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Three-dimensional Rigid-Body Models of the Vibration Isolation Systems for LCGT

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Introduction

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- Mechanical models are necessary to estimate seismic noise and control noise in the interferometer
- Conventional 1-D models: No couplings between different DoFs
- Rotation occurs by couplings with translational motions
 Rotation amplitudes of the mirror must be estimated by 2-D or 3-D models
- When the beam-spot is off-centered, rotation of the mirror changes the light-pass.







Construction of the Models

Vibration Isolation Systems=
 Rigid Bodies+Elastic Elements (wires, springs)



- Each body has 6 DoFs (X,Y,Z,θx,θy,θz).
- Wire potential is divided into stretches and torsions.
- A GAS filter works as a uni-dimensional ideal spring.
- Elasticity of the heat links is taken into account.
- No deformation of the bodies, no violin motions of the wires





LCGT Type-A System: 10 bodies (57 DoFs)

Calculation Sequence



- Set the parameters (geometry, mass, moment of inertia, etc.)
- Calculate the potential (U), dissipation (F) and kinetic (T) energies.
- Find the local minimum (equilibrium point) of the potential (U).
- Linearize the equations of motion around the given equilibrium point.

$$\frac{d}{dt}\frac{\partial T(\mathbf{x}, \dot{\mathbf{x}})}{\partial \dot{x}_i} + \frac{\partial F(\dot{\mathbf{x}})}{\partial \dot{x}_i} + \frac{\partial U(\mathbf{x})}{\partial x_i} = f_i \xrightarrow{\text{Linearize}} \mathbf{M}\ddot{\mathbf{x}} + \mathbf{C}\dot{\mathbf{x}} + \mathbf{K}(\mathbf{x} - \mathbf{x}_{eq}) = \mathbf{f}$$

Calculate the eigen-frequencies and frequency response of the system.

Mathematica is used for the calculation.



Estimation of the spectrum densities of the angular fluctuation of the test-mass mirrors, due to seismic motions



Angular Motions of the Bodies



- Angular motions are excited by couplings with translational motions.
- The couplings come from asymmetry of the systems: vertical separations between suspension points and CoMs, asymmetry in the wire lengths or diameters, asymmetry in the spring constants, etc.



It is impossible to expect the asymmetry of the real systems.

→ Asymmetries are randomly given, and the computation is iterated for many times (Monte Carlo simulation)

Asymmetry Wire lengtsh: ±0.5 mm Wire diameters: ±5 % Suspension points: ±0.5 mm for x, y, z

- Effective stiffness of the inverted pendulums: ± 50 %
- Attachment point of the heat link: ±5 cm from CoM

Inverted Pendulums







Spectrum Density of the Mirror Angular Fluctuation

Iteration: 20

 Seismic motion spectrum : Measured data in February, 2007



Impact on the Sensitivity

Assume 1 mm misalignment of the beam spots.







Rough Estimation

RMS Amplitude





We need to consider the curvature of the mirrors, and the radiation pressure effects. \rightarrow Another talk from Y. Michimura

To suppress the RMS





Summery

- We construct **3-D rigid-body** models of the vibration isolation systems.
- We estimate the angular fluctuation of the test-mass mirrors due to the seismic motions.
- We find that the impact on the sensitivity by the mirror angular motion is smaller than the impact by the translational motion (under the given asymmetry for this time).

Future Works

- Validation of the calculation by prototype experiments
- Development of the local control systems of mirrors
- Estimation of the suspension thermal noise of the multi-pendulums







The End





Appendix





- Measured data on Feb. 13th, 2007
 (>20Hz is interpolation by f^(-2) function)
- Bad seismic weather. (Normally, the seismic motion is much smaller around 0.1~1 Hz)



Need More Attenuation!





Sensitivity curve (Jan. 2011) V.S. Seismic noise (H+V/300)

- Seismic noise is barely under the nominal sensitivity in > 10 Hz.
- > 2 Hz is affected by the heat links.
- The vibration on the inner shield of the cryostat might be larger than the ground vibration.
- We will need vibration isolation for the heat links



Compensation of Effective Bending Points

Due to the elasticity of the wire, the effective bending point and the clamp point is separated by:

$$\Delta = \sqrt{\frac{EI}{T}}$$

- E: Young's modulus
- I: Moment of area
- T: Tension



Dissipation



- Dissipation considered in the calculation : Viscous damping and Structure damping
- Viscous damping: Damping force is proportional to the relative velocity (Eddy current damping in our case)

$$E_{\rm Damp} = \frac{1}{2} C (\dot{x}_1 - \dot{x}_2)^2$$

 Structure damping: Caused by the internal friction of the elastic elements. The spring constants are extended to the complex numbers.

$$k \to k(1 + i\phi)$$

Dissipation Dilution



- In our models, the restoring force of pendulum is caused by the elasticity of the wires.
- In actual cases, the restoring force is caused mainly by the gravitational energy, so that the loss of the pendulum is smaller than the loss angle of the wire material.

$$\phi_{\text{Pendulum}} = \frac{1}{2L} \sqrt{\frac{EI}{T}} \phi_{\text{Wire}}$$

To take this into account, the dissipation of the vertical bonce of the wire and the horizontal motion of the suspended body is separately calculated.

What If the IM is Suspended by 4 Wires?

- Pitch-longitudinal couplings are relatively large.
- Additionally, we expect vertical-pitch couplings due to the asymmetry of the spring constants of mini-GAS filters.





Pitch





Yaw





Recycling Mirrors



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Beam Splitter

