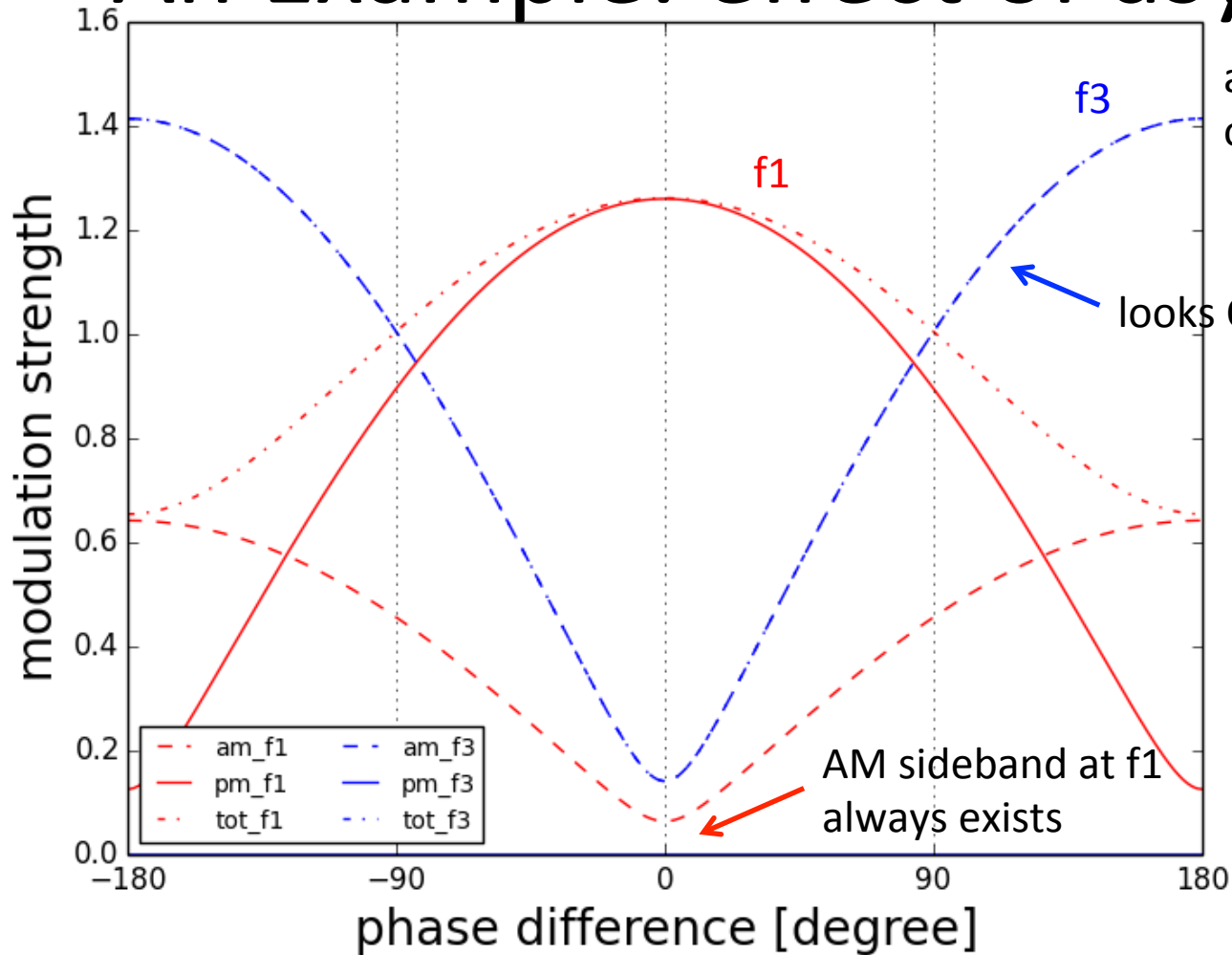
delay line 2.66 m --> $\theta(f_1) = 54^\circ$
 delay line 7.99 m --> $\theta(f_1) = 162^\circ$

$$2A + m \left\{ \left[\cos\left(\frac{\pi}{4} - \frac{\theta}{2}\right) + \cos\left(\frac{\pi}{4} + \frac{\theta}{2}\right) e^{i\phi} \right] e^{i\omega_m t} - \left[\cos\left(\frac{\pi}{4} + \frac{\theta}{2}\right) + \cos\left(\frac{\pi}{4} - \frac{\theta}{2}\right) e^{i\phi} \right] e^{-i\omega_m t} \right\}$$

Remaining issues

- Probably we need some control on the phase difference.
 - How can we the phase difference? Resonant EOM => phase of transfer function modulation/applied voltage can be different for two EOMs and can even be time dependent.
- We need to consider the effect of asymmetries with respect to the requirement; modulation depths of two EOMs, non-perfect mid-fringe lock, non-perfect dark-fringe lock, etc..
- and what else?

An Example: effect of asymmetry



assumed 20 % difference of modulation depths

looks OK for f3

AM sideband at f1 always exists

- f1: PM and AM
- f3: AM only

delay line 2.66 m --> $\theta(f_1) = 54^\circ$
 $\theta(f_3) = 180^\circ$

$$2A + m \left\{ \left[\cos\left(\frac{\pi}{4} - \frac{\theta}{2}\right) + \cos\left(\frac{\pi}{4} + \frac{\theta}{2}\right) e^{i\phi} \right] e^{i\omega_m t} - \left[\cos\left(\frac{\pi}{4} + \frac{\theta}{2}\right) + \cos\left(\frac{\pi}{4} - \frac{\theta}{2}\right) e^{i\phi} \right] e^{-i\omega_m t} \right\}$$