

# Alignment Sensing and Control for KAGRA

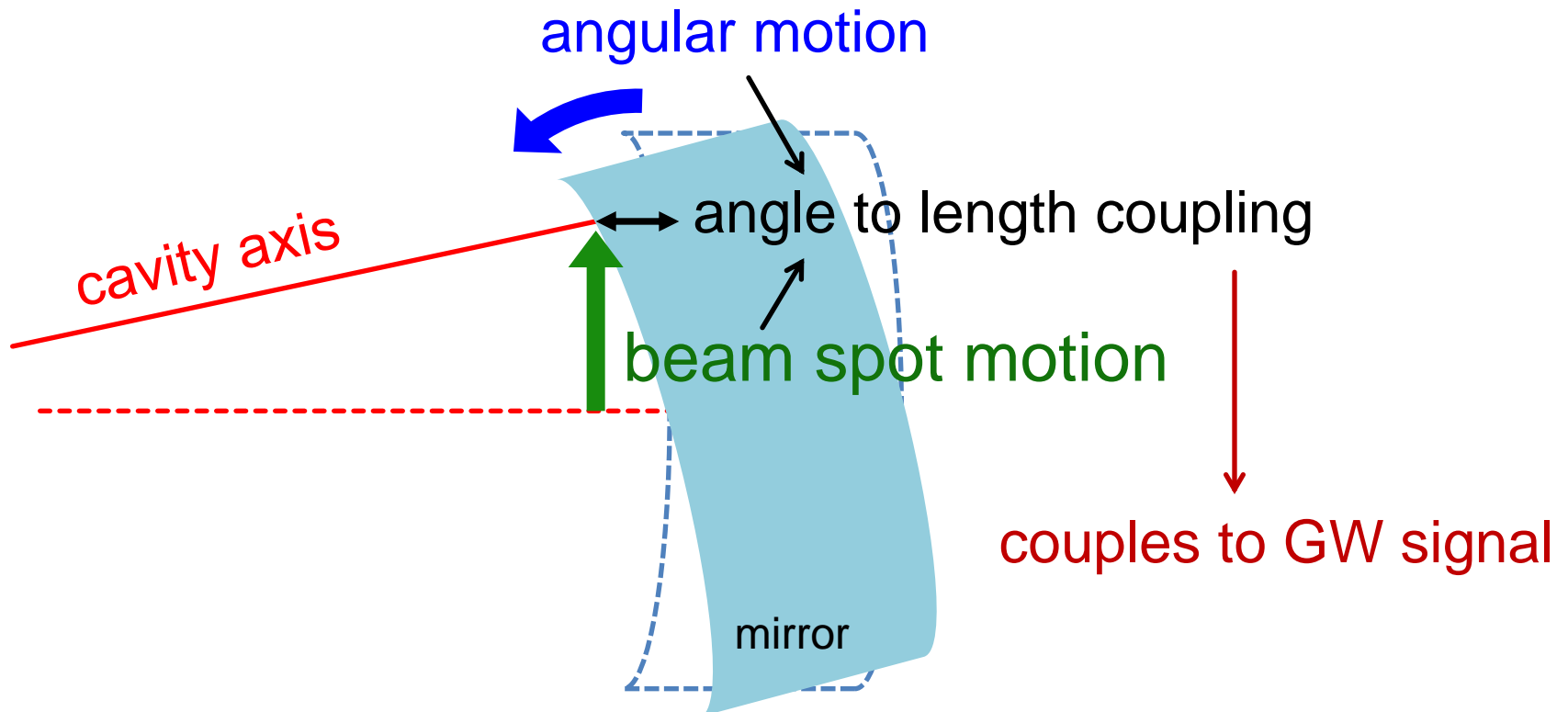
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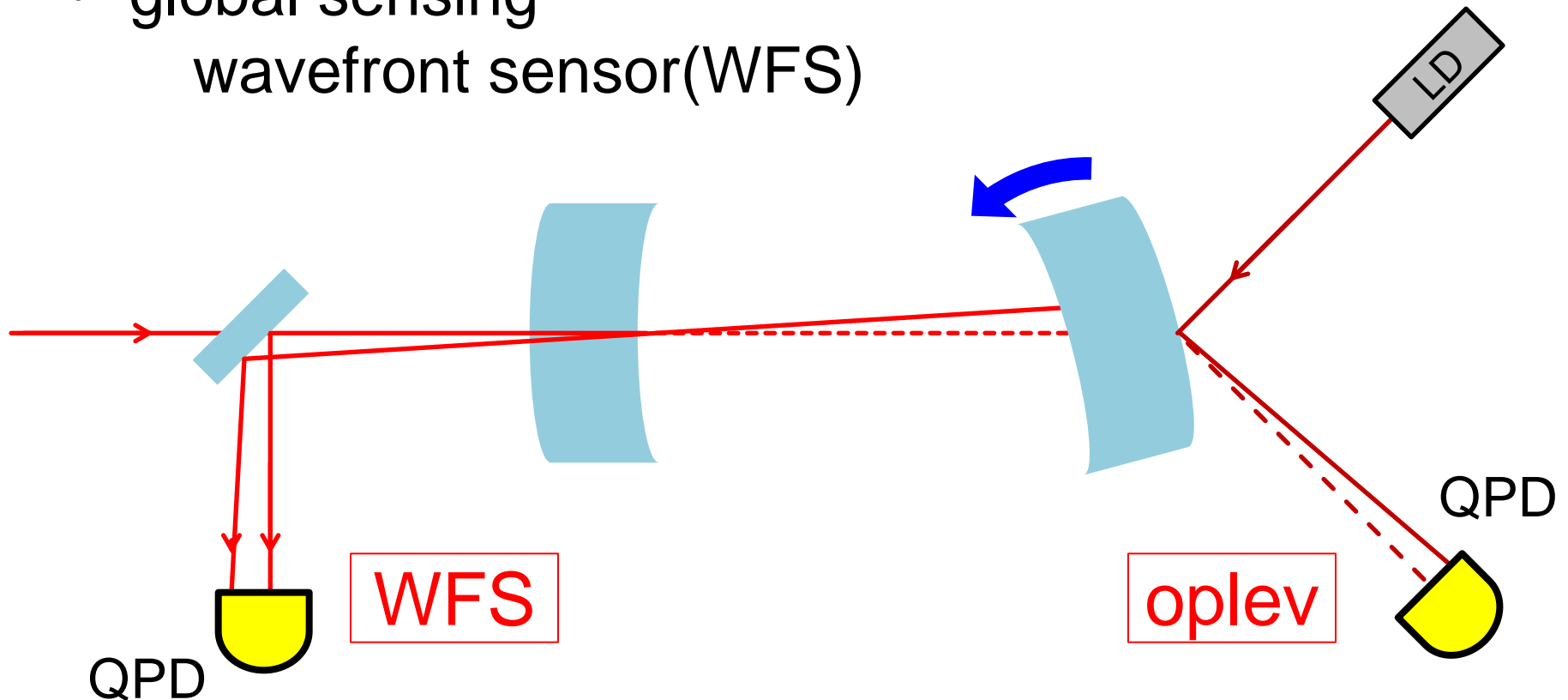
# What is ASC?

- Alignment Sensing and Control
- angular motion is a noise source to IFO  
→ must be controlled



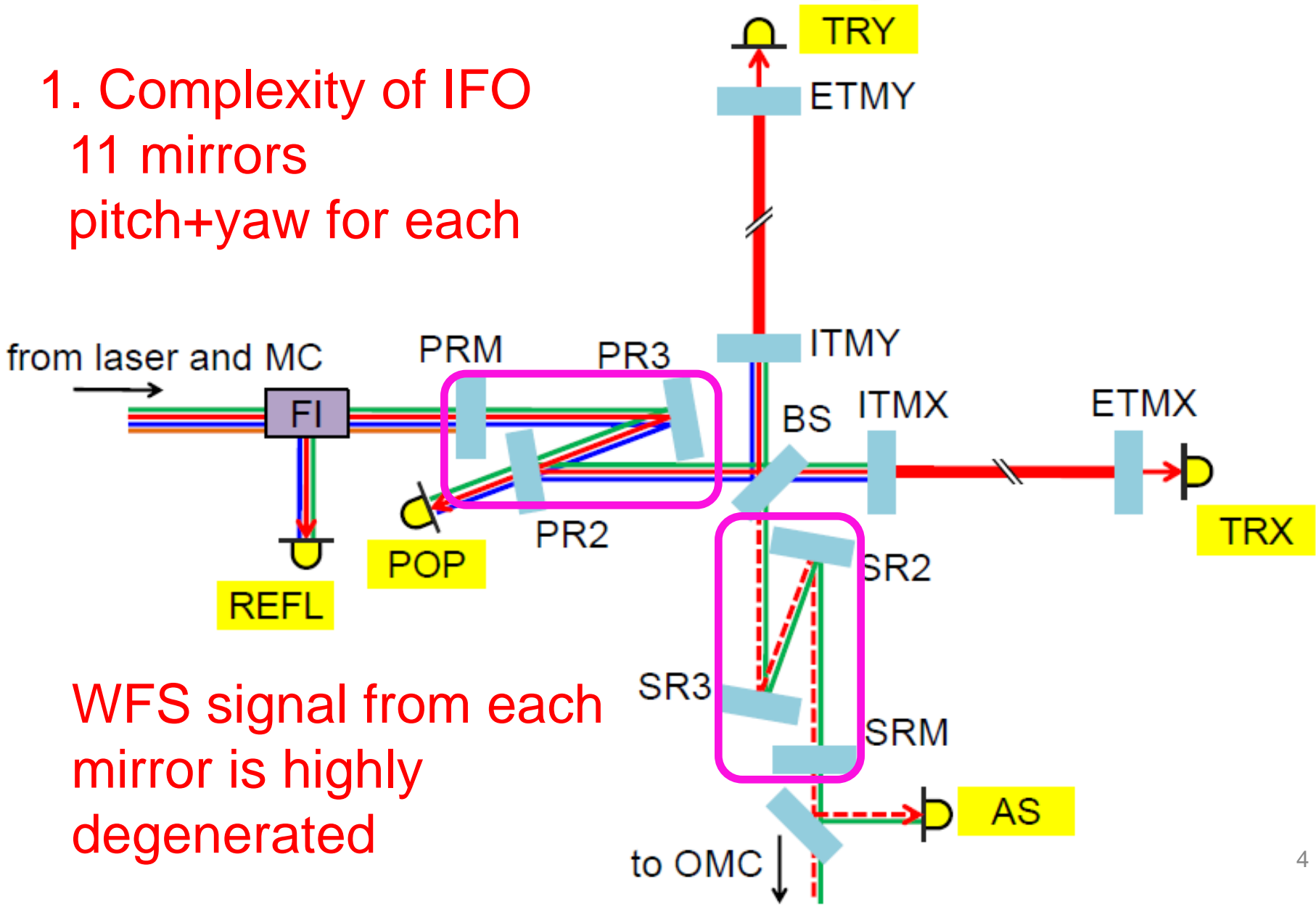
# Alignment Sensing

- local sensing  
optical levers, OSEMs, .....
- global sensing  
wavefront sensor(WFS)



# ASC is tough

- 1. Complexity of IFO
  - 11 mirrors
  - pitch+yaw for each

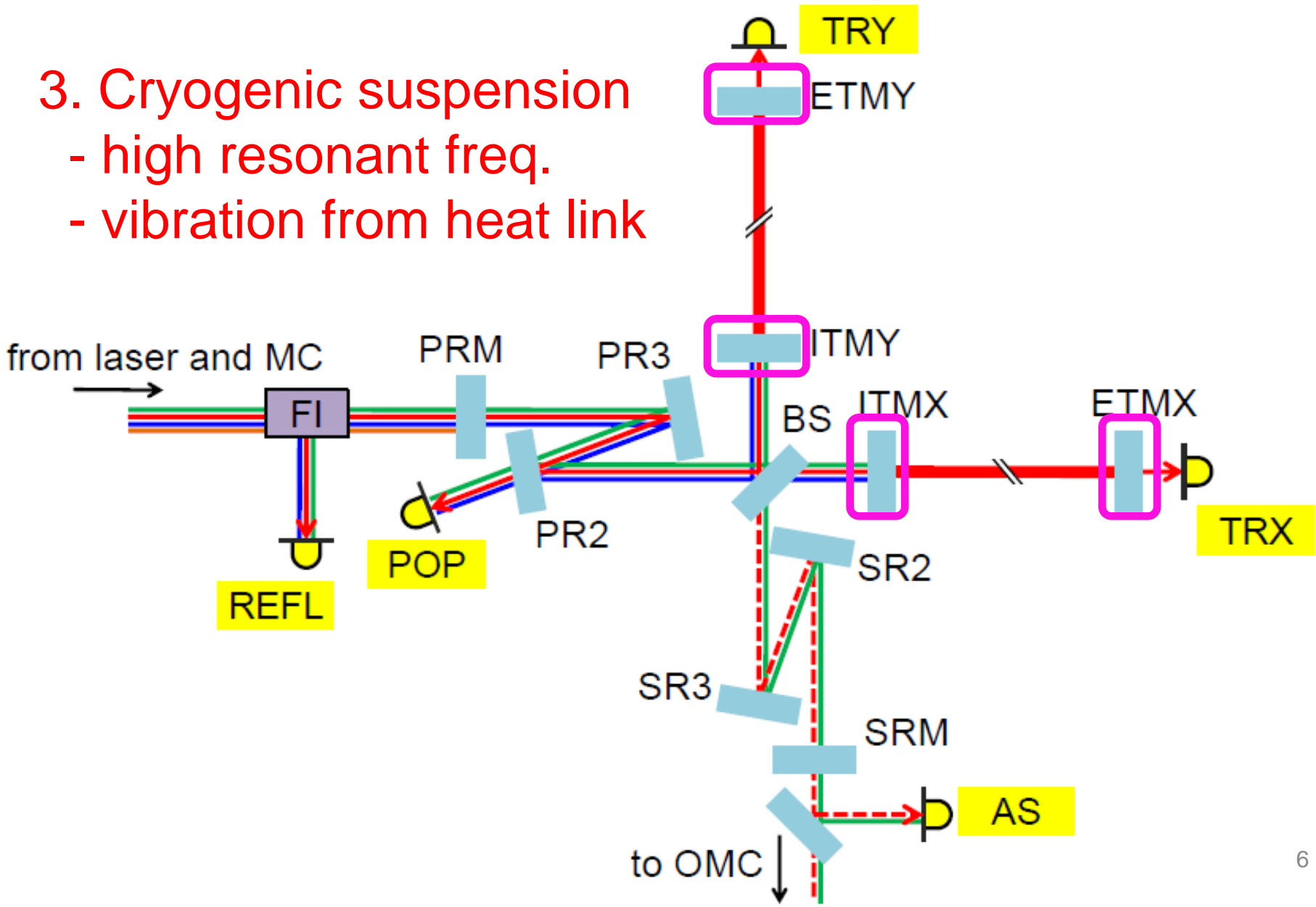


WFS signal from each mirror is highly degenerated



# ASC is tough

- 3. Cryogenic suspension
  - high resonant freq.
  - vibration from heat link



# What we have done

- developed 3D rigid body model for modeling suspension (by T. Sekiguchi)
- developed a tool for simulating/designing WFS servo loop
- finalized IFO design based on many considerations including ASC

# WFS servo modeling

- optical response of IFO is simulated using *Optickle*
- loop noise calculation similar to *pickle* (aLIGO ASC tool)
- uses suspension TF, angular seismic noise as input
- matrix based, frequency domain  
( $11 \times 11 \times \text{freq}$  matrix)



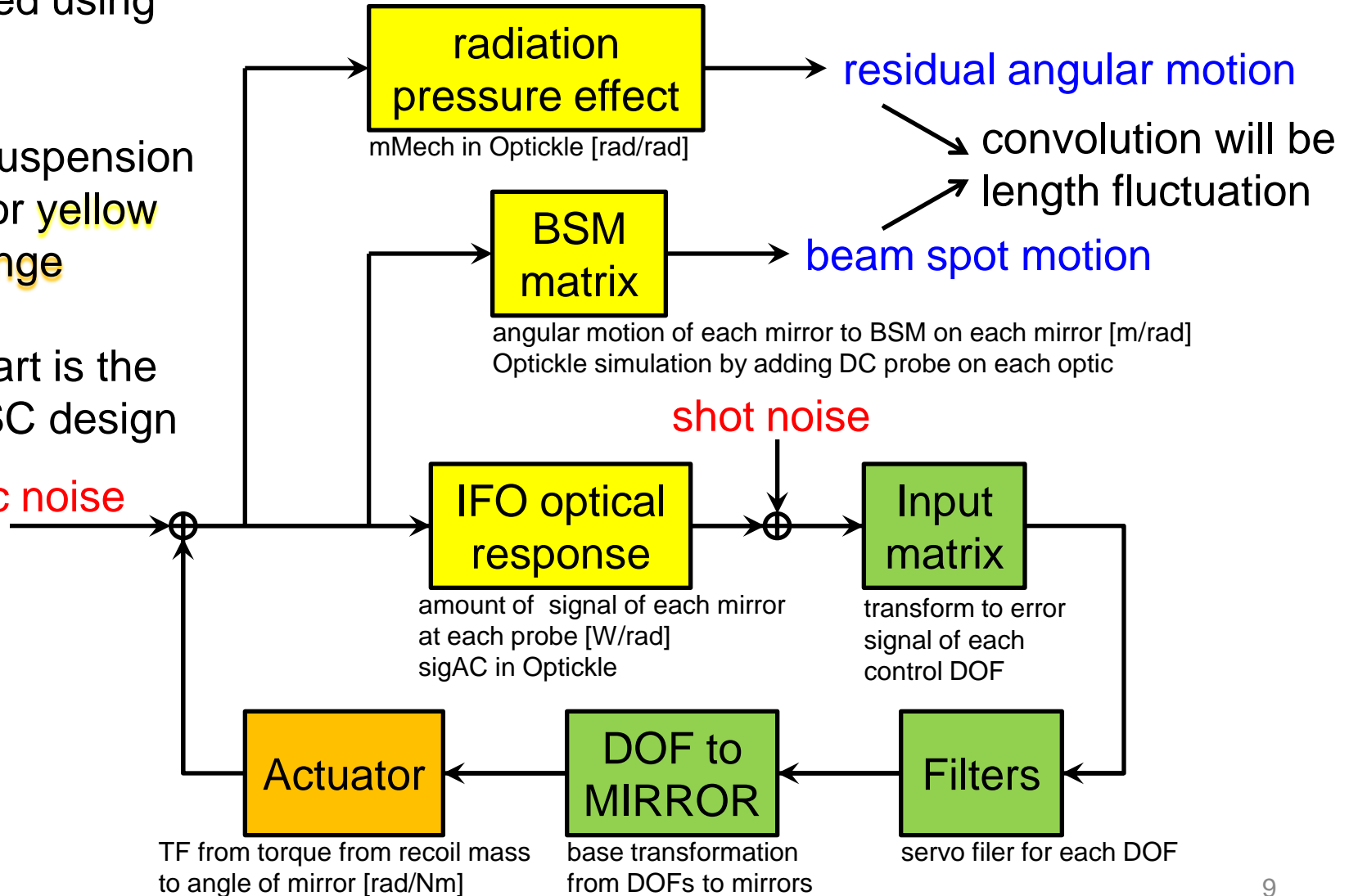
# Structure of WFS servo model

yellow matrices are calculated using Optickle

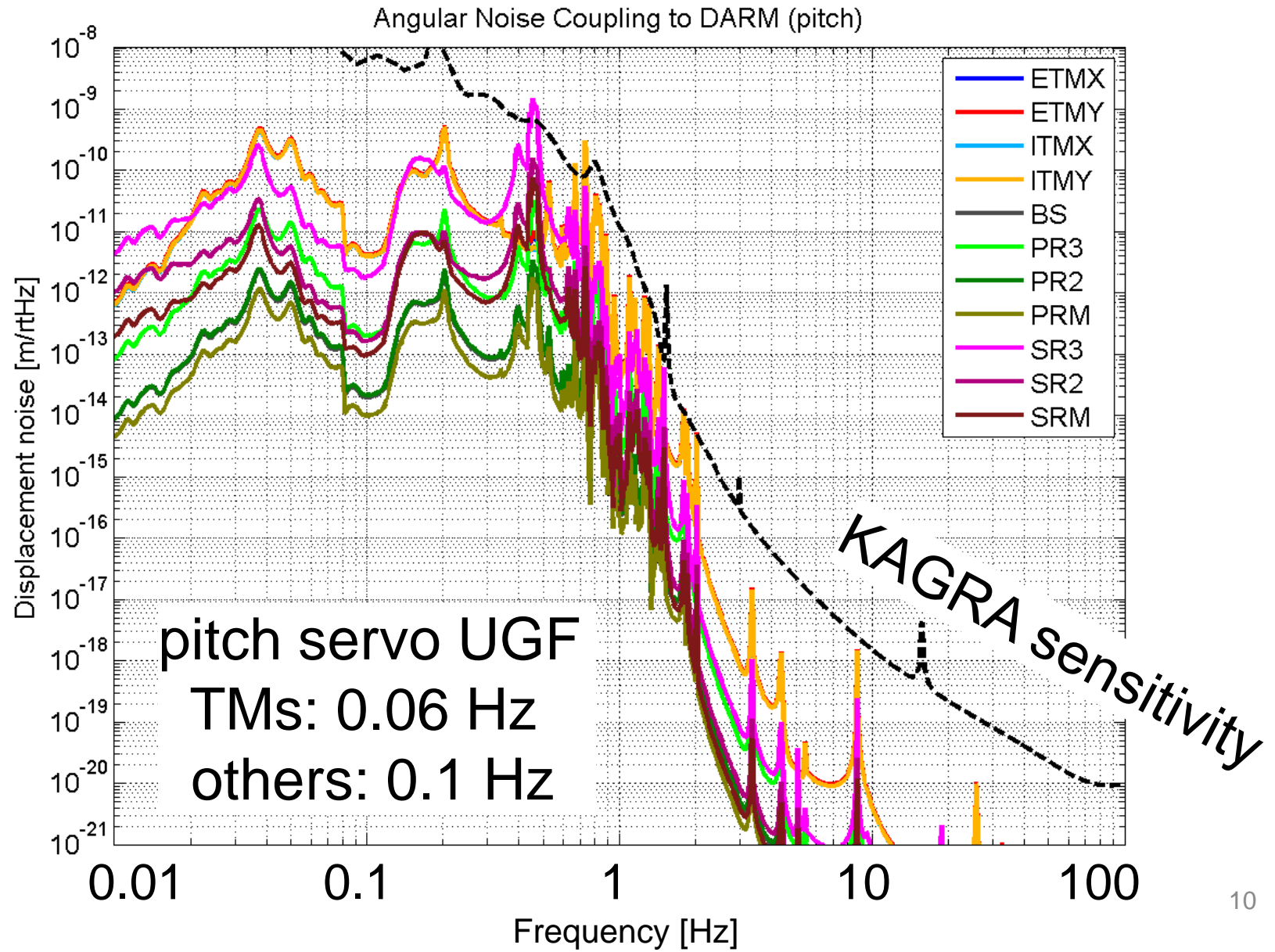
needs suspension model for yellow and orange

green part is the main ASC design

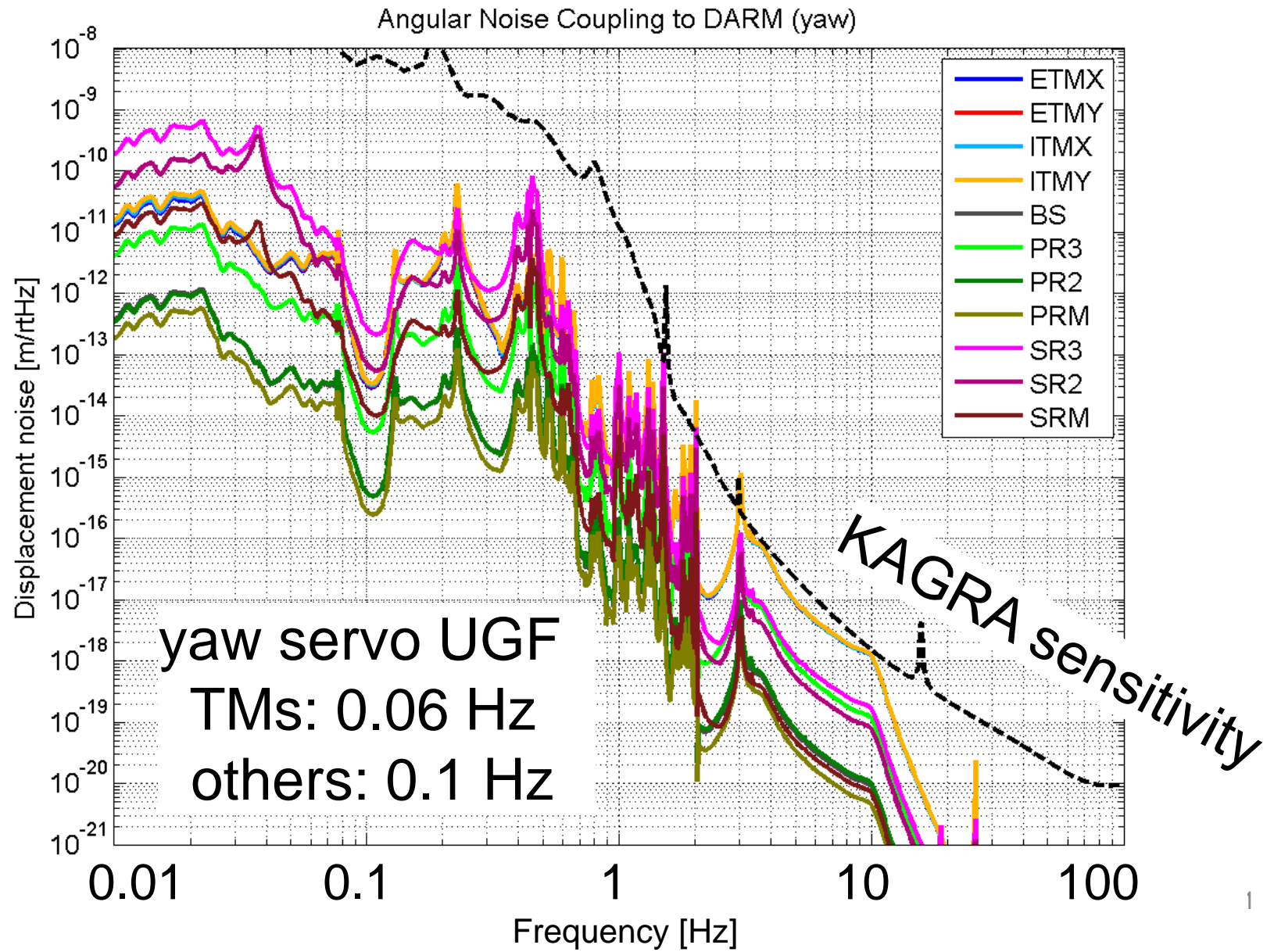
seismic noise



# Angular noise coupling



# Angular noise coupling

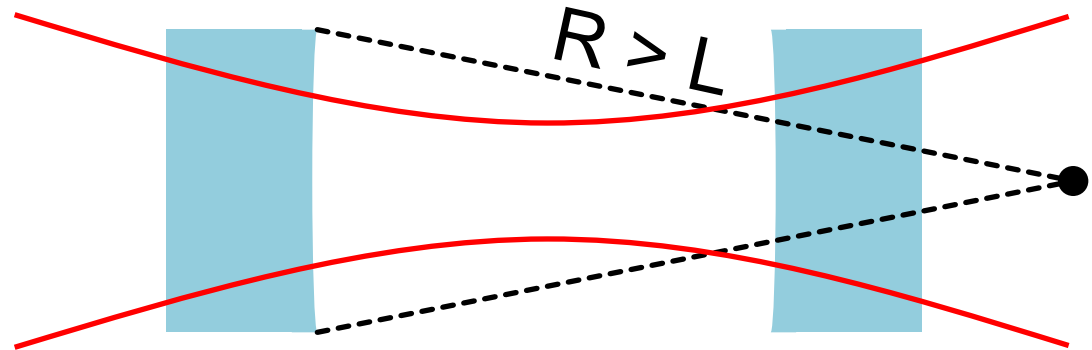




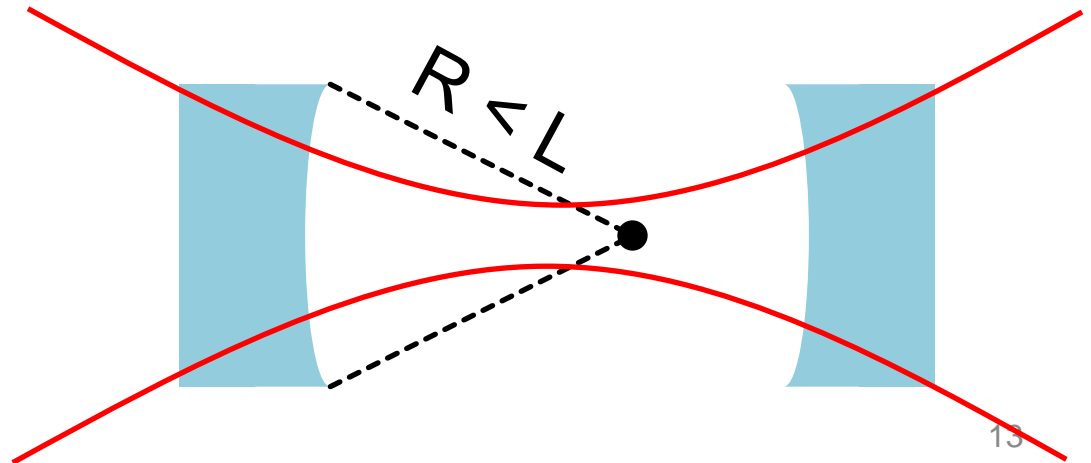
# Arm cavity g-factor

- g-factor  $\leftarrow$  beam spot size  $\leftarrow$  mirror thermal noise
- two solutions for the same spot size

positive g-factor



negative g-factor

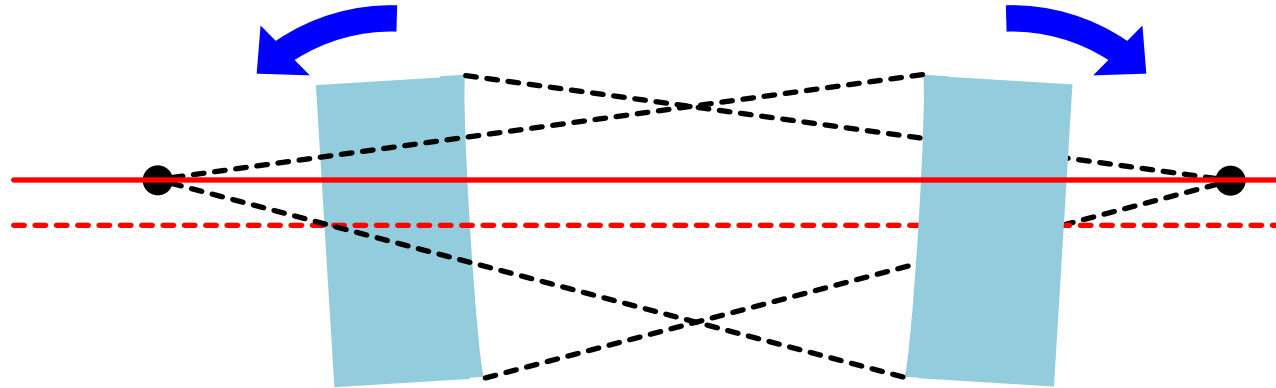


# Sidles-Sigg instability

- angular instability due to radiation pressure anti-spring

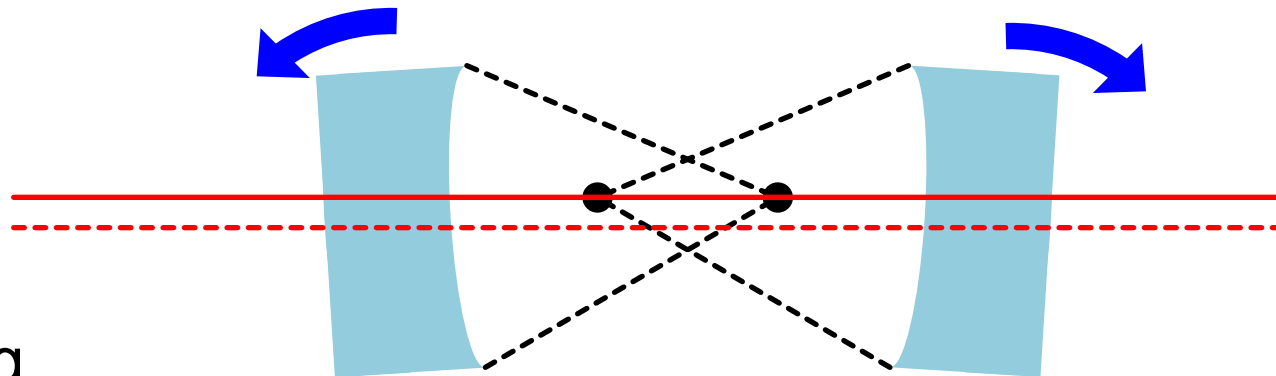
positive g-factor

- larger beam displacement
- larger anti-spring



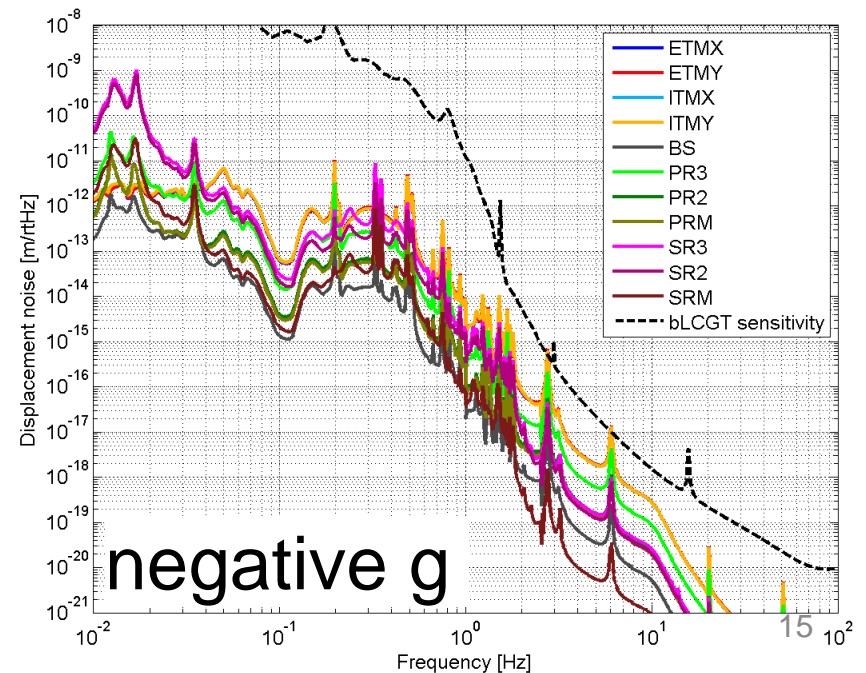
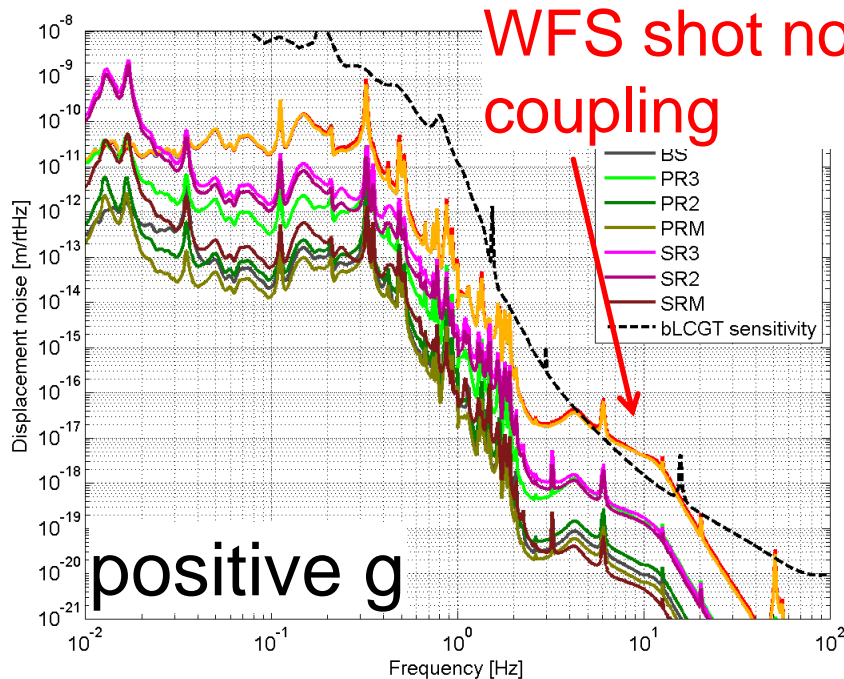
negative g-factor

- smaller beam displacement
- smaller anti-spring



# Positive or negative

- positive g-factor gives larger anti-spring
  - needs to be controlled with high UGF
  - strong coupling of WFS shot noise
  - worse IFO sensitivity
- decided to use negative g-factor



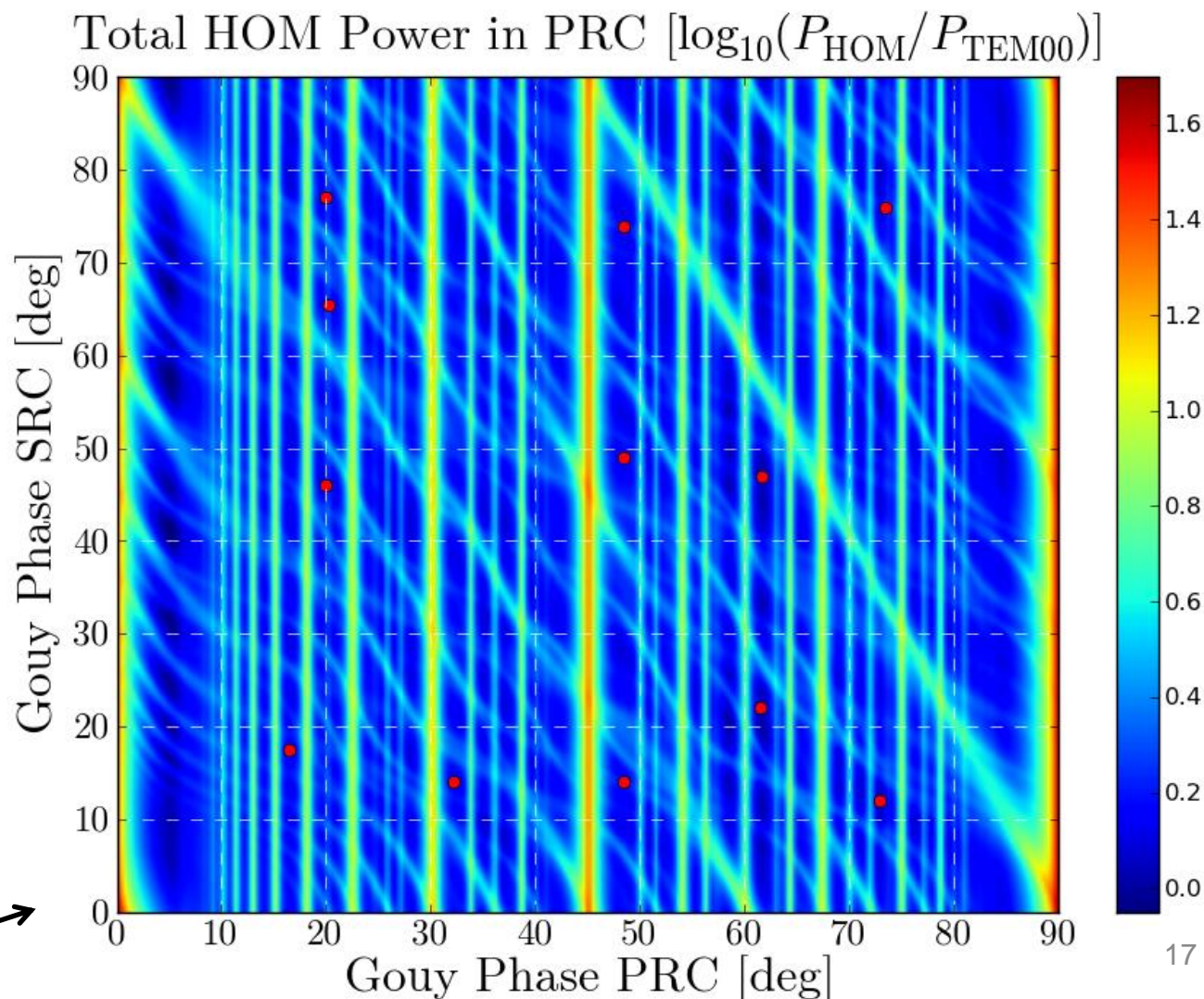
# Recycling cavity Gouy phase

- RC Gouy phase suppresses HOMs in RC
- too much suppression of TEM<sub>10/01</sub> suppresses WFS signal (especially of RC mirrors)
- design procedure we took
  1. Pick PRC/SRC Gouy phase pairs based on HOM suppression
  2. Calculate level of WFS signal degeneracy for each candidates
- how can we estimate “level of degeneracy” ?



# HOM power and RC Gouy phase

- red dots are the candidates



by Y. Aso



# WFS sensing matrix

WFS Sensing Matrix [W/mrad/sqrt(2/pi)]

(Gouy phases at POP A:-13.0, POP B:-76.3 REFL A:88.7, REFL B:-85.6, AS A:6.8, AS B:-84.1, TR A:-64.1 deg)

	CS	CH	DS	DH	BS	PR3	PR2	PRM	SR3	SR2	SRM
TRX_ADC	-12.37	-0.03	-12.38	-0.07	0.00	-0.01	-0.00	-0.00	-0.00	-0.00	-0.00
REFL_A2I	-37.31	-136.45	0.04	0.20	5.93	17.57	2.46	2.92	-0.00	-0.00	-0.00
TRY_ADC	-12.37	-0.03	12.38	0.07	-0.01	-0.01	-0.00	-0.00	0.00	0.00	0.00
AS_A1Q	0.00	0.01	8.70	43.63	0.08	-0.01	-0.00	-0.00	-0.00	-0.00	-0.00
POP_A1Q	0.03	-0.00	0.48	-0.44	0.31	-0.03	-0.00	-0.00	-0.01	-0.00	-0.00
POP_A2Q	-2.44	0.65	0.00	0.00	1.44	4.15	0.51	0.25	-0.00	-0.00	-0.00
POP_BDC	0.22	-0.03	-0.00	-0.01	-0.15	-0.38	-2.62	-1.28	0.02	0.00	0.00
REFL_BDC	-1.01	-5.47	0.02	-0.02	-0.07	-0.11	-0.00	2.97	0.03	0.00	0.00
POP_B1I	2.64	-0.38	0.00	0.00	-0.58	-3.04	-0.37	-0.18	-1.36	-0.16	-0.08
AS_BDC	-0.01	0.01	0.00	-0.00	-0.01	0.00	-0.00	-0.00	0.02	0.00	-0.04

# Sensing matrix diagonalization

- we use input matrix to extract error signal for each mirror from sensing matrix

$$\begin{array}{ccc} \begin{array}{c} \text{error signal for each mirror} \\ \left( \begin{array}{c} \text{signal at} \\ \text{each port} \\ \mathbf{S}^{-1} \end{array} \right) \\ \uparrow \\ \text{input matrix} \\ [\text{rad/W}] \end{array} & \times & \begin{array}{c} \text{each mirror} \\ \text{motion} \\ \left( \begin{array}{c} \text{signal at} \\ \text{each port} \\ \mathbf{S} \end{array} \right) \\ \uparrow \\ \text{sensing matrix} \\ [\text{W/rad}] \end{array} = \begin{array}{c} \text{error signal for each mirror} \\ \left( \begin{array}{c} \text{each mirror} \\ \text{motion} \\ \mathbf{I} \end{array} \right) \\ \uparrow \\ \text{ideally,} \\ \text{identity matrix} \end{array} \end{array}$$

# Estimation for degeneracy level

- in reality, WFS shot noise contaminates

$$\begin{array}{c}
 \text{error signal for each mirror} \\
 \text{signal at each port} \\
 \left( \mathbf{S}^{-1} \right) \\
 \uparrow \\
 \text{input matrix} \\
 [\text{rad/W}]
 \end{array}
 \times
 \begin{array}{c}
 \text{each mirror} \\
 \text{motion} \\
 \text{WFS} \\
 \text{shot noise} \\
 \text{signal at each port} \\
 \left( \begin{array}{c|c}
 \mathbf{S} & \mathbf{N} \\
 \hline
 & 
 \end{array} \right) \\
 \uparrow \\
 \text{sensing matrix} \\
 [\text{W/rad}] \\
 \text{shot noise matrix} \\
 [\text{W/rtHz}]
 \end{array}
 =
 \begin{array}{c}
 \text{error signal for each mirror} \\
 \text{each mirror} \\
 \text{motion} \\
 \text{WFS} \\
 \text{shot noise} \\
 \left( \begin{array}{c|c}
 \mathbf{I} & \mathbf{S}^{-1}\mathbf{N} \\
 \hline
 & 
 \end{array} \right) \\
 \uparrow \\
 \text{ideally,} \\
 \text{identity matrix} \\
 \text{equivalent shot noise} \\
 [\text{rad/rtHz}]
 \end{array}$$

# Equivalent shot noise

- PRC 16.5 deg, SRC 17.5 deg was the best
- basically larger Gouy phase gives worse SNR

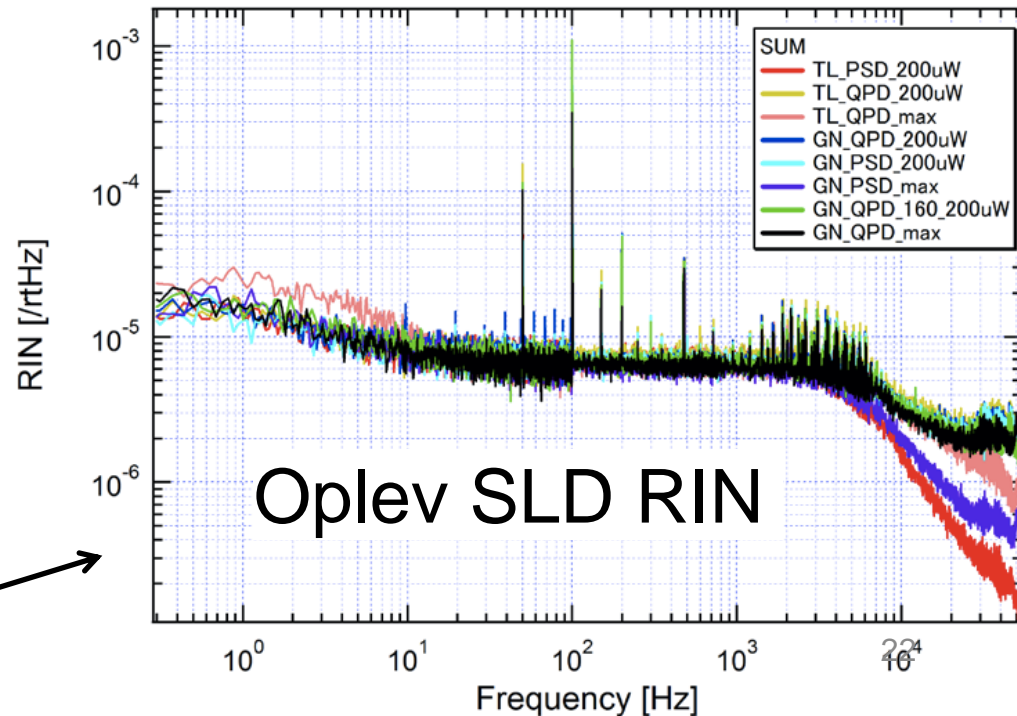
	P195_S195	P615_S220	P200_S770	P735_S760	P165_S175	P350_S250
CS:	7.75	7.75	7.76	7.76	7.75	7.76
CH:	4.27	6.48	21.35	9.55	4.61	5.85
DS:	7.76	7.76	7.75	7.76	7.76	7.76
DH:	1.92	2.3	2.47	2.46	1.87	2.04
BS:	457.18	743.18	160.78	125.74	431.02	511.87
PR3:	162.78	320.06	194.93	326.1	153.1	199.67
PR2:	62.55	347.09	128.62	1114.51	55.78	104.97
PRM:	29.75	106.14	159.81	292.25	27.53	48.83
SR3:	214.27	496.29	515.94	412.98	196.14	312.74
SR2:	0	0	0	0	0	0
SRM:	627.87	719.27	1142.56	2142.45	579.1	712.03

SR2 is not controlled by WFS  
because of too much degeneracy

(all in  $10^{-15}$  rad/rtHz)

# Optical levers?

- for some mirrors, WFS equivalent shot noise is  $\sim 10^{-13}$  rad/rtHz
- but optical levers are worse
  - shot noise:  $\sim 10^{-12}$  rad/rtHz (5 mW)
  - intensity noise:  $\sim 10^{-10}$  rad/rtHz (RIN  $10^{-5}$  /rtHz)
- optical levers can be used only for local damping



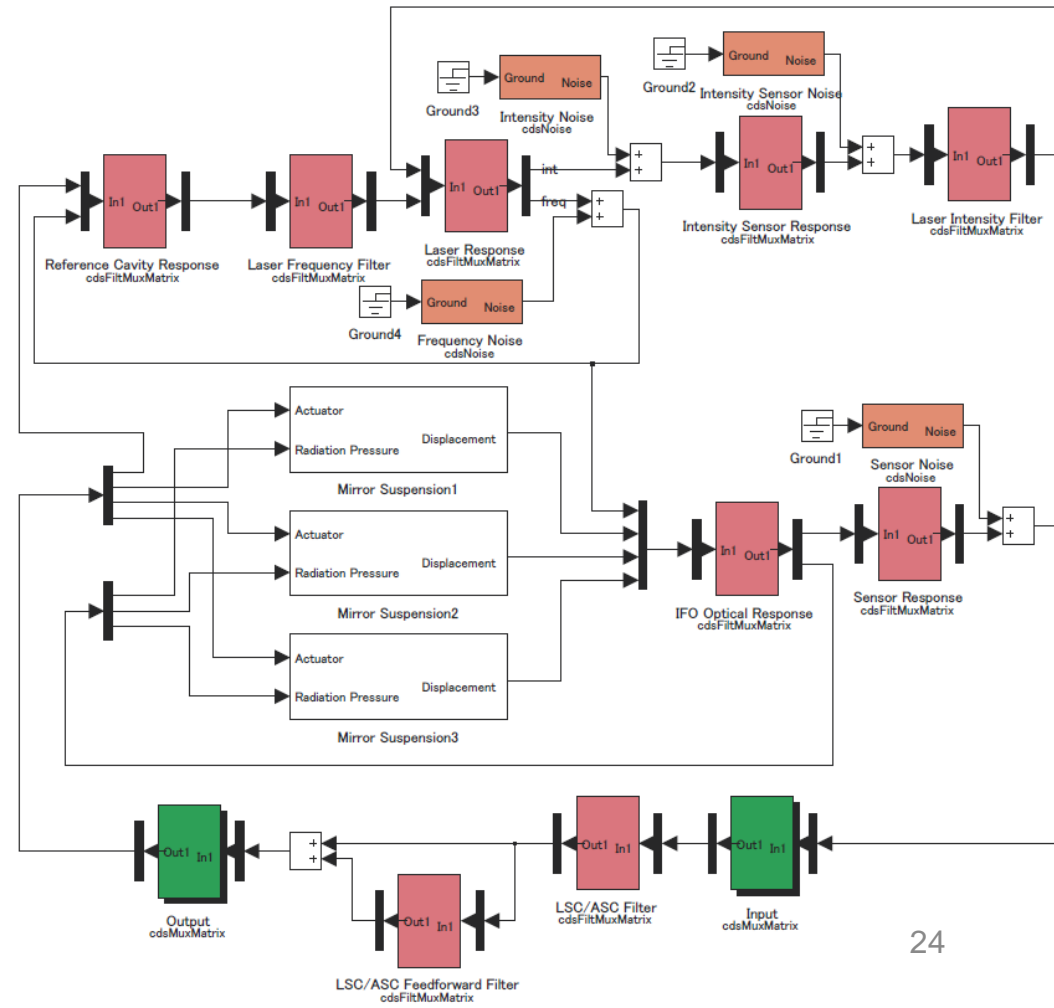
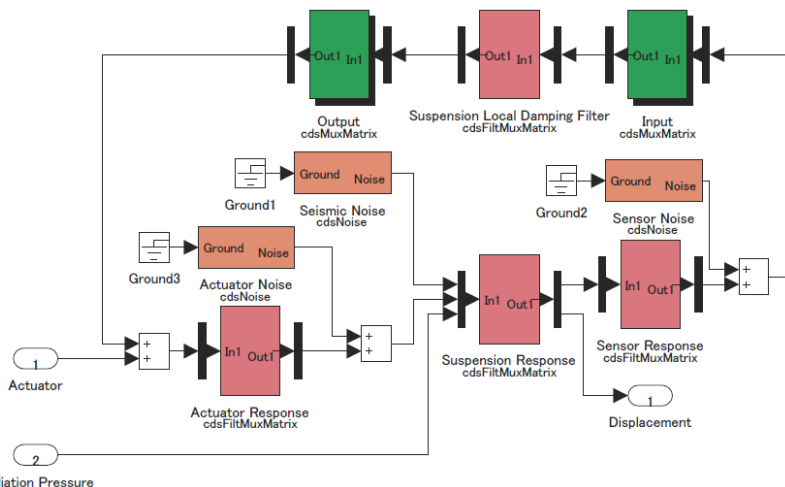
by K. Agatsuma  
JGW-G1201388

# Future plans

- modeling of suspension local damping  
no local damping is included yet
- geometrical study of IFO beam  
for better DOF selection
- include seismic/electrical noise on QPDs etc  
for more realistic modeling
- estimate thermal effect on ASC  
thermal lensing changes Gouy phase
- initial alignment scheme  
lock acquisition mode / science mode

# Overall modeling of ISC

- including all LSC/ASC, suspension local damping, laser intensity/frequency servo .....
- can be used for
  - servo design
  - loop noise calc.
  - noise budgeting
  - PD/circuit range





# Summary

- developed a tool for simulating / designing ASC
- finalized IFO designing
- needs modeling of suspension local damping
- work for ISC modeling has started