2012/08/21 Thermal Noise Seminar @ Jena



Cryogenic Suspension for KAGRA and Suspension Thermal Noise Issues

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As a member of vibration isolation system (VIS) subgroup for KAGRA



Contents



- 1. Introduction of KAGRA cryogenic suspensions
- 2. Suspension thermal noise in KAGRA
- 3. Ideas to reduce suspension thermal noise in KAGRA
- 4. Summary and discussion

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KAGRA-SAS Overview

Suspension systems for KAGRA core optics



KAGRA-SAS Key Technologies





Cryogenic Suspension for KAGRA KAGRA



KAGRA Cryogenic Payload Schematic Design





KAGRA Cryogenic Payload Heat Flow





Initial cooling time problem



 ~ months to reach target temperature



→ Slow down commissioning, reduce duty cycle

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Heat link wiring problem

- Aluminum heat links work as soft mechanical springs (~10 mHz)
- Cryostat vibration is transmitted to the mirror via heat links
- → Spoil the performance of SAS







More details: GWADW2012 presentation, JGW XXX-XXXX



Sapphire fiber problem

- **Thick** and **short** sapphire fibers (Φ1.6 mm, L 30 cm).
- Rough surface decreases thermal conductivity
 → Need surface polishing
- Sapphire bonding may be necessary??

Many difficulties in engineering!!



Sapphire fiber problem

Vertical bounce mode and violin mode peaks at ~100 Hz. → Pollute detector sensitivity!!





We use cryogenic suspension for thermal noise reduction.

- Many difficulties have been found.
 - Initial cooling time is quite long.
 - Heat links introduce non-negligible seismic noise.
 - Thick sapphire fibers introduce non-desired peaks around target frequencies.

Still many R&Ds remain!! (but schedule is tight...)

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- Thermal fluctuation of mirror displacement due to mechanical loss of suspension system.
- Power spectrum can be predicted by fluctuationdissipation theorem

$$x_{\text{therm}}^{2}(\omega) = \frac{4k_{B}T}{\omega} \text{Im}[H(\omega)]$$

Imaginary part of force – displacement transfer function

Suspension Thermal Noise

Thermal fluctuation of simple oscillator

- Material loss: structural damping model
- Pendulum Q is larger than intrinsic material Q (dissipation dilution)







k

Dissipation dilution



In pendulum, most potential energy stored as lossless gravitational potential energy



Ue: Potential energy stored in the bending of fibers Ug: Gravitational potential energy (lossless)

 $\phi_{\rm pendulum} =$ $\varphi_{\rm fiber}$ []

1 / Dilution factor



Dilution factor gets large for thin and long fibers

$$\mathrm{DF} \propto L, d^{-2}$$

L: wire length, d: wire diameter

However, thick and short fibers are used in KAGRA for thermal conduction.

> Initial LIGO dilution factor: ~464 KAGRA dilution factor: ~19



Sapphire fiber thermal noise estimation (pendulum mode) $f = 1 \text{ Hz}, \phi = (2 \times 10^{-7})/19, T = 20 \text{ K}$



Violin Modes

For high frequency response, violin modes of fiber should be taken into account.

Eq. of motion of fiber

 $\rho \ddot{x}_{w}(z) = EI \frac{d^{4}}{dz^{4}} x_{w}(z) - T \frac{d^{2}}{dz^{2}} x_{w}(z)$

$$M\ddot{X} = EI \frac{d^3 x_w(z)}{dz^3} \bigg|_{z=L} - T \frac{dx_w(z)}{dz} \bigg|_{z=L}$$



Ζ



Sapphire Fiber Thermal Noise



 Sapphire fiber thermal noise estimation (pendulum mode + violin modes)



Vertical Thermal Noise



- In KAGRA, we have un-avoidable V-H coupling of 1/300.
- Contribution of vertical thermal fluctuation is not negligible.





Generally, thermal noise from upper stage (and recoil mass) loss is cut off at high frequencies.





In KAGRA, due to large stiffness of sapphire fibers, vertical thermal noise from upper stage (and recoil mass) loss directly transmits to the mirror.





 Thermal noise simulation including upper stages and recoil mass (with intrinsic material Q of ~10⁴)



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- Thick sapphire fibers introduce resonant peaks of vertical & violin modes around 100 Hz.
- Thermal noise from upper stages and recoil mass is not negligible even at high frequencies.
- Especially, recoil mass can introduce large vertical thermal fluctuation at 20-200 Hz.



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- Vertical thermal noise
 - Reduce V-H coupling (1/300)

Reduce vertical bounce mode frequency (~100 Hz)

Horizontal thermal noise

Increase dilution factor (~19)

- Push violin modes to higher frequencies (~200 Hz)
- Loss at recoil mass
 - Improve recoil mass suspension (Q~10⁴)

Remove recoil mass

New Suspension Design

- A fresh approach to the design of low thermal noise cryogenic suspension for KAGRA (and ET)
- Design development is conducted by R. DeSalvo









- Vertical stiffness of sapphire fiber introduces:
 - An annoying peak around 100 Hz
 - Large thermal fluctuation from recoil mass stage

Practically, we cannot equalize tension of four fibers.





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Cantilever Spring

- Hold the mirror from cantilever springs
- What material should be used?
 - High Q
 - Large thermal conductivity
- → Candidate: **silicon** cantilever





Silicon cantilever blades



- Etch the bending area
- Leave thick section for clamping and for fiber connection
- With 0.15 Gpa only limited flexure possible (~25 Hz)
- With >1GPa large deflection



4.9 rad





- MEM sensors operating at 1.4 GPa, ~ 10 times higher limit!
- Is etching eliminating surface defect and therefore causing the larger strength?
- if YES, large bends possible!
- Lower frequency bounce modes



NIKHEF Test



Produce a number of samples

Test and see



Silicon Cantilever Solution



 Thermal noise estimation with cantilever spring (assuming f₀ ~10 Hz, Q~10⁻⁷)

Pitch



Frequency [Hz]

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Small dilution factor due to thickness of fibers.

Can we increase dilution factor without spoiling thermal conductivity?

 \rightarrow Fiber with **flexure** design





Most bending energy concentrates on the fiber ends

Why Flexure?

Bending energy can be reduced by using soft fiber in the ends







Flexure Design



- Ultra-Sound Machined structure
- Etching of the flexure surface
- Expected to increase the break point >1GPa





Ribbons Key features:

- Compression joint attachment
- Machined-polished Sapphire ribbons
- (from bulk, not grown)
- High quality sapphire
- High quality surface finish (sub-phonon defect size)
- = > High thermal conductivity !





Preliminary result (calculated last night...)





We can push the violin modes to higher frequencies.





- Can We Remove Recoil Mass ??
- Thermal noise from RM suspension loss is quite large.
- Can we remove recoil mass??
- In Virgo, the actuators on TM are not used during operation!! (thanks to large seismic attenuation)









No suspended recoil mass for TM

- Actuators only used for damping
- Coil should be opened during operation



No Recoil Mass Case



- No peaks at 10-100 Hz!!
- Alternative: also employ springs for RM





Summary



- Using low-loss cantilevers, vertical thermal noise is dramatically reduced and annoying peak disappears.
- Fibers with flexure design has both profit and demerit.
- Removing RM, or employing cantilever for RM?



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Discussion



The END



Appendices



Flexure Design



- Ultra-Sound Machined structure
- Etching of the flexure surface
- Expected to increase the break point >1GPa





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- Compression joint attachment
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Why Gallium



- Indium proved extremely effective to eliminate friction noise in compression joints (Vladimir Braginsky)
- Melts at relatively high temperature
- May need heating mirror to more than 160°C for disassembly

Indium vs. Gallium



Property	Unit	Indium	Gallium	score
Solid density (near r.t.)	g⋅cm ⁻³	7.31	5.91	
Liquid density @ m.p.	g⋅cm ⁻³	7.02	6.095	
Expansion at melting		1.041	0.9696	G
Melting point	°K	429.7485	302.9146	G
Melting point	°C	156.60	29.77	G
Wetting silicates		Yes	Yes	Х
Boiling point	К	2345	2477	G
Vapor pressure	Ра	1 @ 1196°K 📏	1@1310°K	G
Vapor pressure	Pa	10@1325°K	10@1448°K	G
Elec. resistivity (20 °C)	nΩ·m	83.7	270	
Thermal conductivity	$W \cdot m^{-1} \cdot K^{-1}$	81.8	40.6	Ι
Therm. expansion (25 °C)	µm•m ⁻¹ •K ⁻¹	23.1	18.0	G
Young's modulus	GPa	11	9.8	Х
Poisson ratio			0.47	
Brinell hardness	МРа	8.83	60	G
Atomic radius	pm	167	135	
Magnetic ordering		diamagnetic	diamagnetic	Х

Violin mode elimination



Fiber-fed Red-shifted Fabry-Perot Can cool violin modes and bounce modes to mK level (Same for Parametric Instabilities ?)



Conductance budget

- Preliminary conductance budget from Sakakibara with 1 W load
- Thin ribbon responsible for bulk of loss !!!
- Plenty of space for parametric optimization



Chao Shiu laboratory, Taiwan Silicon cantilever with KOH wet etching

4" un-doped double-side polished (001) silicon wafer, 500 m thickness etched down to 92 and 52 μ m



0.3 10⁻⁶ loss measured from residual gas

Thermo-elastic limit



- @ 59 Hz 0.945 10⁻⁶ loss angle predicted (T.E.)
- 1.3 10⁻⁶ measured (-) 0.3 10⁻⁶ residual gas
- 1.10⁻⁶ loss angle measured
- => 100% Thermoelastic limited !!!





Distribution of thermal noise source (H)





Distribution of thermal noise source (V)



Mode Shape (Beam Profile)



