

# Backscattering TMS

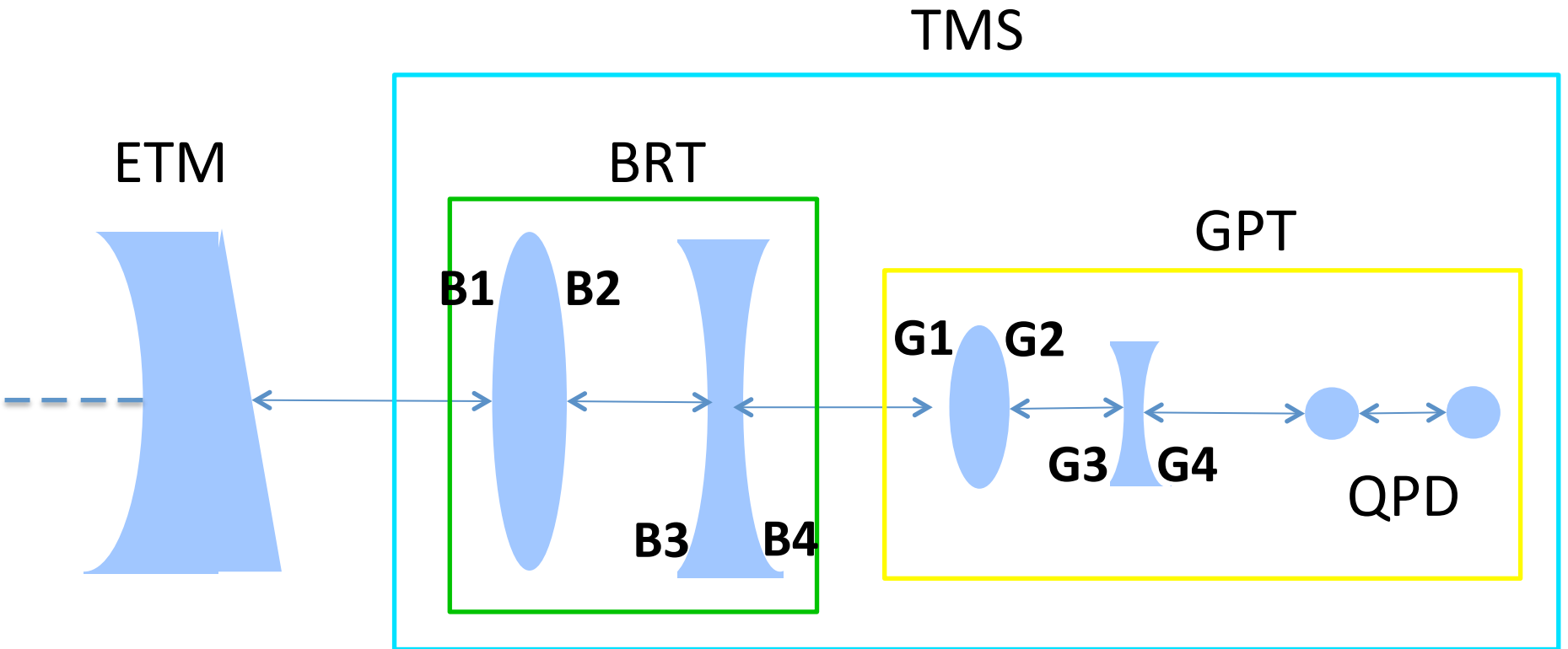
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# What I did

I computed the backscattering noise on the each surface of BRT and GPT lenses.

- Simple estimation
- Including radiation pressure
- up-conversion
- up-conversion using the relative motion between ETM and TMS elements

# Transmission Monitor System



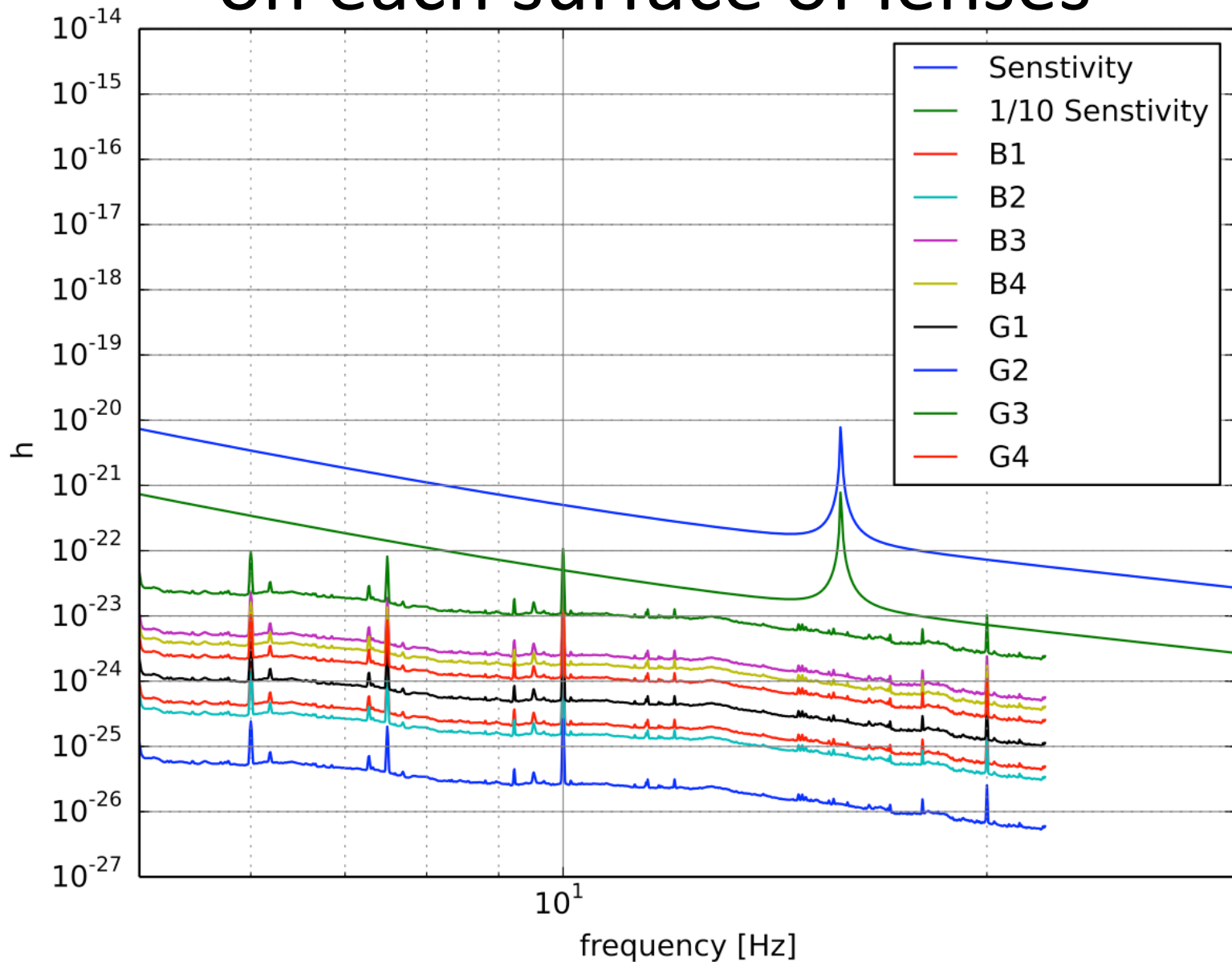
# Simple estimation

$$\underline{\Phi(t) \ll 1}$$

$$h = \text{sqrt}(f_{sc}) * T/L * \delta x$$

$$f_{sc} = |\text{overlap integral}|^2 * R_{AR}$$

# Simple estimation on each surface of lenses



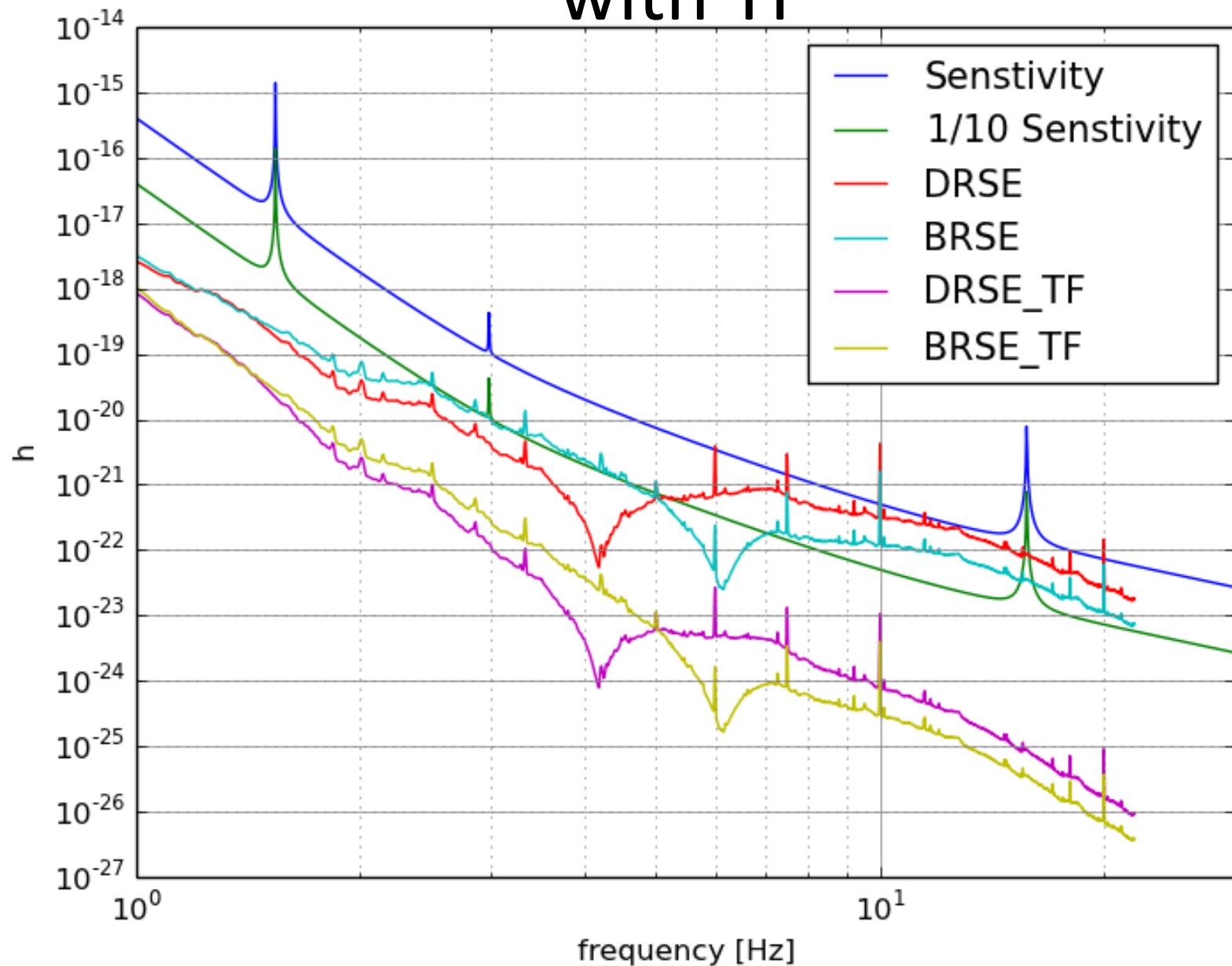
# Including radiation pressure

- $h = G \cdot \sqrt{f_{sc} \cdot T \cdot P_{cav} / P_{in}} / L \cdot 4\pi / \lambda \cdot \delta x$   
(G is given by Aso-san)

- Transfer Function (Simple pendulum)

$$TF = 1 / (1 - \omega^2 / \omega_0^2 + i\omega / \omega_0 \cdot 1/Q)$$

# Including radiation pressure with TF



# up-conversion

$$E_{sc} * e^{i\Omega t} [\cos(\phi(t)) + \underline{i \sin(\phi(t))}]$$

$$\underline{\phi(t) \ll 1}$$

$$h = G * \sqrt{f_{sc} * T * P_{cav} / P_{in}} / L * \frac{4\pi / \lambda * \delta x}{P_{\phi}(\omega)}$$

$$\underline{\phi(t) \gg 1}$$

**Up-conversion ;  $\phi(t) \rightarrow \sin(\phi(t))$**

$$P_{\phi}(\omega) \rightarrow P_{\sin\phi}(\omega) \equiv P_a(\omega)$$



# autocorrelation function

$$C_{\Phi}(\tau) = \int_{-\infty}^{\infty} \frac{P_{\Phi}(\omega) e^{i\omega\tau} d\omega}{\text{既知}}$$

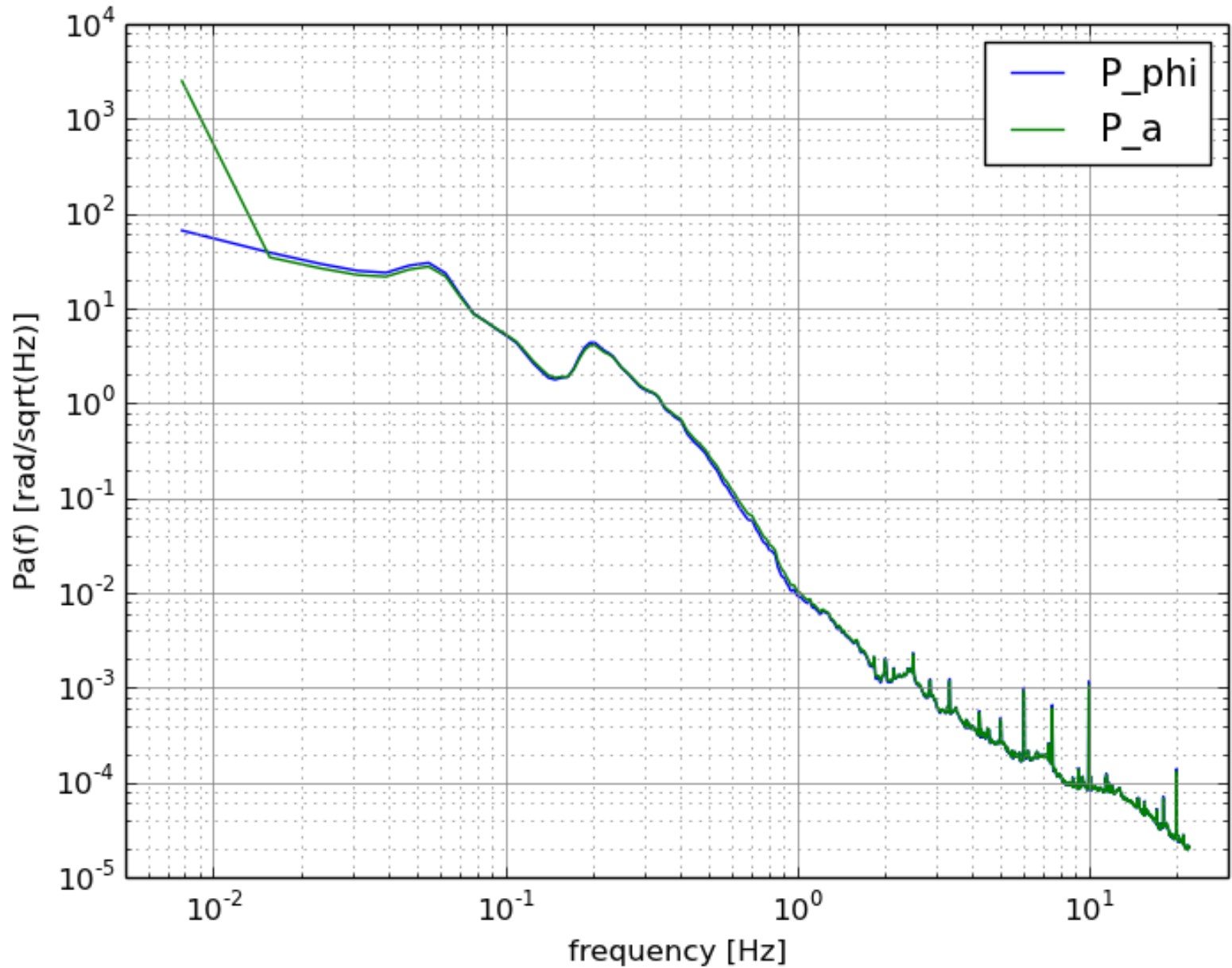
already know

$$C_a(\tau) = \frac{1}{2} \exp\{C_{\Phi}(\tau) - C_{\Phi}(0)\}$$

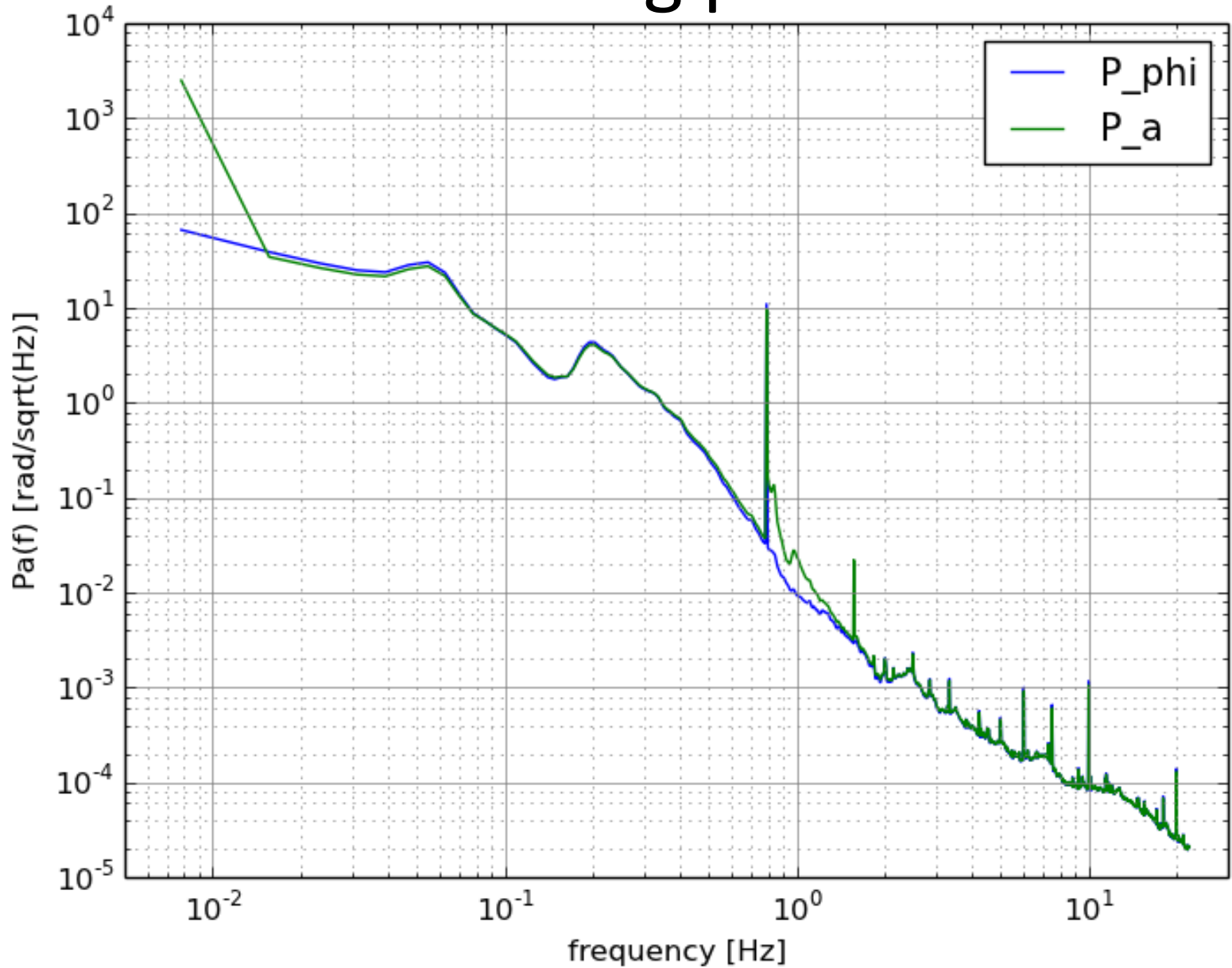
$$\frac{P_a(\omega)}{\text{求めたい}} = \frac{1}{2\pi} \int_{-\infty}^{\infty} C_a(\tau) e^{-i\omega\tau} d\tau$$

want to know

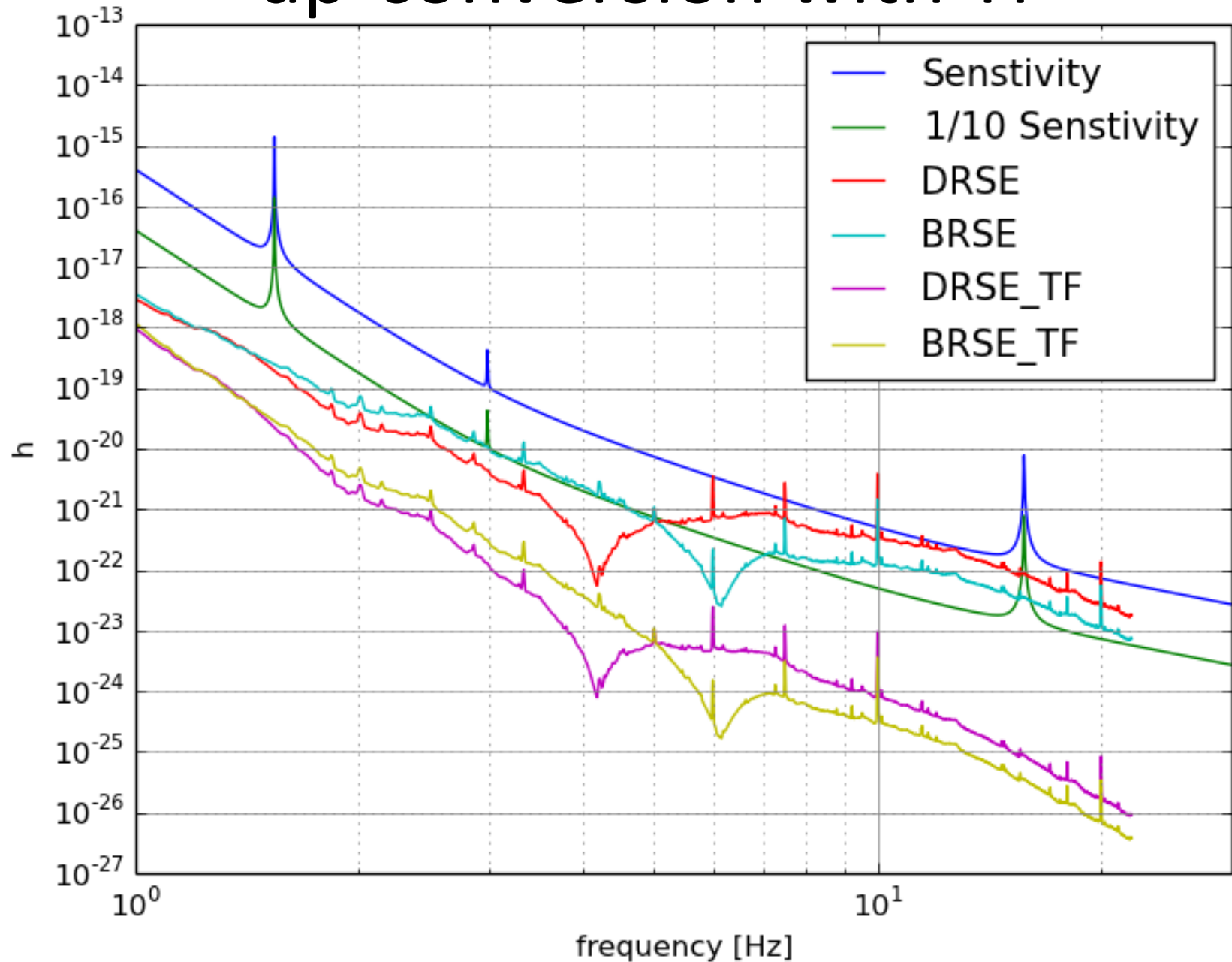
# $P_\phi(\omega)$ & $P_a(\omega)$



# $P_\phi(\omega)$ & $P_a(\omega)$ adding peek



# up-conversion with TF

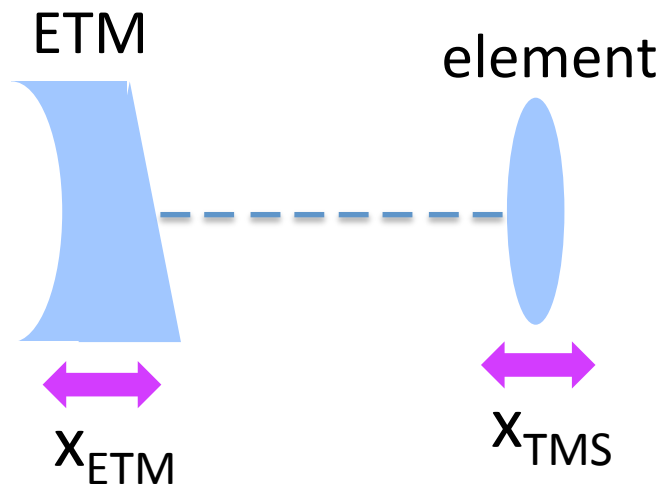


# using relative motion between ETM and TMS

at low frequency :

ETM moves larger, as much as the seismic motion

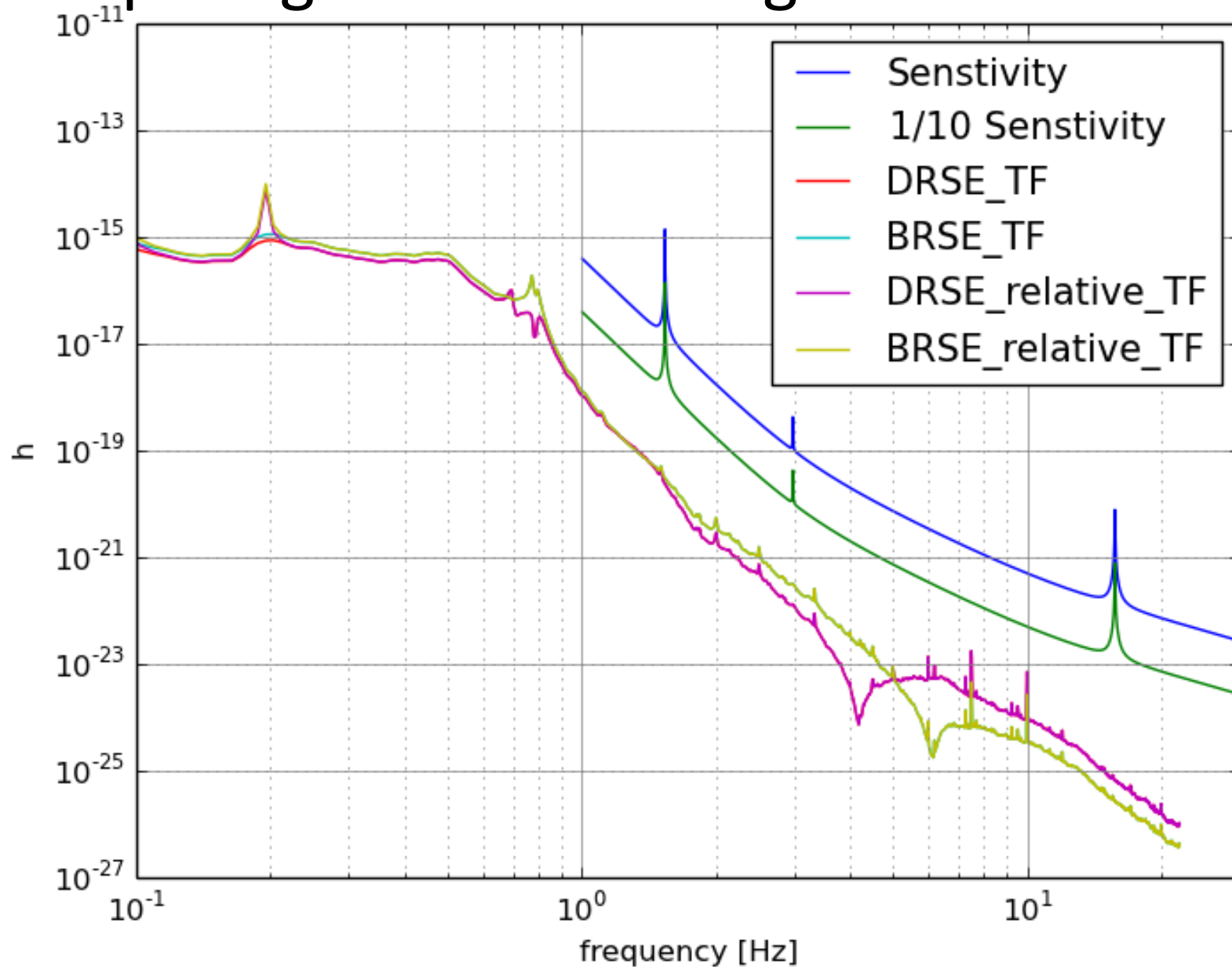
→ We should consider the relative motion between ETM and TMS elements.



$$x_{\text{relative}} = (x_{\text{ETM}}^2 + x_{\text{TMS}}^2)^{1/2}$$

# up-conversion with TF

## comparing normal & using relative motion

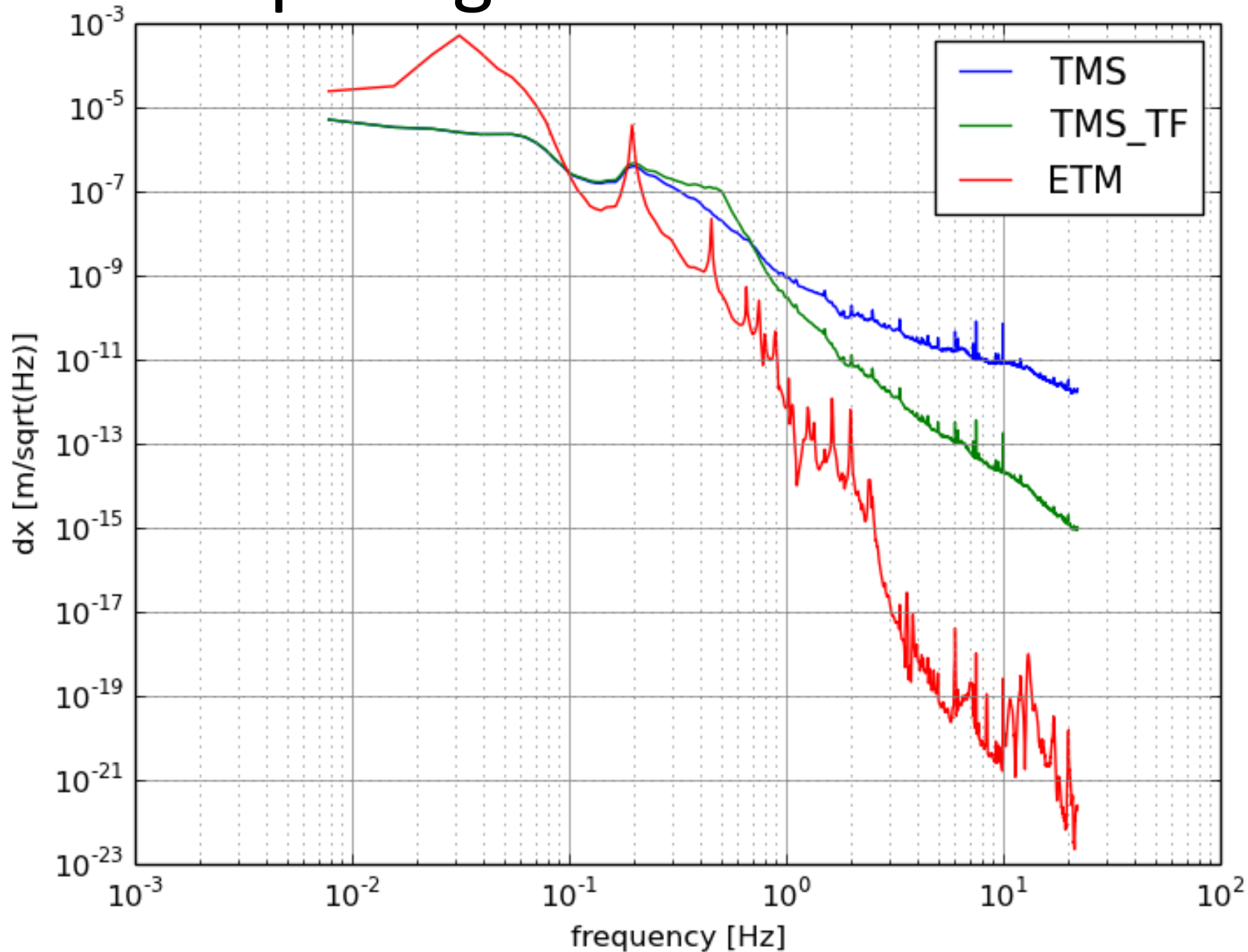


# up-conversion with TF comparing normal & using relative motion

From last slide, we can say that the consideration of relative motion makes almost no difference in the noise estimation.

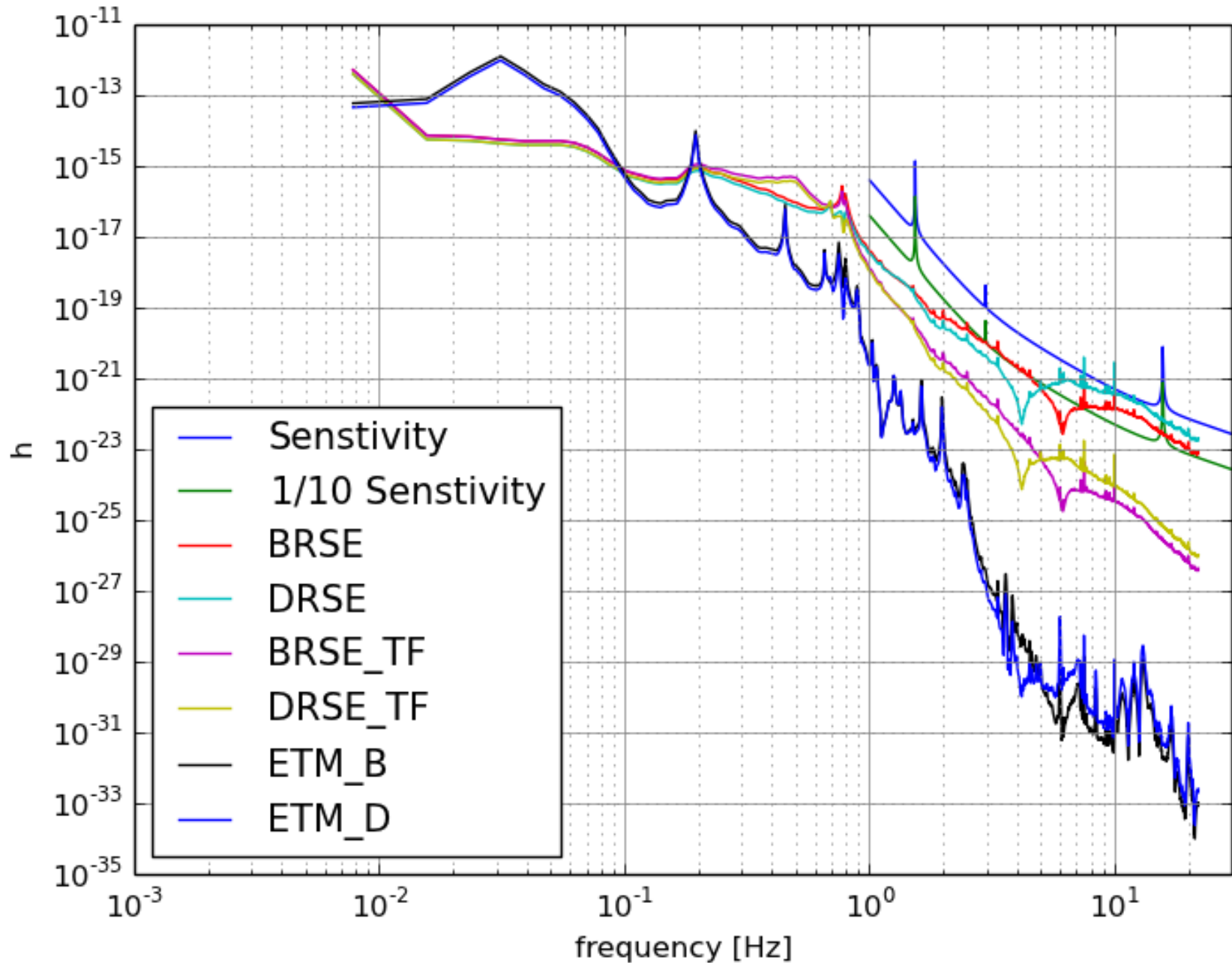
..we can find this reason in the next two slides.  
ETM motion and its contribution to  $h$  are enough smaller than TMS motion at  $> 1$  Hz.

# comparing ETM & TMS motion





# ETM contribution to h



# Conclusion

- TMS should be suspended

Simple pendulum is enough for TMS

- ETM motion is quite smaller than TMS motion  
→ no need to consider the relative motion