

Mirror quality and interferometer performance Hiro Yamamoto - Caltech LIGO

- Introduction
- Gaussian beam and Modal model
- Cavity basic
- PSD, BRDF and loss
- Mirror polishing and coating
- Thermal effects
- Not so nice looking mirrors

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## Introduction idealized vs reality

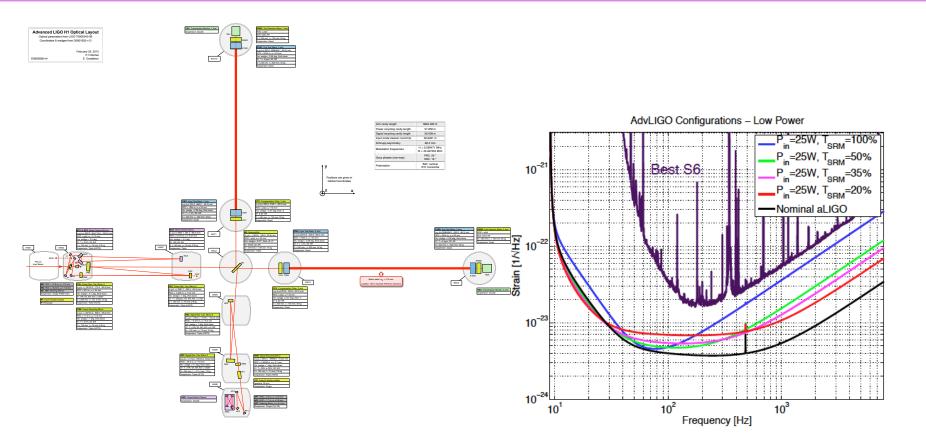


Figure 2: Possible configurations of aLIGO in the early commissioning phase, with 25W of input power. As reference, the nominal aLIGO curves and the best S6 sensitivity are also included.

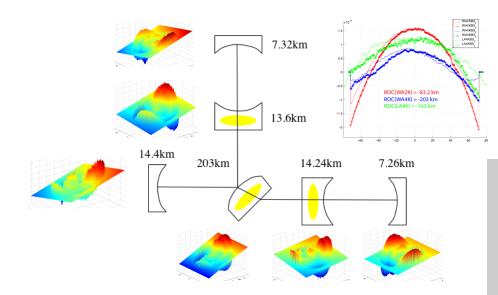
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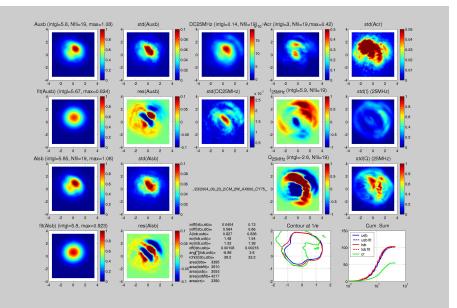
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# Initial LIGO optics and Fields idealized vs reality





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## Gaussian beam and Modal model

• Gaussian beam : stationary state in a two mirror cavity (FP)

$$\begin{array}{l}
\mathbf{R}^{1} \qquad \mathbf{W}^{2} \qquad \mathbf{R}^{2} \qquad G_{00}(x,y,z,t) = G_{00}(x,y,z) \exp[i(\omega \cdot t - k \cdot z)] \\
G_{00}(x,y,z) = \sqrt{\frac{2}{\pi}} \frac{1}{w(z)} \exp(-r^{2}(\frac{1}{w(z)^{2}} + i\frac{k}{2R(z)}) + i \cdot \eta(z)) \\
w(z)^{2} = w_{0}^{2}(1 + \frac{z^{2}}{z_{0}^{2}}), \quad R(z) = z + \frac{z_{0}^{2}}{z}, \quad \eta(z) = a \tan(\frac{z}{z_{0}})
\end{array}$$

$$HG_{mn} = G_{00}(x, y, z, t) \sqrt{\frac{1}{2^{m+n}m!n!}} H_m(\frac{\sqrt{2}x}{w(z)}) H_n(\frac{\sqrt{2}y}{w(z)}) \exp[i(m+n)\eta(z)]$$
$$LG_{pm} = G_{00}(x, y, z, t) \sqrt{\frac{p!}{(p+|m|)!}} \exp(im\varphi) L_p^{|m|}(\frac{2r^2}{w(z)^2}) \exp[i(2p+|m|)\eta(z)]$$

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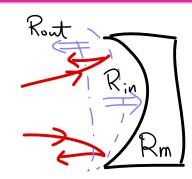
## Gaussian beam and Modal model

• Tilt

 $\sim$ 

$$\begin{split} E_{ref}(\theta) &= G_{00}(\theta = 0) \cdot \exp(i\omega t - i(x \cdot k_x + z \cdot k_z)) \\ &= G_{00} \cdot (1 - i \cdot x \cdot k \cdot \theta) \\ &= G_{00} \cdot (1 - i \cdot \frac{1}{\sqrt{2}} H_1(\frac{\sqrt{2}x}{w(z)}) \cdot \frac{\theta}{\Theta(z)}) \\ &= G_{00} - i \frac{\theta}{\Theta(z)} \cdot G_{10} \\ \Theta(z) &= \frac{1}{\pi} \frac{\lambda}{w(z)}, \ H_1(x) = 2x \end{split}$$

curvature mismatch



$$E_{ref}(\delta R) = G_{00}(R = R_{in}) \cdot Exp[-ikr^{2}(-\frac{2}{2R_{m}})]$$

$$= G_{00}(R = \infty) \cdot Exp[ikr^{2}(\frac{1}{2R_{in}} - (\frac{1}{R_{in}} - \frac{1}{R_{m}}))]$$

$$\approx G_{00}(R = \infty) \cdot Exp[ir^{2}(\frac{1}{2R_{in}})] \cdot (1 - ikr^{2}\frac{\delta R}{R_{in}^{2}})$$

$$= G_{00}(R = -R_{in})(1 - ik\frac{w^{2}}{2}\frac{\delta R}{R_{in}^{2}}(1 - L_{1}^{0}(\frac{2r^{2}}{w^{2}})))$$

$$\approx G_{00}(R = -R_{in}) + i\pi\frac{w^{2}}{\lambda R_{in}}\frac{\delta R}{R_{in}}LG_{1}^{0}(R = -R_{in})$$

 $\delta R = R_m - R_{in}, \ L_1^0(r) = 1 - r$ 

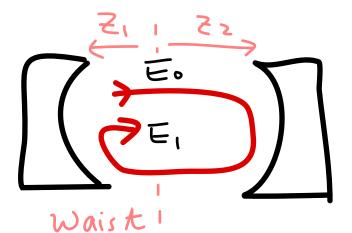
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# Gaussian beam and Modal model

Cavity field and Gouy phase

$$E_1 = E_0 \cdot r_1 r_2 \cdot \exp[i2\phi]$$
$$\phi = \begin{cases} m+n+1\\ 2p+|m|+1 \end{cases} \Delta \eta - kL$$

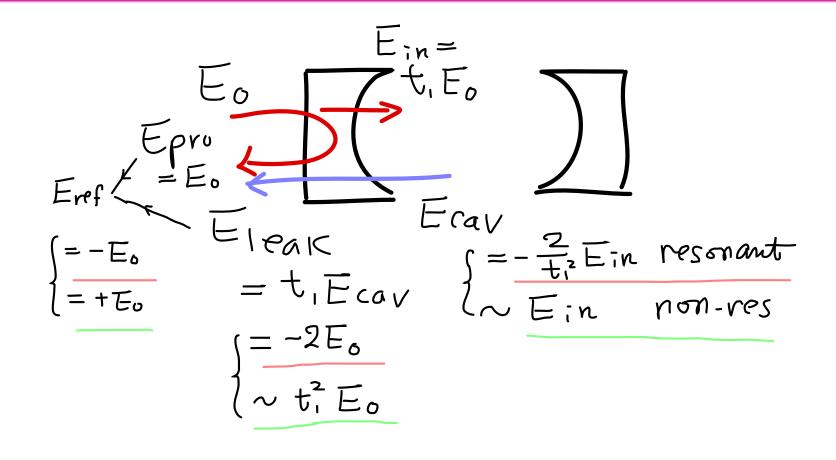


$$\Delta \eta = \eta(z_2) - \eta(-z_1) = a\cos(1 - \frac{L}{R})$$
 for  $R_1 = R_2 = R$ 

- Resonance condition
  - »  $\phi = n\pi$  for main mode
  - » non resonant for other modes

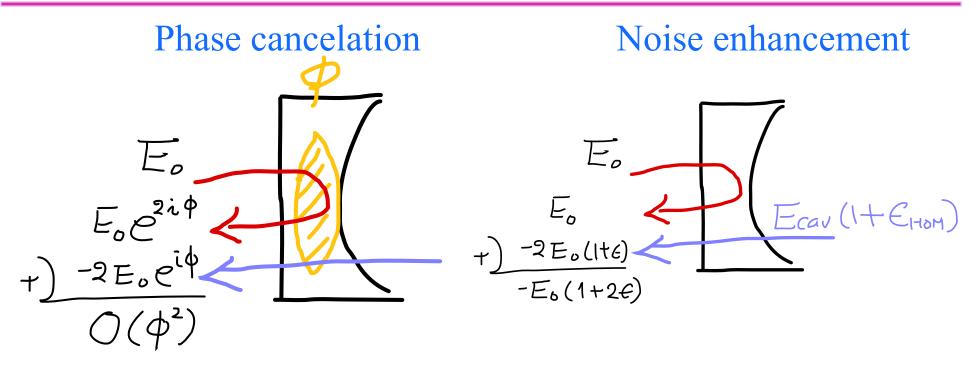


### Cavity basic Resonant vs non-resonant





### Cavity basic Phase cancelation and noise enhancement

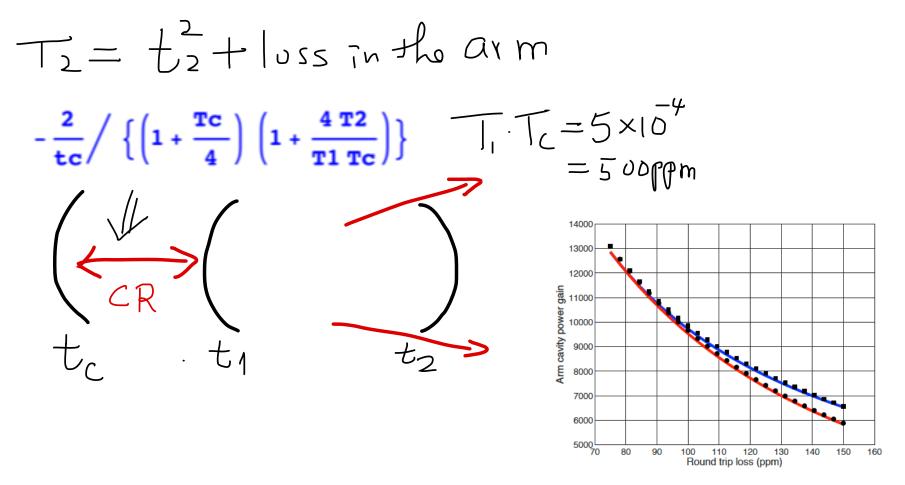


Only carrier (injected field which resonate in the cavity) not sideband (not resonating in the cavity) nor signal sideband (induced in the cavity)

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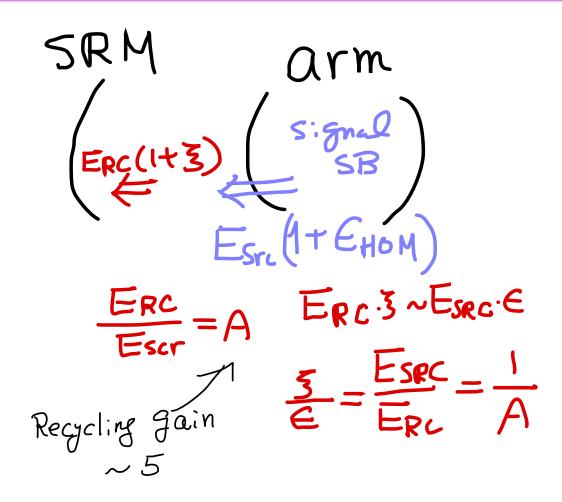
## Cavity basic Coupled cavity



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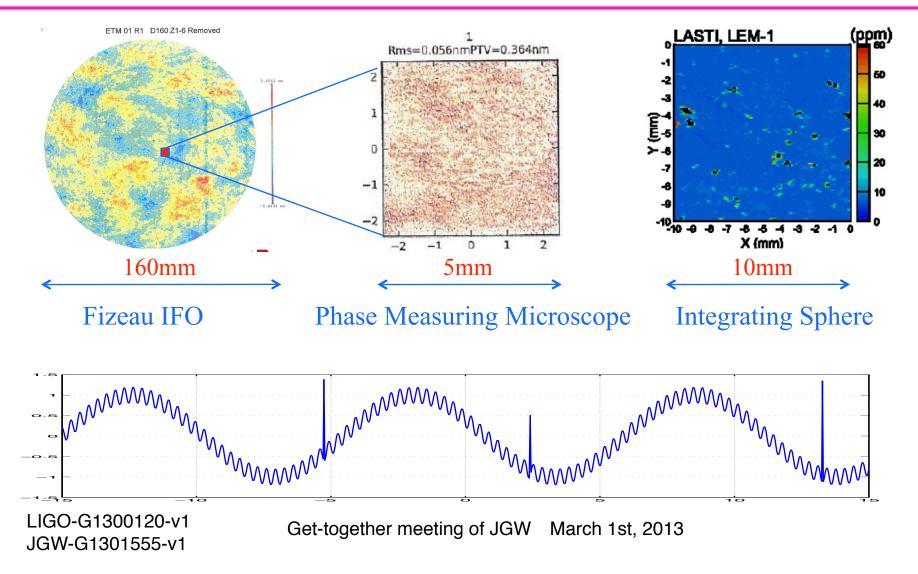
## Cavity basic Mode healing



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# Surface structure with different spatial distribution





# Scattering by aberration

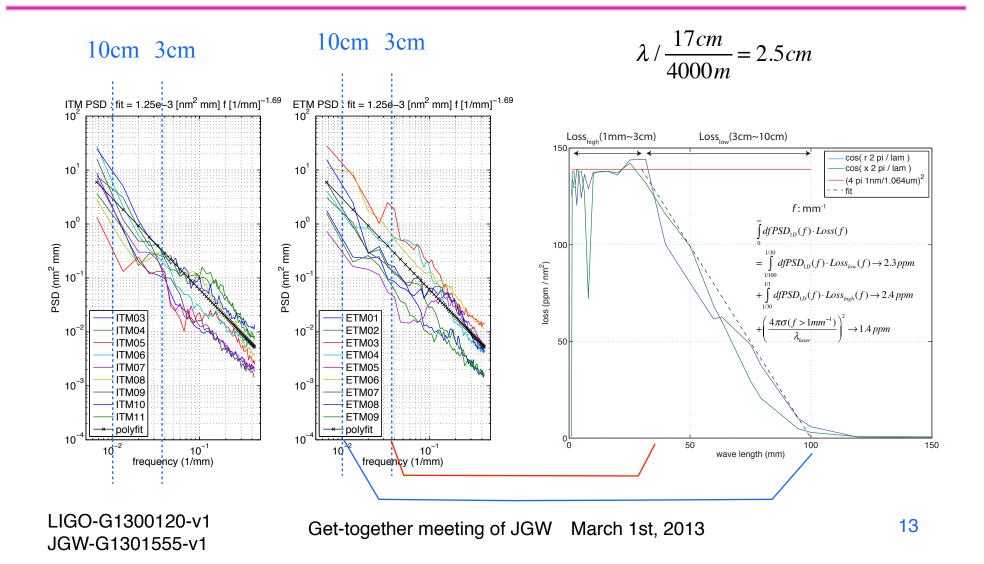
$$\begin{split} E_{ref} &= E_{ref}^{0} \cdot \exp(i2k\delta(x,y)) & dP = \iint dx \, dy \left| E_{ref}^{0} \right|^{2} 4k^{2}\delta(x,y)^{2} \\ &= E_{ref}^{0} \cdot (1+i2k\delta-2(k\delta)^{2}) \\ &= E_{ref}^{0} \cdot (1-2(k\delta)^{2}) + E_{ref}^{0} \cdot i2k\delta \\ &= \int dx \, dy \delta(x,y)^{2} / S \\ &= \int df \, PSD_{1D}(f) \\ for \, \delta(x,y) &= \delta_{0} \sin(k_{x}x) \\ &= E_{ref}^{0} \cdot i2k\delta = E_{ref}^{0} \cdot i2k\delta_{0} \sin(k_{x}x) \\ &= E_{ref}^{0} \cdot (k\delta_{0}(\exp(ik_{x}x) - \exp(-ik_{x}x))) \\ &= E_{ref}^{0} \cdot (k\delta_{0}(\exp(ik_{x}x) - \exp(-ik_{x}x)) \\ &= E_{ref}^{0} \cdot (k\delta_{0}(\exp(-ik_{x}x) - \exp(-ik_{x}x)$$

simple loss

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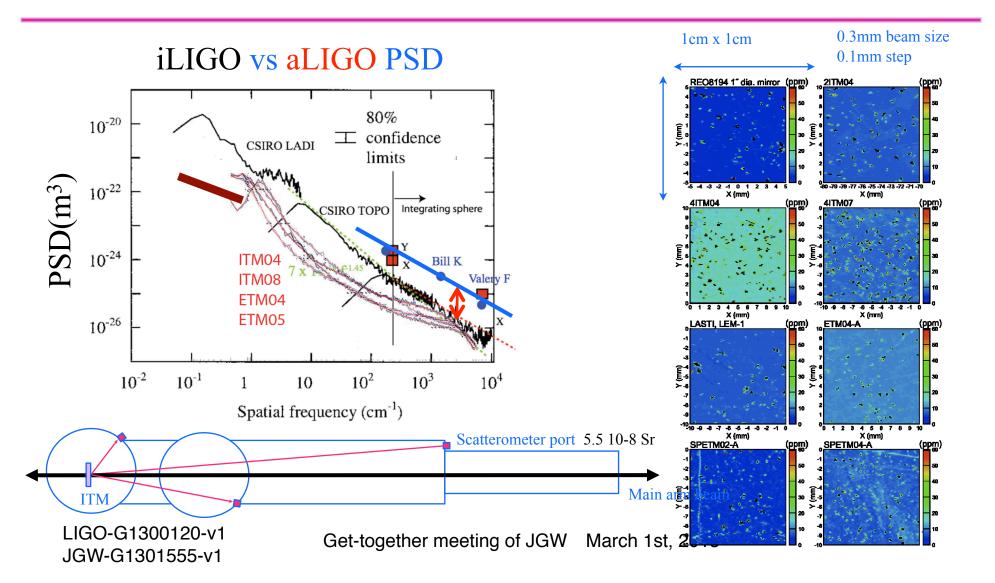


## aLIGO optics scattering loss by polished surface





# Peeking at LIGO mirror profile





# BRDF ≠PSD

#### • BRDF

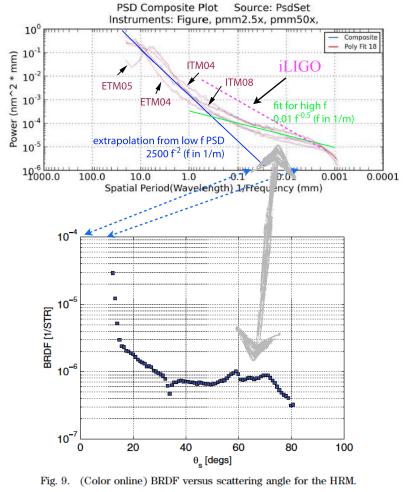
» how light is reflected by an opaque surface

PSD

» spectral density of the surface

$$BRDF(\theta) = \left(\frac{4\pi}{\lambda^2}\right)^2 PSD_{2D}(f) = \left(\frac{4\pi}{\lambda^2}\right)^2 C \frac{PSD_{1D}(f)}{f}$$

$$\lambda_s = \frac{1}{f} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \Theta = \frac{2 \ln s_{er}}{\lambda_s} = f \cdot \lambda_{gaser}$$

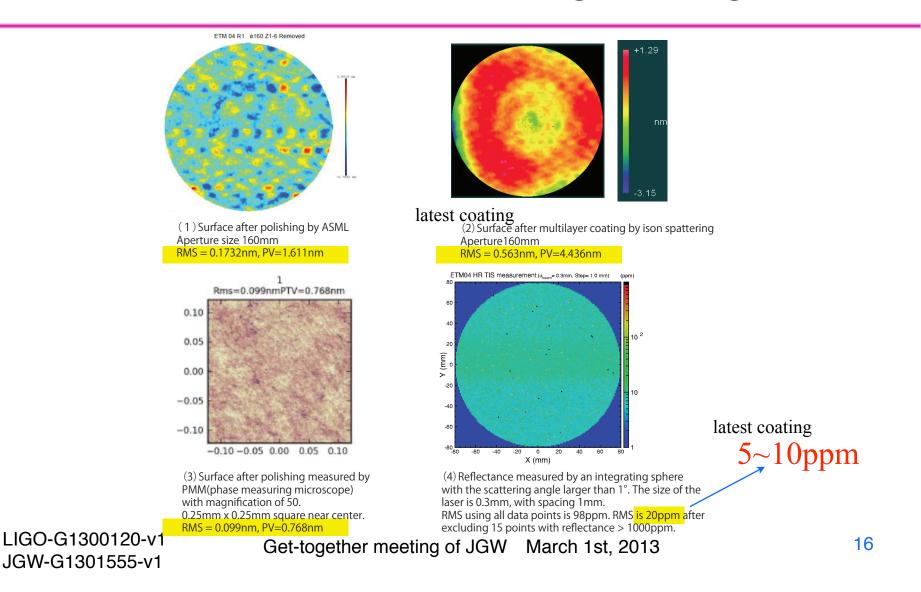


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# Polishing and coating ETM04 : coating is tough





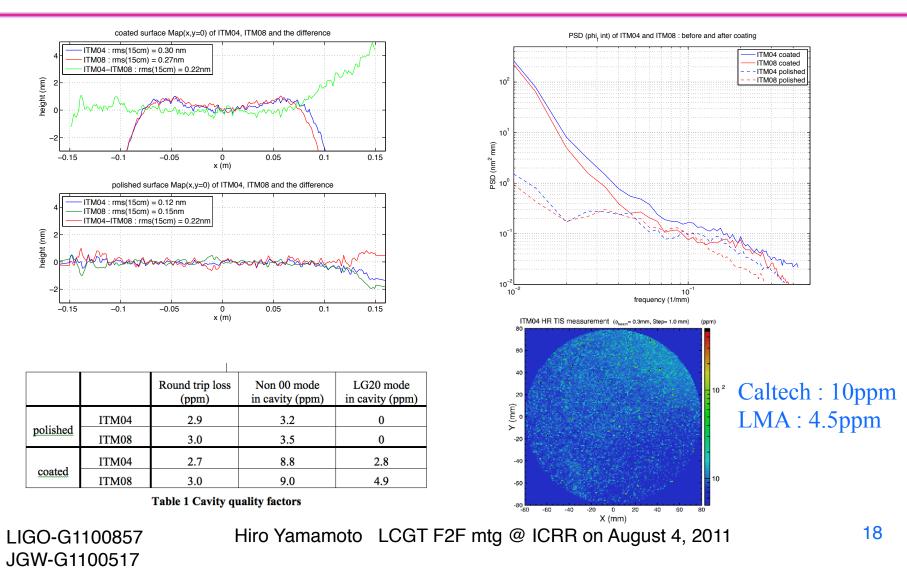
# Polishing by Coastline and ASML

Requirement and result of ITM04

Surface	Specification Parameter	Location	Specification Value	Actual Value	Pass/Fail
1	Spherical, CC, RoC	Central 160 mm	1934 m - 5m/+15m	1938.61 m	PASS
	Radius Difference from all ITMs	Central 160 mm	1938.53 m ± 3 m	0.08 m	PASS
	Astigmatism Amplitude (Z <sub>2,2</sub> )	Central 160 mm	σ <sub>RMS</sub> < 3 nm	0.12 nm	PASS
	Figure Error (LSF) <1mm <sup>-1</sup>	Central 300 mm	σ <sub>RMS</sub> < 2.5 nm	0.37 nm	PASS
	$Z_{0,0} \cdot Z_{1,1} \cdot Z_{2,0} \cdot Z_{2,2}$ Fit	Central 160mm	σ <sub>RMS</sub> < 0.3 nm	0.15 nm	PASS
	Error (HSF) 1-750mm <sup>-1</sup>	Center, Ø60 mm, Ø120 mm	σ <sub>RMS</sub> ≤ 0.16 nm	0.137 nm	PASS



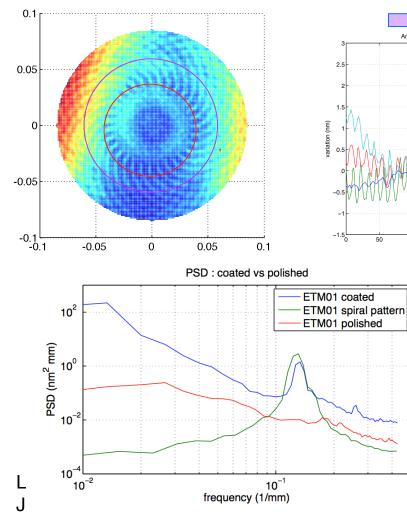
### Coating by LMA ITM04 and ITM08

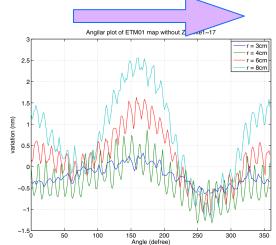




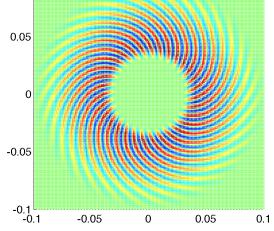
## Coating by LMA ETM01

measured at Caltec - Z1~Z7





P-V 1 nm



Using matlab to extract the spiral pattern, and use it as the phasemap in SIS

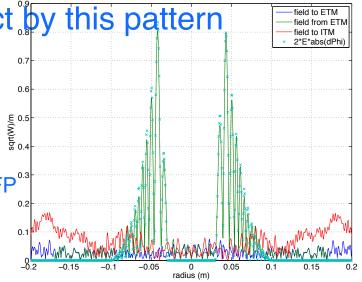
0.1

tg @ ICRR on August 4, 2011

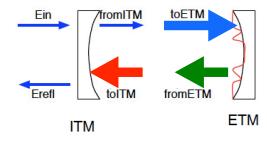


# LMA ETM01 coating accepting test short wavelength spiral pattern

- SIS analysis to understand the effect by this pattern
- Any other effects
  - » Field aberration due to this pattern
    - Field in FP with this map Field in idealistic  $FP^{\circ}$
    - Very fine grid sizes to make sure FFT is OK
  - » Mode analysis if any mode could dominate
    - No dominant mode for LGpm (2p+m<25) and HGmn (m+n<25)</li>
  - » If ITM has similar pattern, can they interfere
    - ITM = MAPPING (DATAFILE("ETM01pattern.dat"), "-x","y") \* 0.5
    - Loss = loss by ETM + loss by ITM no additional by interference



spiral pattern on ET



LIGO-G1100857 JGW-G1100517 Hiro Yamamoto LCGT F2F mtg @ ICRR on August 4, 2011

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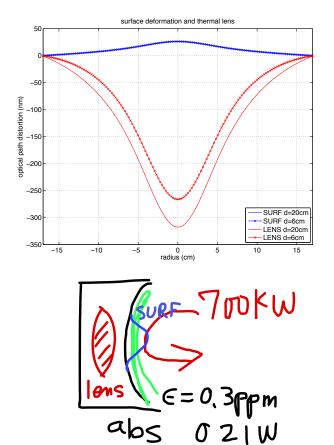
# LMA ETM01 coating accepting test long wavelength central plateau

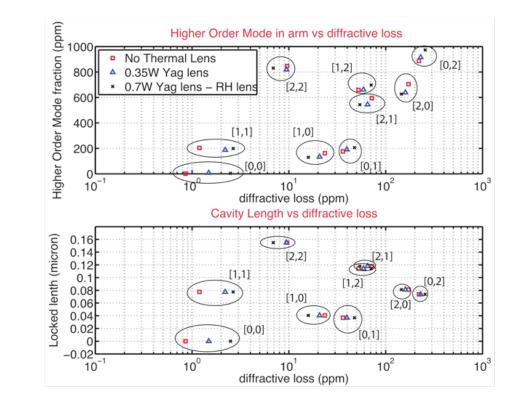
#### Old coating system, one at a time

- » The beam size on ETM is larger than that on ITM and the plateau size on ETM needs to be 20% wider, when coating to coating variation is taken into account
- New coating using the planetary system, a pair at a time
  - » Higher order mode, mostly LG20, in the FP cavity is ~100ppm
    - Better than old, 120ppm, and two ETMs will be "identical", but is this good enough?
    - The plateau size is around the same as the old one
    - Astigmatism uncertainty due to the substrate is not a major issue
    - Asymmetry in the far outside is better (smaller) in the new coating
  - » Coupled cavity simulation
    - LG20 in SRC shows no increase of LG20 by the mode healing
      - Stable signal recycling cavity kills LG20 in SRC
    - LG20 in PRC is ~2000ppm increase by the ETM coating aberration



## Thermal distortion test mass



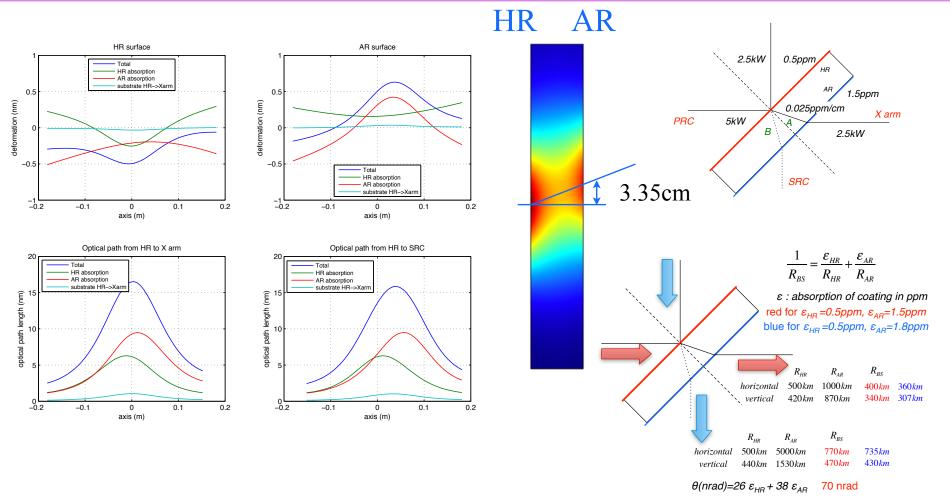


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abs



## Thermal distortion BS

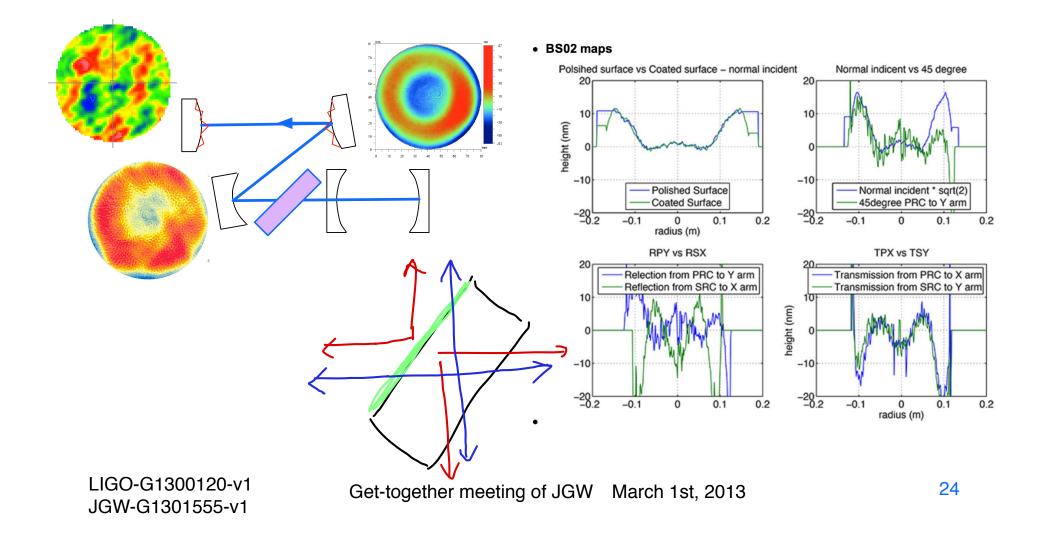


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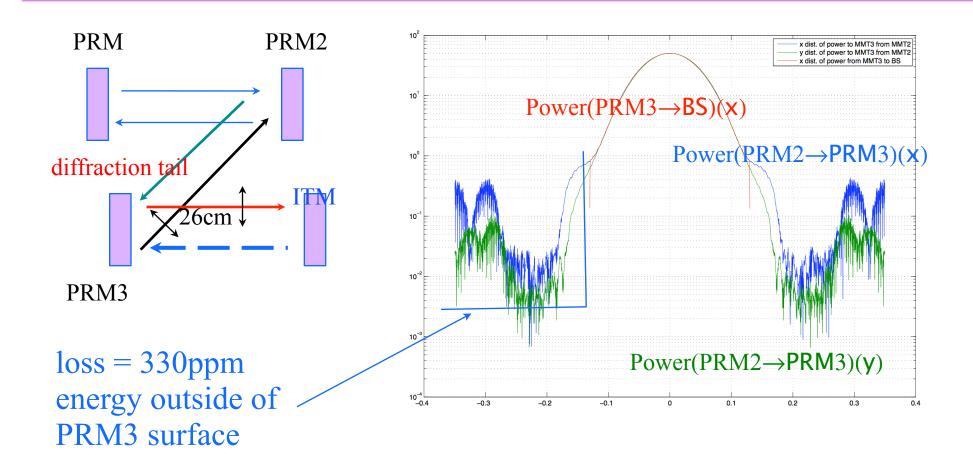


## Not so nice looking mirrors

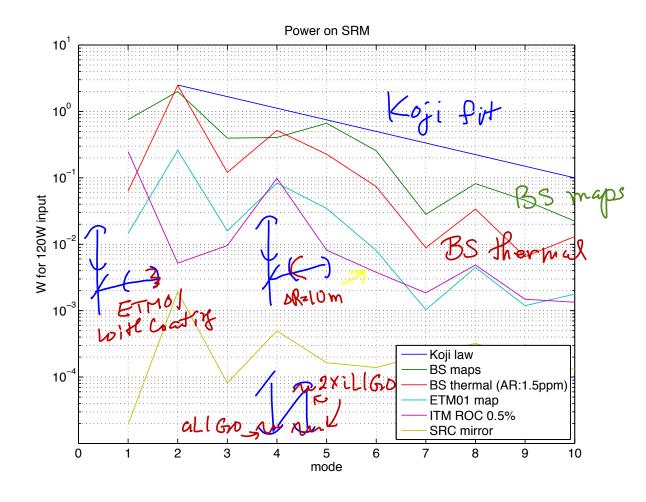




## Why ROC(ITM) < ROC(ETM) Power loss on RM3







LIGO-G1300120 JGW-G1301555-v1