

Continuum, Grain and Burst Behaviors of Stochastic Gravitational Waves from Cosmic Strings by Numerical Simulation



Hirotaka Yuzurihara, Nobuyuki Kanda, Takahiro Yamamoto, Kazuyuki Tanaka and KAGRA collaboration

yuzurihara@yukimura.hep.osaka-cu.ac.jp Department of Phycics, Osaka City University, Osaka, Japan

Market Abstract

With network of ground-based detectors (KAGRA, aLIGO, aVirgo, AIGO), we calculate overlap reduction function and estimate upper limit for isotropic stochastic gravitational wave background (SGWB), $\Omega_{aw}h_0^2 > 10^{-9}$.Compared upper limit estimated with theoretical

predictions of SGWB, we may detect gravitational wave(GW) from cosmic string. Although there are cusp on loop and kink on finite string which emit GW from cosmic string, in this study we focus on GW from cusp. Beamed GW burst are emitted from cusp. GW of bigger amplitude much than detector noise is seen as burst GW, and GW of smaller amplitude appear as continuum of stochastic background. We are also interested in the behavior of small GW components - "grains of small bursts" -, which amplitudes are similar to the detector instrumental noise level and its rate is order of 1Hz. Less enough analysis has performed for such GW before. The waveform of GW from cosmic string in time domain is known. Then we generate simulation data by method that one GW superpositions many times. In this poster, we calculate waveform of GW from cusp and some values which characterize waveform.

What's "Grains of small bursts"?

Usually gravitational wave is categorized by size of amplitude. As there are loops having various circumferences in Universe, the amplitude of GW from cusp covers a very wide range.



Flow Chart



Property of Cosmic String

Cosmic string is one dimensional topological detect which can be formed in the Early Universe. Strings form the network including infinite strings and closed loops. Beamed GW burst are emitted from cusp.



FIG.1 Loops are produced when infinite strings collide and reconnect with themselves.

Cosmic string is characterized three parameters,

 μ : energy per length in string

- α : loop size for Hubble scale
- p: reconnection probability. (p=1 fixed)

When loop generated, typical loop size is αl_H . As loop emit GW,

loop lose its length and finally vanish. Although α is unknown, $G\mu/c^2$ is constrained by LIGO search [3] for GW burst from cosmic

string and by CMB observation [4].

$$G\mu/c^2 < 2.3 \times 10^{-7} \ (95\% \ c.l.)$$



FIG.2 When two curves which move to opposite direction intersect on loop, cusp is generated and emits GW. While circumference of loop L > 0, these events are repeated.

(bottom right) z_{make} vs period τ

Overlap Reduction Function

This function quantifies two effects:[1]

- 1, separation time delay between two detectors.
- 2, non-parallel alignment of the detector arms.

Of Upper Limit

Upper limit for isotropic stochastic background is estimated by following inequality, [1]





$$\begin{split} \gamma(f) &= \frac{5}{8\pi} \sum_A \int_{S^2} d\hat{\Omega} \ e^{i2\pi f \hat{\Omega} \cdot \Delta \vec{x}/c} F_1^A F_2^A \\ F_i^A(\hat{\Omega}) \text{ is the response of } i\text{-th (}i\text{=}1\text{,}2\text{) to the A = +,\times polarization} \\ \hat{\Omega} \ \text{ is a unit vector specifying a direction.} \end{split}$$



 $\Omega_{gw}(f) \ge \frac{1}{\sqrt{T_{tot}}} \frac{10\pi^2}{3H_0^2} \left[\frac{\gamma^2(f)}{f^6 P_1(f) P_2(f)}\right]^{-1/2} \times \sqrt{2} \left[\operatorname{erfc}^{-1}(2\alpha) - \operatorname{erfc}^{-1}(2\gamma)\right]$

 H_0 is a Hubble constant. $\gamma(f)$ is overlap reduction function. $P_i(f)$ is the noise power spectra. α is a false alarm rate. γ is a desired detection rate. (not overlap reduction function) Here, we fix $\alpha = 5\%$ and $\gamma = 95\%$.

And we can extend this upper limit from two detector to the network,

 $(h_0^2 \Omega_{gw})^{-2} = \sum_{j=0}^n \sum_{j<i}^n ((i,j)h_0^2 \Omega_{gw})^{-2}$

Taking combination of many detectors will improve upper limit. In this case, we calculate with KAGRA, LIGO Livingston, LIGO Hanford, Virgo, AIGO.

FIG.5 Frequency vs overlap reduction function $\gamma(f)$. On-going detectors are used to calculate. Labels mean that J is KAGRA, L is LIGO Livingston, H is Hanford, V is Virgo. Only detectors under going on are showed.

FIG.6 Frequency vs $\Omega_{qw}h_0^2$.

With Network of detectors, the upper limit for isotropic SGWB $\Omega_{qw}h_0^2 < 3 \times 10^{-9}$ reach