Localization of coalescing binaries with a hierarchical network of gravitational wave detectors

Work report at APP Yoshinori Fujii

This work is mainly supported by Frederique Marion, Thomas Adams and MBTA team (especially in LAPP)



Contents

- **1. Introduction of LAPP and hierarchical search**
- 2. GW-EM follow up pipe line for low-latency CBC search
- 3. Calculation setup
- 4. Optimization of Virgo threshold
- 5. Summary and KAGRA related topic

Introduction : SCAPP

Laboratoire d'Annecy-le-vieux de Physique des Particules









ATLAS



LHCb



Development of low-latency GW search pipeline etc..

My work at LAPP was mainly about data analysis (not Vibration Isolation System)

Introduction : SCAPP

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Topic : how newly constructed detectors should enter the detection network? (in low-latency CBC search)



Introduction :

Several detectors are needed for source localization (detection network)





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The sensitivities of these detectors would be different from each other, especially just after their construction.

(ex. in observation 2 (O2), the higher sensitive 2 LIGOs, and the less sensitive Virgo)

In the Virgo or KAGRA, GW signals can be buried into noise easier than in LIGOs!

Introduction :

Especially, in the low-latency search for Compact Binary Coalescence (CBC)



The detection threshold SNR of less sensitive detectors are wanted to be lowered..

Introduction :

However, if the threshold SNR is purely lowered, we have to handle tons of the triggers



→ Computational cost and time cost get large.. Not low-latency, anymore!

How about including the less sensitive detectors into the network,

- 1. with lower threshold SNR than that of higher sensitive detectors, but
- 2. only when we search triggers, generated from higher sensitive detector's coincidences.

Introduction : "hierarchical search"



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GW-EM follow up pipe line for low-latency CBC search :

https://arxiv.org/pdf/1512.02864.pdf



Multi-Band Template Analysis (MBTA)

 \rightarrow Split the matched filter across two (or more) frequency bands.

- → Shorter templates in each frequency band
- \rightarrow Phase of the signal is tracked over fewer cycles.
- → Smaller sampling rate for low frequency band



Computational cost reduction



BAYESian TriAngulation and Rapid localization (BAYESTAR)



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If arrival timing

is not correct.

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Purpose of this work : in the hierarchical search with HLV,

- 1. What is the optimal threshold for the V1?
- 2. How the localization gets improved at the threshold?



Definitions of the offset angle and the searched area :

<u>1. Offset angle</u>:

Angle between the sky localization of the injected signal, and the reconstructed max probability pixel.

2. Searched area :

The smallest area of the highest confidence region around the max probability pixel, to include the sky location of the injected signal.



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Calculation setup : Main flow

3. Re-construct sky map



Calculation setup : How to transform the triggers, HL \rightarrow HL or HLV

Considered 3 patterns :

Case 1 var. : HL \rightarrow HL or HL + random V

If *p* > FAP, otherwise

Suppose the V1 triggers from noises



Case2 : HL \rightarrow HL, or HL + V based on injection If V1 SNR < threshold, otherwise Suppose the V1 triggers from signals

🛑 Best case

Case 3 : $HL \rightarrow HL$, or HL + random V, or HL + V based on injection

If *p* > FAP and V1 SNR < threshold, If *p* < FAP , If *p* > FAP and V1 SNR > threshold

Suppose the V1 triggers from both of noises and signals

Hore realistic case More realistic case

(How to generate the FAP, random V, V based on injection, is following)

1. "random V trigger : Vr "

1. SNR = Random above a threshold SNR, following measured O1 SNR distribution



 $t_0 = t_{H1}$ if $SNR_{H1} > SNR_{L1}$, otherwise $t_0 = t_{L1}$.

 $\Delta t =$ random uniform number from -35 ms to 35 ms.

3. Phase = random uniform number from 0 rad to 2 π rad.



next page)



Plot SNR distribution from ~ about 20 hours data → Choose typical curve ("quiet")

1. "random V trigger : Vr "

1. SNR = Random above a threshold SNR, following measured O1 SNR distribution



 $t_0 = t_{H1}$ if SNR_{H1} > SNR_{L1}, otherwise $t_0 = t_{L1}$. $\Delta t =$ random uniform number from -35 ms to 35 ms.

3. Phase = random uniform number from 0 rad to 2 π rad.





 $FAP = 1 - \exp(-R \times T)$

R = cumulative rate of background triggers per template, above a given threshold, per template,

T = analyzing time for the V1 (less sensitive detector) -

70 ms for V1

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2. "V based on injection : Vi "

1. SNR = SNR^{expected} + Δ SNR SNR^{expected} = from injection metadata $\Delta SNR = Gaussian(0, 1)$ 2. Timing = $t^{\text{expected}} + \Delta t$ $t^{\text{expected}} = \text{injection meta data}$ $\Delta t = Gaussian(0, 1 ms)$ 3. Phase = $\phi^{\text{expected}} + \Delta \phi$ $\phi^{\text{expected}} = \text{injection meta data}$ $\Delta \phi = \text{Gaussian}(0, 0.25 \text{ rad})$

These uncertainties are added to simulate more from realistic performance. The typical values are used.

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Optimization of Virgo threshold :

Typical result : Self-consistency test

→ Probability - Probability Plot :

90 % confidence area \rightarrow 90% of injections should be included.

For the "case 2", V1 threshold SNR is set at 3.0.



→ Localization depends on :
 1. arrival timing difference

- 2. phase difference
- 3. relative SNR.

 \rightarrow If the added uncertainties are properly, the curve should along with the diagonal line.

In this HLV search (blue), the curve gets below the diagonal line a little bit. \rightarrow The added uncertainties are not crazy (though a little bit not realistic).

2. Timing =
$$t^{\text{expected}} + \Delta t$$

 $\Delta t = \text{Gaussian}(0, 1 \text{ ms}) ----> 1 \text{ ms} \times \frac{6}{V1 \text{ SNR}}$ etc. ?



Collect the median values, with changing V1 threshold SNR



The optimal threshold SNR for V1 is at around 3.5 ~ 4.0. (Threshold for H1, L1 = 5.0)

Optimization of Virgo threshold :

Is the optimal threshold still valid for the noisy case?

What is happen if noisier SNR distribution, FAP are used?

Calculation setup : How to transform the triggers, HL \rightarrow HLV

Changed points :

Optimization of Virgo threshold :

If the background triggers are noisy, the localization can be worse. However, the optimal threshold for V1 still works.

ratio

0.8

0.4

0.2

Median 9.0

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Summary

Investigated sky localization performance in "hierarchical search" with 3 detectors HLV, and look for the optimal threshold for V1

1. What is the optimal threshold for the V1?

 \rightarrow Optimal threshold for V1 is around 3.5 ~ 4.

2. How the localization gets improved at the threshold?

 \rightarrow Offset angle, searched area are reduced to ~70 % at the threshold, according to the setup.

→ even if the V1 is less sensitive than H1, L1, in the hierarchical search, V1 improves the sky localize performance, comparing to the double detector search.

 \rightarrow The hierarchical search is useful to enter newly constructed detectors into the network.

... How about the "Hierarchical search" with 4 detectors HLVK ?

KAGRA related topic (Just for introducing)

1) K1 Noise curve

2) K1 Horizon distance are same as V1:

H1, L1 = 70 Mpc, V1, K1 = 20 Mpc.

3) V1, K1 thresholds are set as same.

Look for the optimal threshold SNR for V1, K1, in this search.

KAGRA related topic : Setup

(Parameters for V1, K1 are mostly same in each other.)

False Alarm Probability

SNR distribution (per template)

 $FAP = 1 - \exp(-R \times T)$

R = cumulative rate of background triggers per template,

above a given threshold, per template,

T = analyzing time for the V1 (less sensitive detector) -

70 ms for V1 80 ms for K1

Calculation setup : How to transform the triggers, HL \rightarrow HLV or HLK or HLVK

2 Procedure	Case 3 : V1, K1 triggers are either random or based on injection parameters				
p_{V1} , p_{K1} = random uniform number from 0 to 1.	FAP = FAP(SNR) if SNR > Threshold, otherwise $FAP = FAP(Threshold)$				
Case 1 : V1, K1 triggers are random	• $p_{V1} < FAP_{V1}$ and $p_{K1} < FAP_{K1}$ \Rightarrow HL + V _{random} + K _{random} • $p_{V1} < FAP_{V1}$ and, $p_{K1} > FAP_{K1}$ and $SNR_{K1} > Threshold_{K1}$ \Rightarrow HL + V _{random} + K _{inj}				
$HL + V_{random} + K_{random}$	 p_{V1} > FAP_{V1} and SNR_{V1} > Threshold_{V1} and 				
Case 1 var : V1, K1 triggers are random	$p_{K1} < FAP_{K1}$ \Rightarrow HL + V _{inj} + K _{random} • $p_{V1} > FAP_{V1}$ and SNR _{V1} > Threshold _{V1} and				
$p_{V1} < FAP_{V1}$ and $p_{K1} < FAP_{K1} \Rightarrow HL + V_{random} + K_{random}$	$p_{K1} > FAP_{K1}$ and $SNR_{K1} > Threshold_{K1} \Rightarrow HL + V_{inj} + K_{inj}$ • $p_{V1} < FAP_{V1}$ and				
$p_{V1} > FAP_{V1}$ and $p_{K1} < FAP_{K1} \Rightarrow HL + K_{random}$ $p_{V1} < FAP_{V1}$ and $p_{K1} > FAP_{K1} \Rightarrow HL + V_{random} +$	$p_{K1} > FAP_{K1}$ and $SNR_{K1} < Threshold_{K1} \Rightarrow HL + V_{random} + p_{V1} > FAP_{V1}$ and $SNR_{V1} < Threshold_{V1}$ and				
$p_{V1} > FAP_{V1}$ and $p_{K1} > FAP_{K1} \Rightarrow HL + +$	$p_{K1} < FAP_{K1} \Rightarrow HL + K_{random}$ $\Rightarrow p_{V1} > FAP_{V1}$ and $SNR_{V1} > Threshold_{V1}$ and				
Case 2 : VI, KI triggers are based on injection parameters Best case	$p_{K1} > FAP_{K1}$ and $SNR_{K1} < Threshold_{K1} \Rightarrow HL + V_{inj} +$				
$SNR_{V1} > Threshold_{V1}$ and $SNR_{K1} > Threshold_{K1} \Rightarrow HL + V_{inj} + K_{inj}$ $SNR_{V1} < Threshold_{V1}$ and $SNR_{K1} > Threshold_{K1} \Rightarrow HL + K_{inj}$ $SNR_{V1} > Threshold_{V1}$ and $SNR_{K1} < Threshold_{K1} \Rightarrow HL + V_{inj} +$	• $p_{V1} > FAP_{V1}$ and $SNR_{V1} < Threshold_{V1}$ and $p_{K1} > FAP_{K1}$ and $SNR_{K1} > Threshold_{K1} \Rightarrow HL + K_{inj}$ • $p_{V1} > FAP_{V1}$ and $SNR_{V1} < Threshold_{V1}$ and				
$SNR_{V1} < Threshold_{V1}$ and $SNR_{K1} < Threshold_{K1} \Rightarrow HL + +$	$p_{K1} > FAP_{K1}$ and $SNR_{K1} < Threshold_{K1} \Rightarrow HL + +$				

Optimization of V1, K1 threshold :

Offset angle

Now calculation of HLVK is ongoing..

1.2

1.0

Median ratio 9.0 8

0.4

0.2

0.0 0

Maximum probability Searched area Worst Best **More realistic** 0.4 case 1 var.

Offset angle

(Uncertainties of the red points are to be investigated.)

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Searched

area

Injection position

Optimization of V1, K1 threshold : Offset angle

Now calculation of HLVK is ongoing..

Case2 = "Best" case

Searched

area

Maximum

probability

Injection position

Offset angle

Case3 = "More realistic" case

Optimization of V1, K1 threshold : Searched area

Now calculation of HLVK is ongoing..

Injection position Searched arched area Offset angle Maximum Case3 = "More realistic" case

Case2 = "Best" case

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Next step (ongoing)

- 1. To get more realistic results,
 - simulate the localization performances with changing the added timing uncertainties.
- 2. Continue the calculation about the hierarchical search with 4 detectors HLVK

...

Tools which I learned : Vega

vega : plotting tool based on ROOT.

Mainly (in my case)

* Plot histograms, such as SNR distribution.

* Fit

* Edit MBTA output files (.gwf), or Bayestar input files (.xml)

Tools which I learned : Bayestar

Bayestar : mainly

bayestar_localize_coinc :

* Generate files to plot skymaps (this process needs long time : ~ one night)

bayestar_aggregate_found_injections :

* Generate files to plot offsets angles, searched area, 90 % confidence area ,,,

bayestar_plot_allsky :

* Generate skymaps

olserver59[~]: bayestar_	
bayestar_aggregate_found_injections	bayestar_plot_found_injections
bayestar_bin_samples	bayestar_plot_pileup
bayestar_lattice_tmpltbank	bayestar_prune_neighborhood_tmpltbank
bayestar_littlehope	bayestar_realize_coincs
bayestar_localize_coincs	bayestar_sample_model_psd
bayestar_localize_lvalert	bayestar_sim_to_tmpltbank
bayestar_plot_allsky	
olserver59[~]: bavestar	

Bayestar has more functions. what I'm using is only these ones.

* Except for them, I'm using "ligolw", some python codes etc.

Definitions of the offset angle and the searched area :

- 1. Offset angle
- 2. Searched area

How far the localization is from the true injected position

Certain confidence area
 (ex. 90 % confidence area)

How spread or concentrated each probability is

Optimization of Virgo threshold :

Is the optimal threshold still valid for the noisy case?

SNR distribution

rate [evt/hour/template]

trigger

False Alarm Probability

Update the sky localization performance in the case 3 : Summary of sky localization performance

HLVr = HL + Vrandom HLVi = HL + Vinjection

Update the sky localization performance in the case 3 : Summary of sky localization performance HLVr = HL + Vrandom HLVi = HL + Vinjection

Start to generate skymaps with 4 detectors (one-template search)

Start to generate skymaps with 4 detectors (one-template search)

Vr = Vrandom Vi = Vinjection

Trigger population seems to be strange...

* Start to generate skymaps with 4 detector

 $\Delta T_{HK} \equiv 30 \text{ msec}$

- $\Delta T_{LK} \equiv 40 \text{ msec}$
- $T \equiv 80 \text{ msec}$

(T is Time window for searching K1 trigger)

- $\Delta T_{HV} \equiv 35 \text{ msec}$
- $\Delta T_{LV} \equiv 35 \text{ msec}$
- $T \equiv 70 \text{ msec}$

(Time window for searching v1 trigger)

HL \rightarrow HL or HLV or HLK or HLVK

1.1 Genetaing random triggers : V_{random} , K_{random}
• $SNR = Raodom$ above a threshold SNR, following measured O1 SNR distribution.
• Time = $t_0 + \Delta t$ • $t_0 = t_{H1}$ if SNR _{H1} > SNR _{L1} , otherwise $t_0 = t_{L1}$ • Δt = random uniform number: from -35 ms to 35 ms, for V1. from ms to ms, for K1.
• Phase = random uniform number from 0 rad to 2π rad.
• Effective distance $D_{\rm eff} = 2.26 \times \text{detection range} \times 8 / \text{SNR}$
1.2 Generating triggers based on injection parameters : V_{inj} , K_{inj}
• SNR = SNR ^{expected} + Δ SNR • SNR ^{expected} = 2.26 × detection range × 8 / D_{eff} • Δ SNR = random Gaussian(0, 1). • D_{eff} = injection meta data • detection range for V1 = 54 Mpc × 20 Mpc / 70 Mpc • detection range for K1 = 54 Mpc × 20 Mpc / 70 Mpc
• Time = $t^{\text{expected}} + \Delta t$ • t^{expected} = injection meta data • Δt = random Gaussian(0,1 ms).
• Phase = $\phi_0 + \Delta \phi$ • $\phi_0 = \phi_{H1} - \Delta \phi_{HV}^{expected}$ if SNR _{H1} > SNR _{L1} , otherwise $\phi_0 = \phi_{L1} - \Delta \phi_{LV}^{expected}$, for V1 • $\phi_0 = \phi_{H1} - \Delta \phi_{HK}^{expected}$ if SNR _{H1} > SNR _{L1} , otherwise $\phi_0 = \phi_{L1} - \Delta \phi_{LK}^{expected}$, for K1 $\phi_{H1}, \phi_{L1} =$ injection metadata $\Delta \phi_{HV}^{expected}, \Delta \phi_{HK}^{expected}, \Delta \phi_{LK}^{expected}$ are generated from injection metadata. • $\Delta \phi =$ random Gaussian(0, 0.25 rad).
Note that the Gaussian(μ , σ) corresponds to this function:

Gaussian
$$(\mu, \sigma) \equiv \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$$

2 Procedure						
$p_{V1}, p_{K1} =$ random uniform number from 0 to 1.						
Case 1 : V1, K1 triggers are random						
$HL + V_{random} + K_{random}$				(2)		
Case 1 var : V1, K1 triggers are random						
$p_{V1} < FAP_{V1}$ and $p_{K1} < FAP_{K1} \Rightarrow HL + V_{ra}$	ndom	+ K _{random}		(3)		
$p_{V1} > FAP_{V1}$ and $p_{K1} < FAP_{K1} \Rightarrow HL +$		+ K _{random}		(4)		
$p_{V1} < FAP_{V1}$ and $p_{K1} > FAP_{K1} \Rightarrow HL + V_{ra}$	ndom	+		(5)		
$p_{V1} > FAP_{V1}$ and $p_{K1} > FAP_{K1} \Rightarrow HL +$		+		(6)		
Case 2 : V1, K1 triggers are based on injection parameters						
$SNB_{V1} > Thresholdy_1$ and $SNB_{K1} > Threshold_{K1}$	⇒	HL + Vini +	Kini	(7)		
$SNR_{V,1} \leq Thresholdy_1$ and $SNR_{K,1} \geq Threshold_{K,1}$, ⇒	HL + +	Kini	(8)		
$SNR_{V1} > Threshold_{V1}$ and $SNR_{K1} < Threshold_{K1}$	⇒	HL + Vini +	- mj	(9)		
$SNR_{V1} \leq Threshold_{V1}$ and $SNR_{V1} \leq Threshold_{V1}$, ⇒	HL + +		(10)		
				()		
Case 3 : V1, K1 triggers are either random or based o	n in	jection parame	ters			
FAP = FAP(SNR) if SNR > Threshold, otherwise $FAP = F$	AP(Threshold)				
• $\pi \mu i < FAP \mu i$ and $\pi \mu i < FAP \mu i$	->	HI. + Varatar	+ Keeder	(11)		
• $p_{VI} < FAP_{VI}$ and $p_{KI} < FAF_{KI}$	7	III. + Viandom	+ Israndom	(11)		
$p_{V1} > FAP_{V1}$ and $SNB_{V1} > Thresholder$	-	$HL + V_{-1}$	+ K	(12)		
• $p_{K1} > FAP_{K1}$ and $SNR_{K1} > Thresholdy_{k1}$ and	7	random	1 Isinj	(12)		
$p_{V1} \leq FAP_{V1}$ and $Stat_{V1} \geq Intested V_1$ and $p_{V1} \leq FAP_{V1}$	⇒	$HL + V_{i-1}$	+ Kanadara	(13)		
• $p_{V1} > FAP_{V1}$ and $SNR_{V1} > Thresholdy_1$ and		···· inj	random	(10)		
$p_{V1} > FAP_{V1}$ and $SNR_{V1} > Threshold_{V1}$	⇒	HL + Vini	+ K::	(14)		
• $\pi_{K1} < FAP_{V1}$ and		· · · · · · · · · · · · · · · · ·	i inj	()		
$p_{K1} > FAP_{K1}$ and $SNB_{K1} < Threshold K1$	⇒	HL + Vrandom	+	(15)		
• $p_{V1} > FAP_{V1}$ and $SNR_{V1} < Thresholdy_1$ and				(10)		
$p_{V1} \leq FAP_{V1}$	⇒	HL +	+ Krandom	(16)		
• $p_{V1} > FAP_{V1}$ and $SNR_{V1} > Threshold_{V1}$ and			1 - Tandom	()		
$p_{K1} > FAP_{K1}$ and $SNR_{K1} < Threshold_{K1}$	⇒	HL + Vini	+	(17)		
• $p_{V1} > FAP_{V1}$ and $SNR_{V1} < Threshold_{V1}$ and						
$p_{K1} > FAP_{K1}$ and $SNR_{K1} > Threshold_{K1}$	⇒	HL +	+ K _{ini}	(18)		
• $p_{V1} > FAP_{V1}$ and $SNR_{V1} < Thresholdy_1$ and						
$p_{K1} > FAP_{K1}$ and $SNR_{K1} < Threshold_{K1}$	⇒	HL +	+	(1 2) л		
-				54		

* Start to generate skymaps with 4 detector (V1, K1 threshold = 3.5)

* Investigate the SNR distribution at low SNR distribution

At low SNR, if collecting time gets shorter,

1) the saturation gets better, and 2) curves get close to red line(extrapolated one)

At High SNR, there are mostly no differences \rightarrow distributions don't depend on how to analyze, and templates.

* Investigate relation between the P-P plot and timing fluctuation * (Arriving time) = (meta data) + (Gaussian)

Gaussian $\sigma_{\text{Time}} = 1 \text{ ms}$ (Const.) $\rightarrow \sigma_{\text{Time}} = Time \text{ or } Time \times \frac{6}{\text{SNR}}$

