

Cryopayload meeting

26th Aug. 2014
Dan Chen

Thermal noise calculation

Thermal noise:

Yu. Levin PRD 1998

$$S_x(f) = \frac{2k_B T}{\pi^2 f^2} \frac{W_{\text{diss}}}{F_0^2},$$

$$W_{\text{diss}} = 2\pi f U_{\text{max}} \phi(f),$$

We can calculate thermal noise from stored energy “U_max” when we apply a “Levin force” on the mirror.

Levin force:

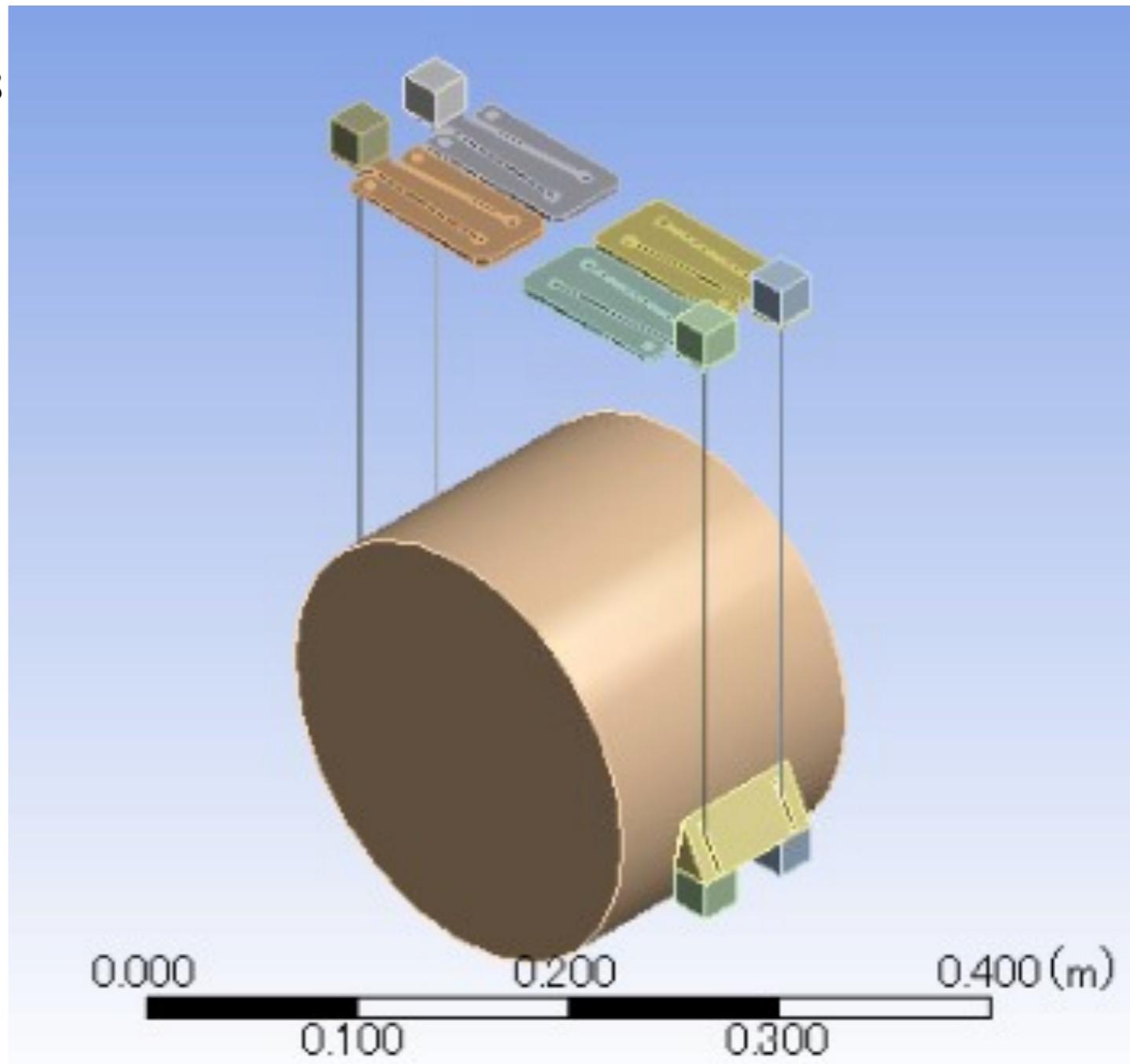
$$F_L = \frac{2a}{\pi w_0^2} \exp\left(-\frac{2r^2}{w_0^2}\right)$$

$$a=1.0, w_0=0.035$$

Loss

Sapphire fiber: 1.0919e-7 measured at Roma

Sapphire bulk: 4.0e-9 measured by Uchiyama-san



Thermal noise calculation

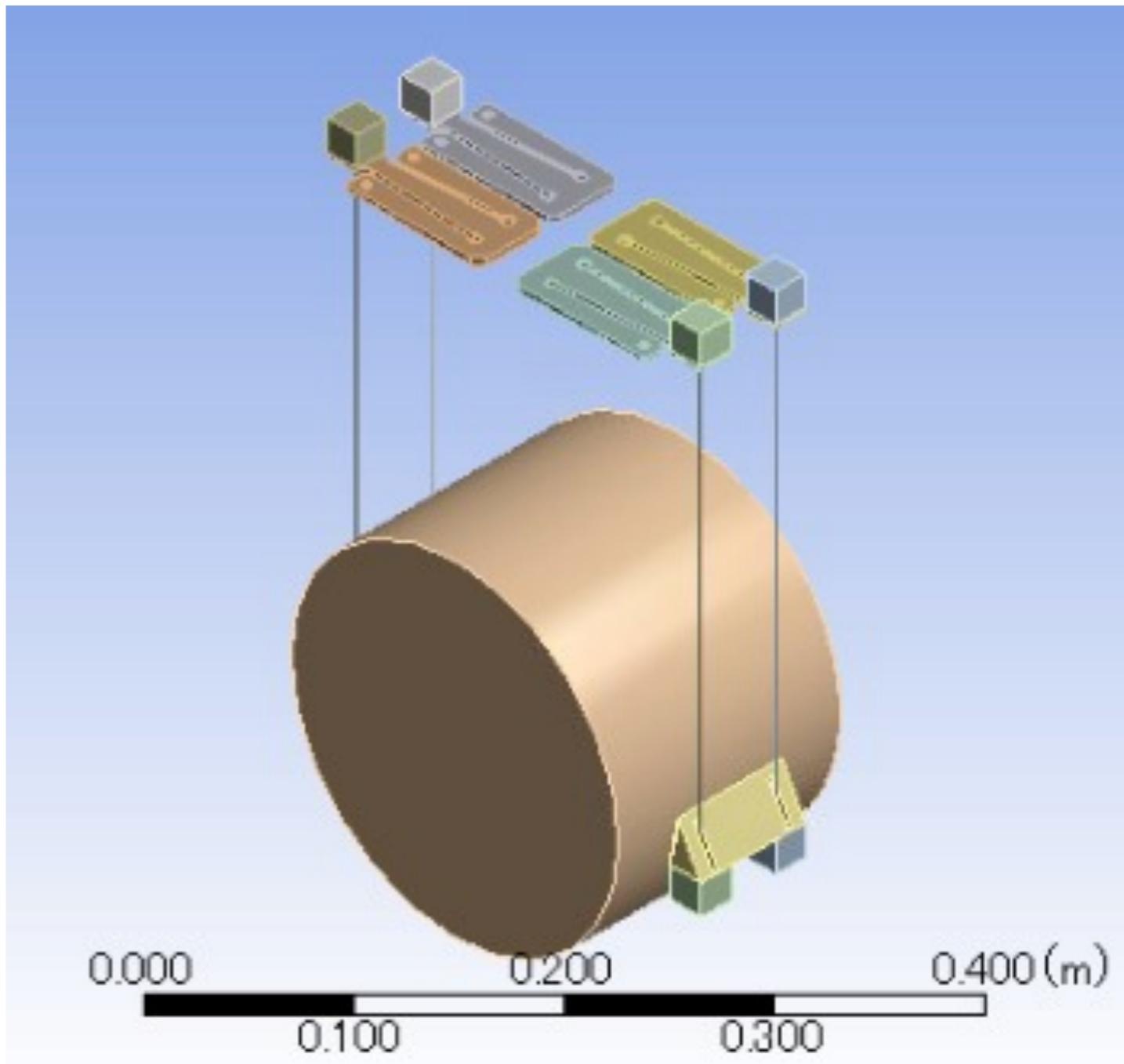
Thermal noise:

Yu. Levin PRD 1998

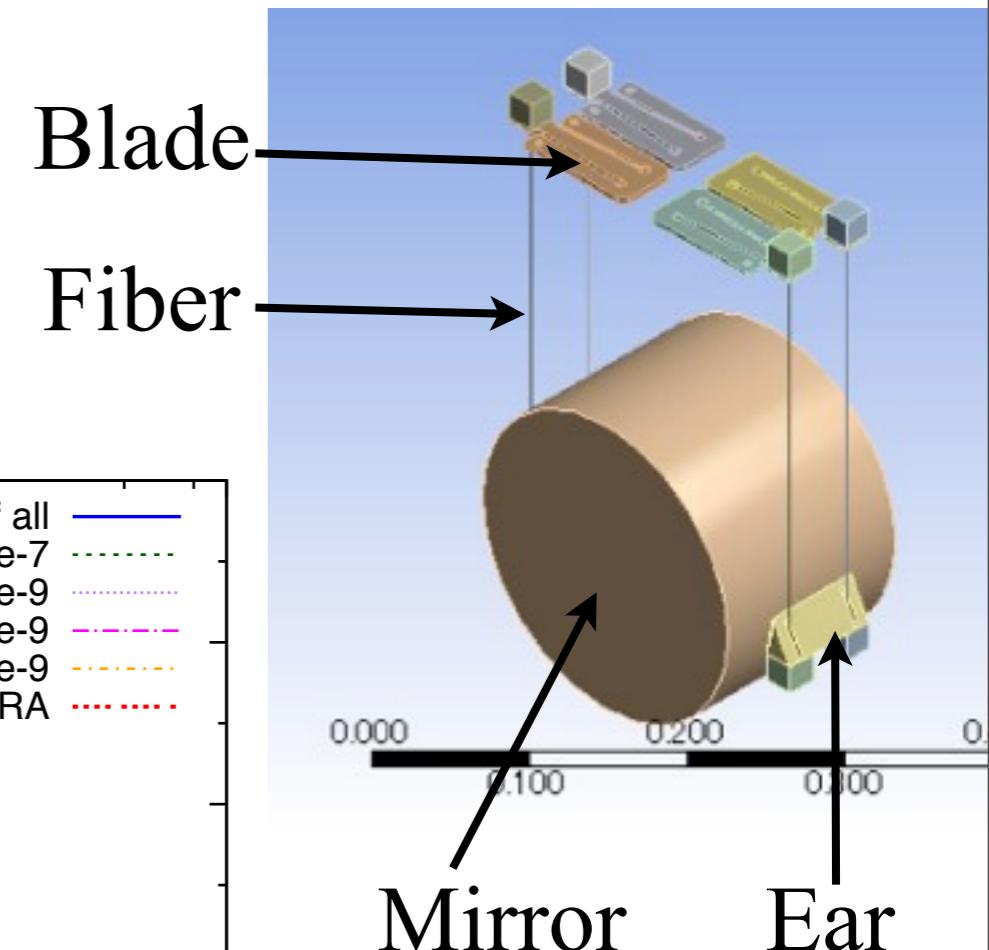
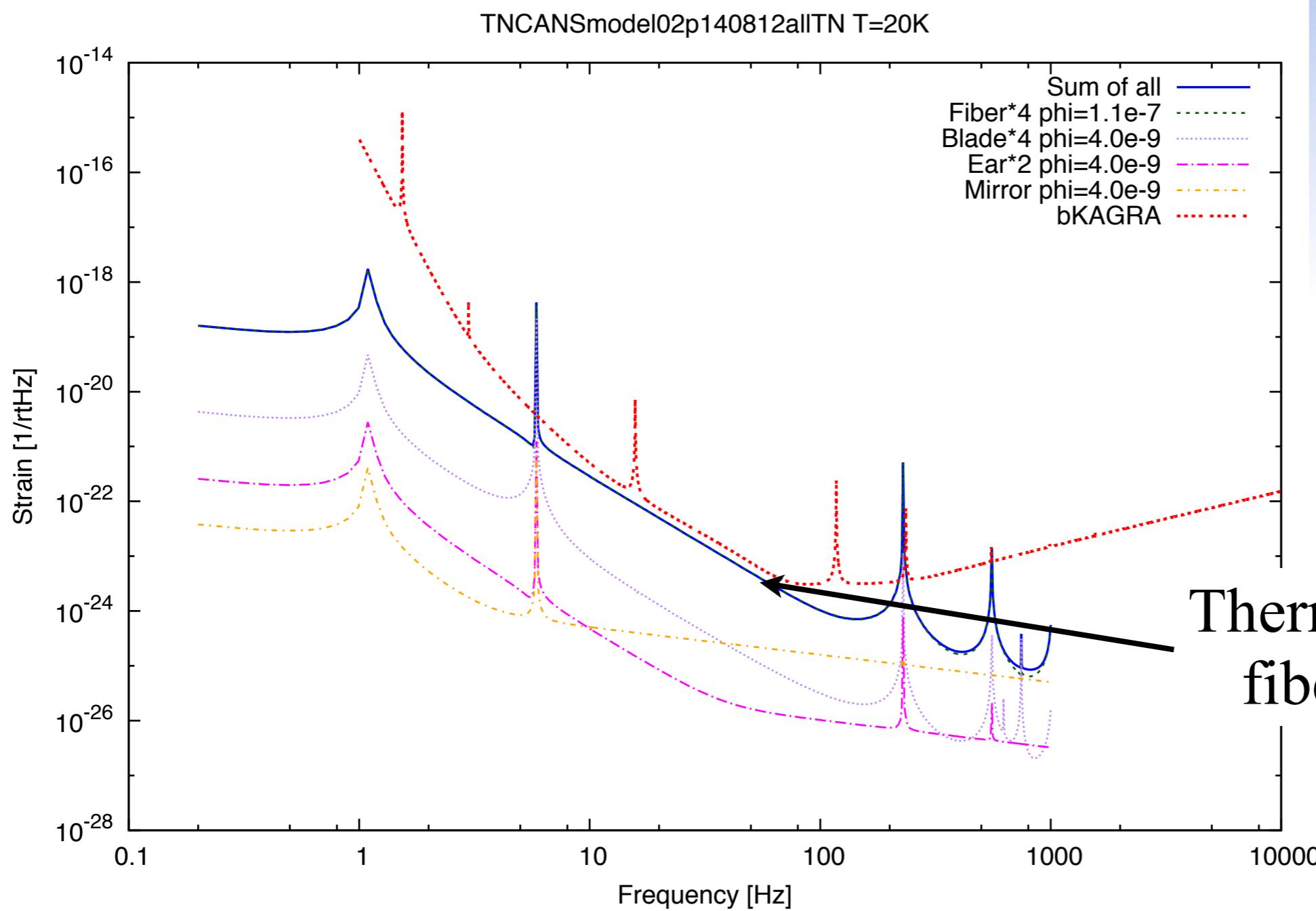
$$S_x(f) = \frac{2k_B T}{\pi^2 f^2} \frac{W_{\text{diss}}}{F_0^2},$$

$$W_{\text{diss}} = 2\pi f U_{\text{max}} \phi(f),$$

If we can calculate U_{max} for each part, we can estimate the contribution from each part.

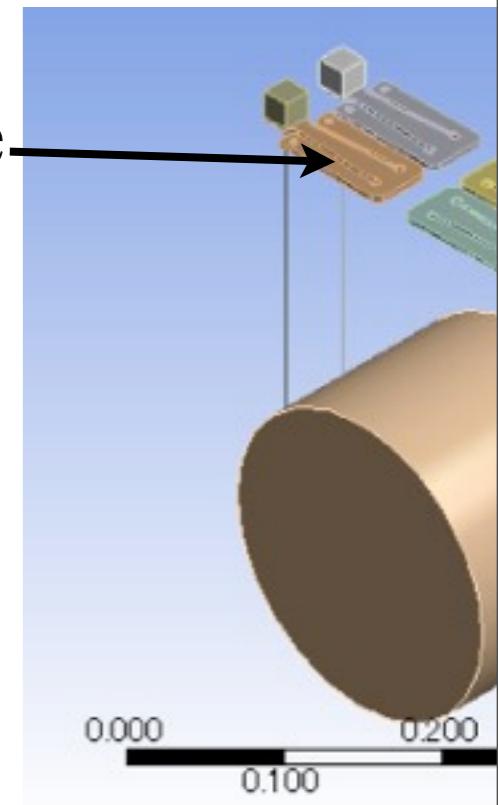
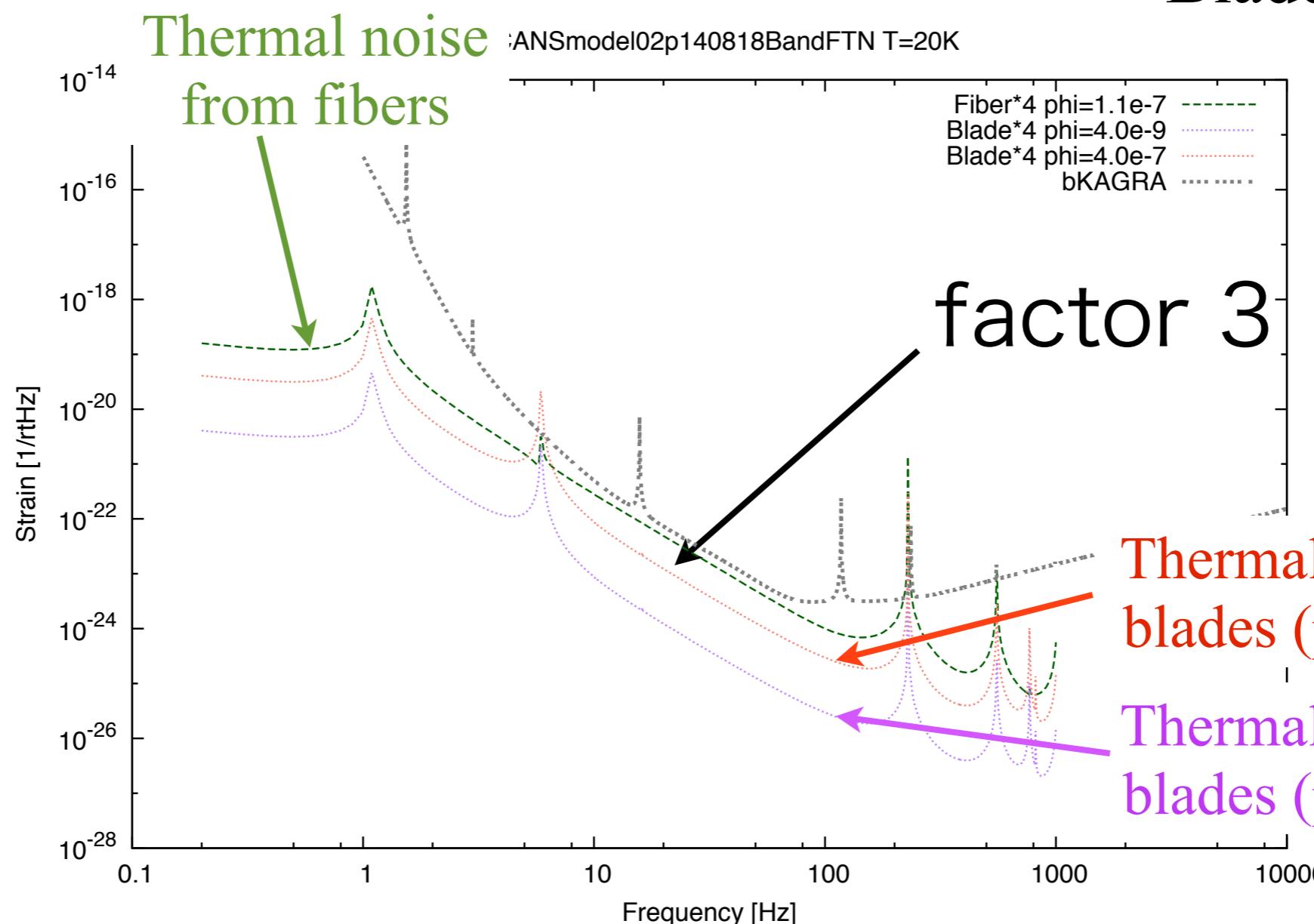


Thermal noise calculation



Thermal noise from
fibers dominate

Thermal noise calculation Requirement for blades



Requirement for loss of blades: $\phi=4.0\text{e-}7$ (?)

We need to decide
safty factor

Thermal noise calculation with clamp

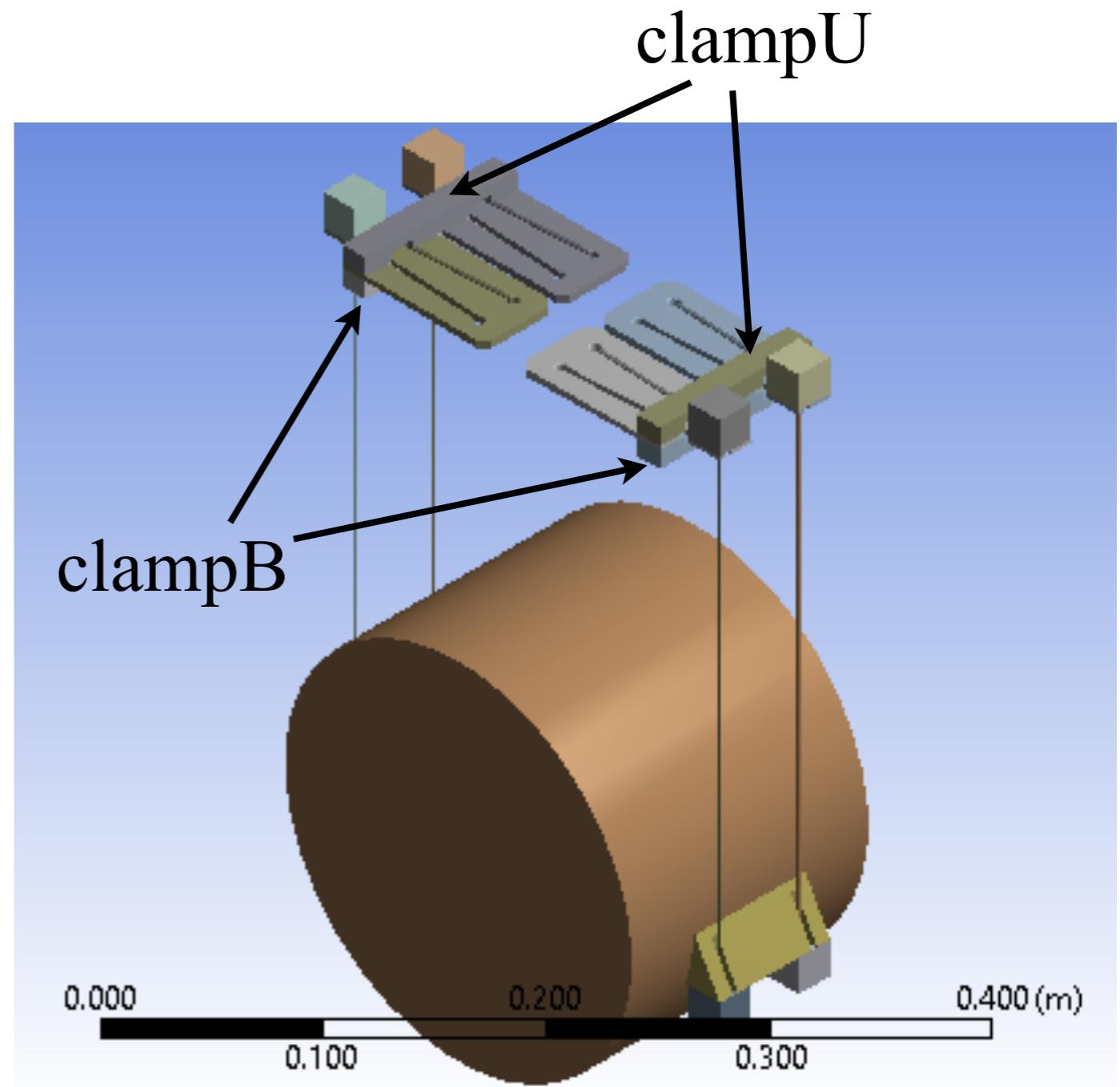
Thermal noise:

Yu. Levin PRD 1998

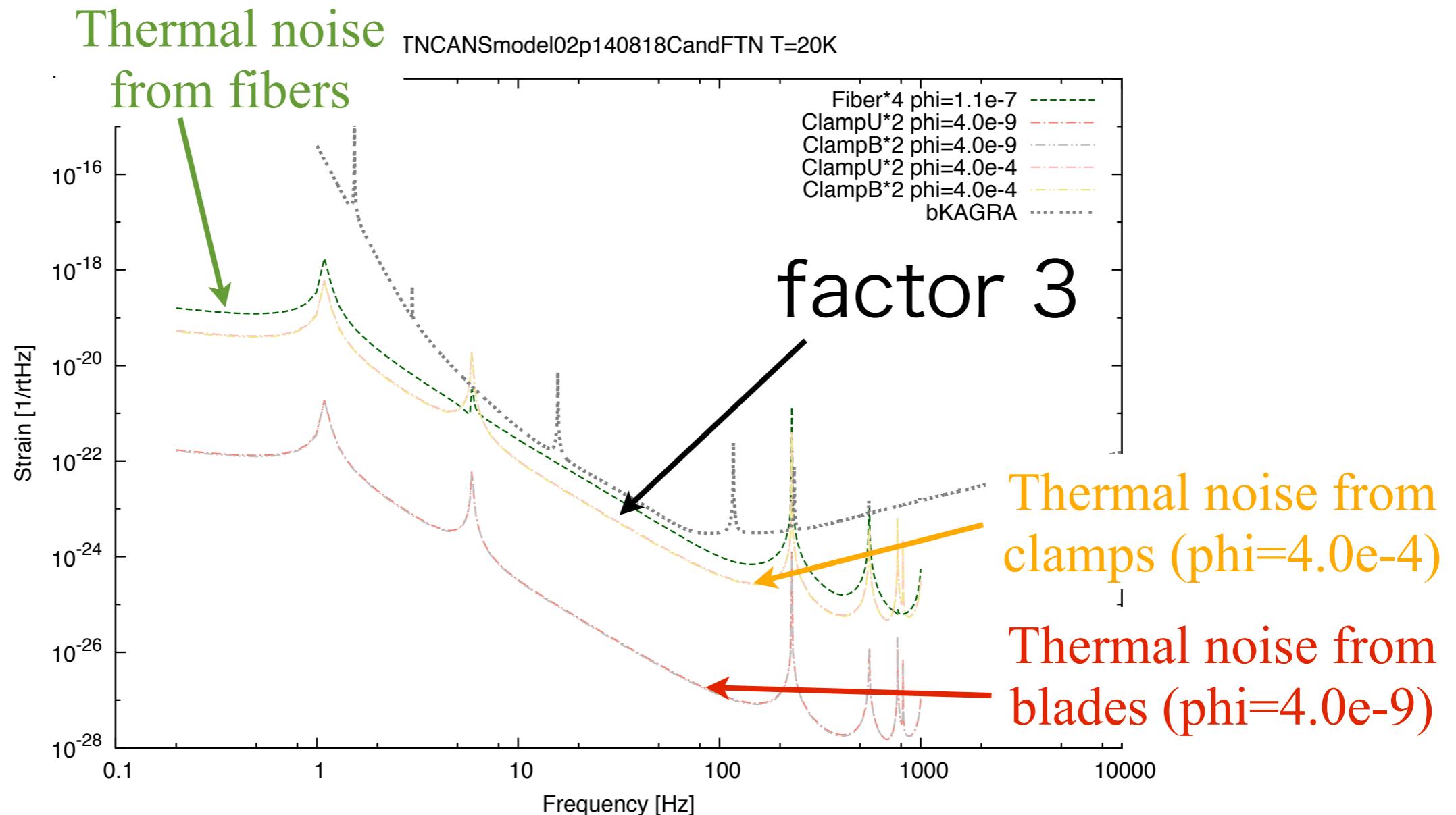
$$S_x(f) = \frac{2k_B T}{\pi^2 f^2} \frac{W_{\text{diss}}}{F_0^2},$$

$$W_{\text{diss}} = 2\pi f U_{\text{max}} \phi(f),$$

I added clamps made of sapphire for blades to calculate the thermal noise contribution.



Thermal noise calculation with clamp

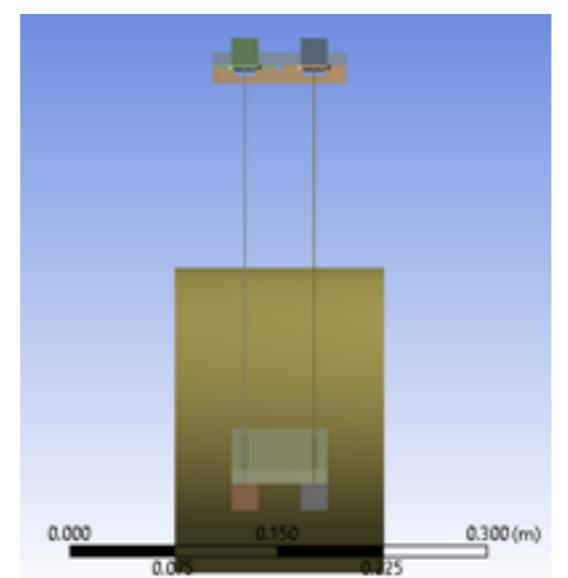
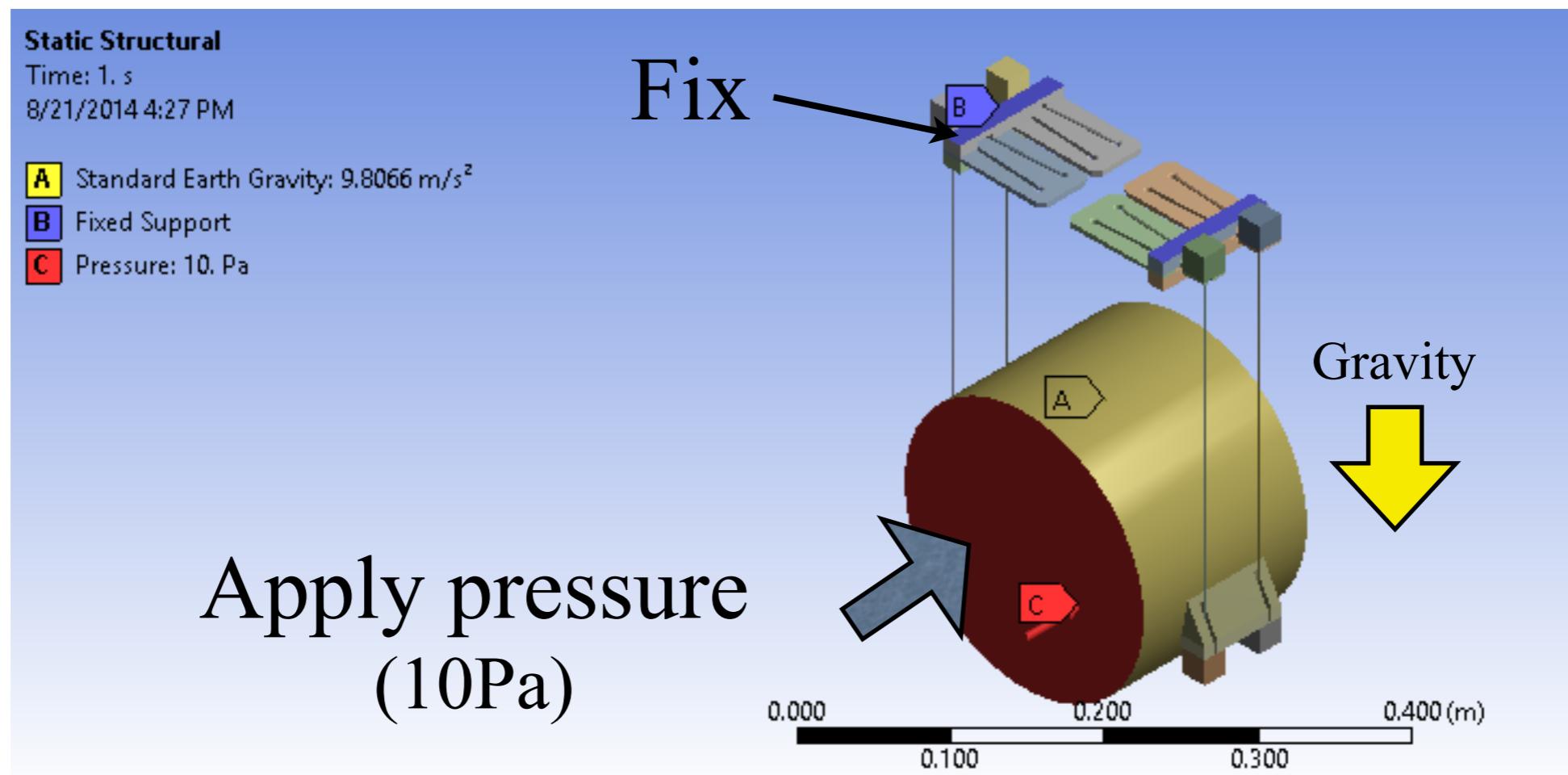


I used Y of sapphire for the clamps.

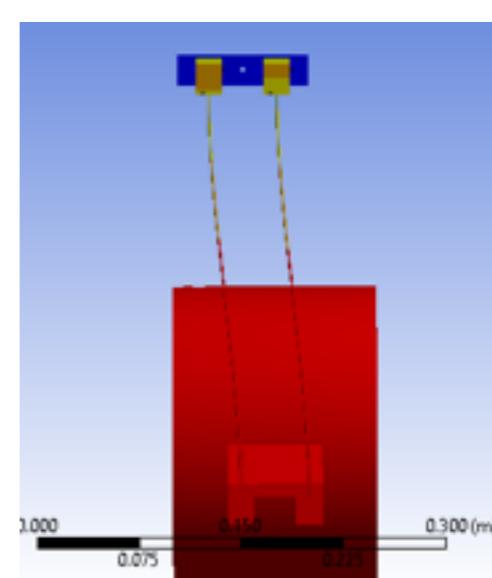
Requirement for loss of clamps: $\phi = 4.0 \times 10^{-4}$ (?)

We need to decide
safty factor

Bending length calculation

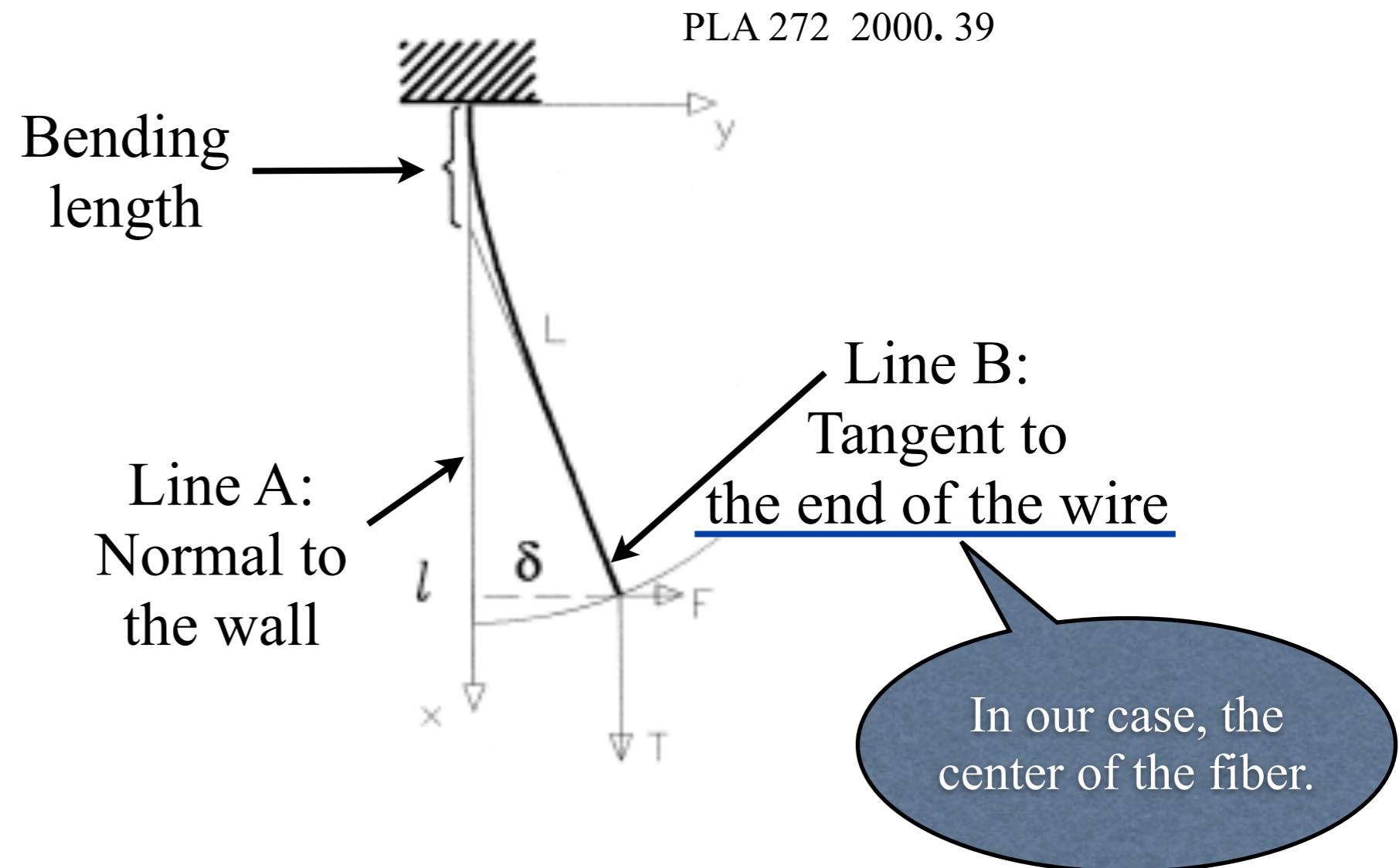
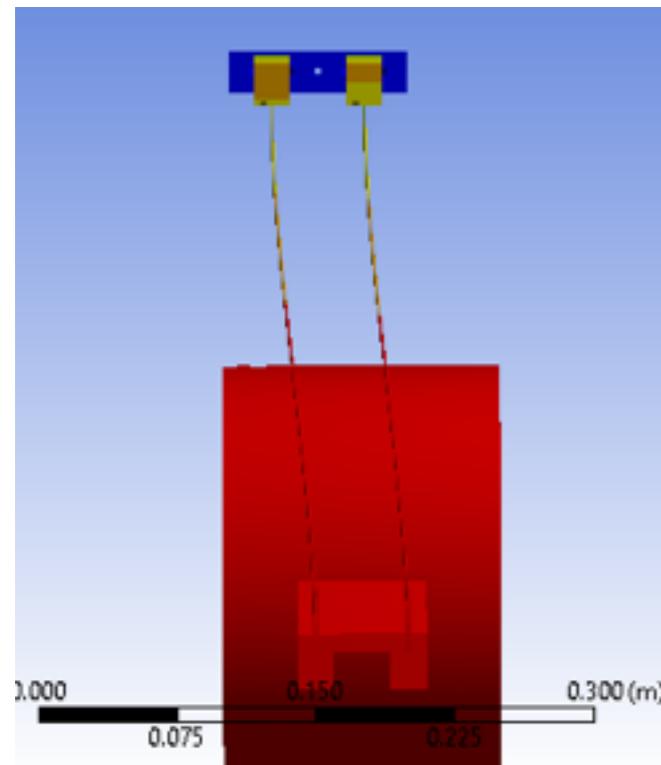


Defomation
by pressure



Bending length calc by ANSYS

Let's define the bending length.

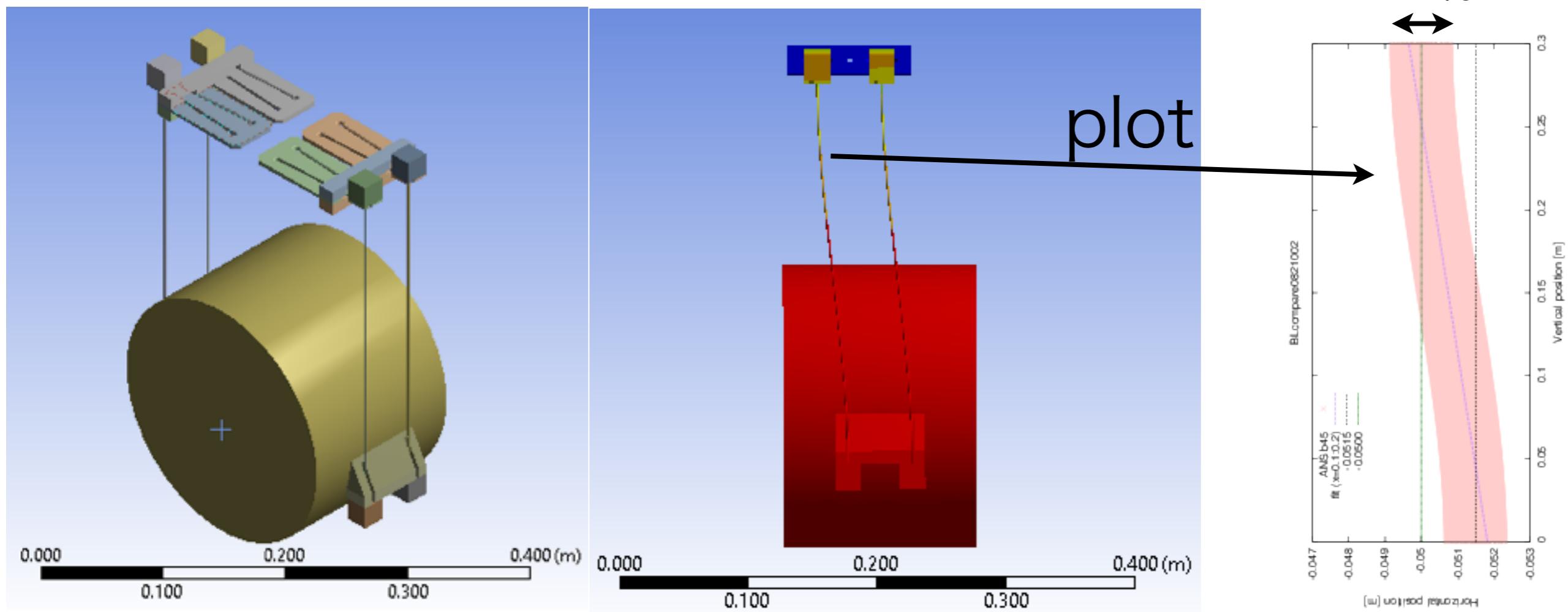


Bending length:

The distance between the wall and the cross point of line A and B

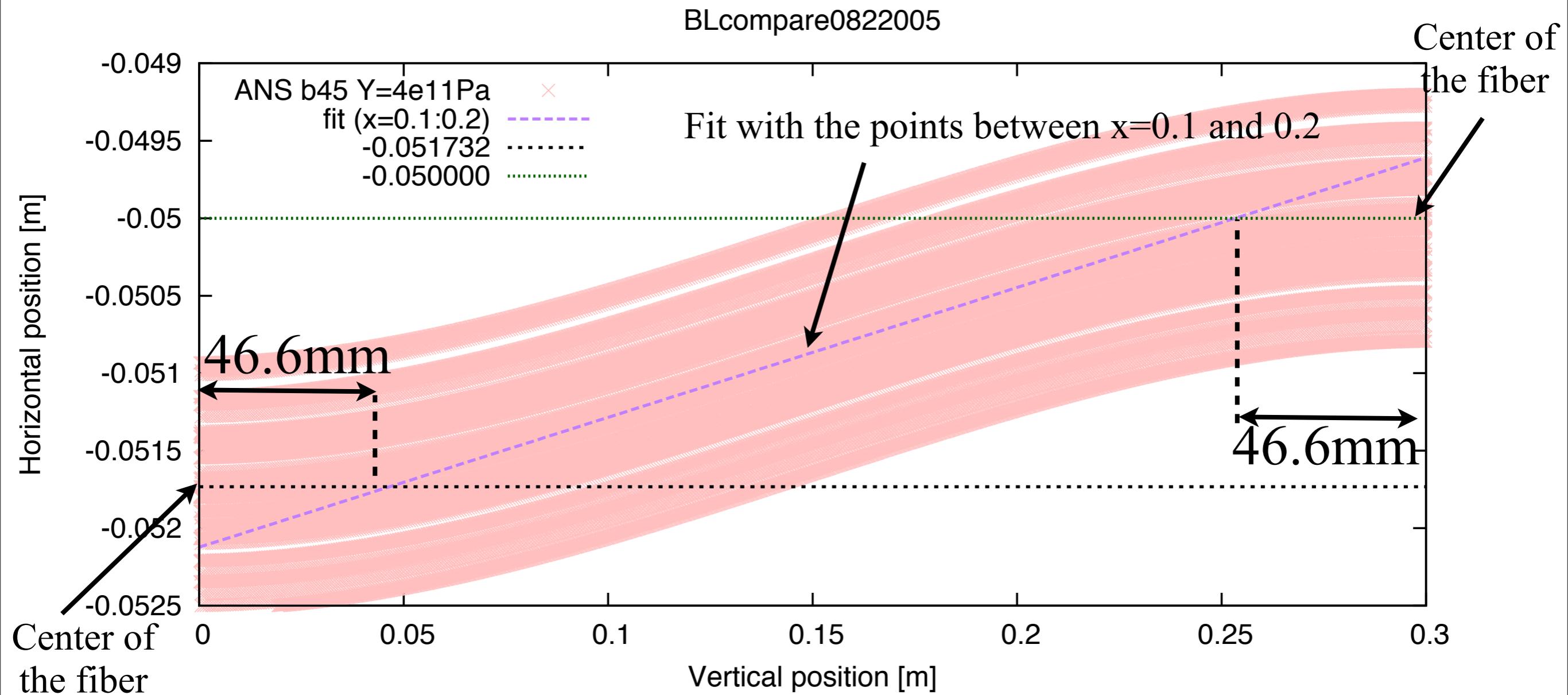
Bending length calc by ANSYS

Result ($b=45\text{mm}$)



Bending length calc by ANSYS

Result ($b=45\text{mm}$, $Y=400\text{GPa}$)



Bending length: 47mm