

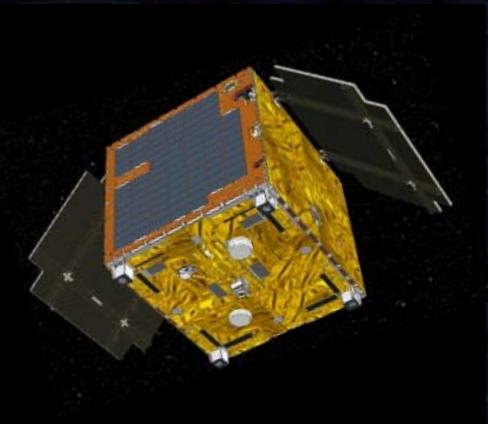
# TOBA: Torsion-Bar Antenna



Small-scale TOBA at Tokyo



Small-scale TOBA at Kyoto



SWIM on SDS-1 satellite

Masaki Ando (Kyoto University)

K. Ishidoshiro, K. Okada, A. Shoda, W. Kokuyama, K. Yagi, K. Yamamoto,  
H. Takahashi, N. Kanda, Y. Aso, N. Matsumoto, K. Tsubono, A. Takamori

# Abstract

## Low-freq. GW observation

- Large amplitude and/or stationary GWs radiated by sources with large masses and long time-scales → Different science.
- Difficult with ground-based detectors because of fundamental limitation and seismic disturbances
- Space-borne detector requires large resources.

## Novel GW detector : TOBA (Torsion-Bar Antenna)

- Low-freq. GW observation even with ground-based config.
- Unexplored band observation with space detector.

# 1. TOBA

Concept and Sensitivity  
Prototype results

# 2. Rotating TOBA

Concept  
Prototype results

## Reference:

- M:Ando, et. al, Phys. Rev. Lett. 105, 161101 (2010)
- K.Ishidoshiro, et. al, Phys. Rev. Lett. 106, 161101 (2011)
- A. Shoda, presentation at GWPAW2011

# TOBA

**Reference:**

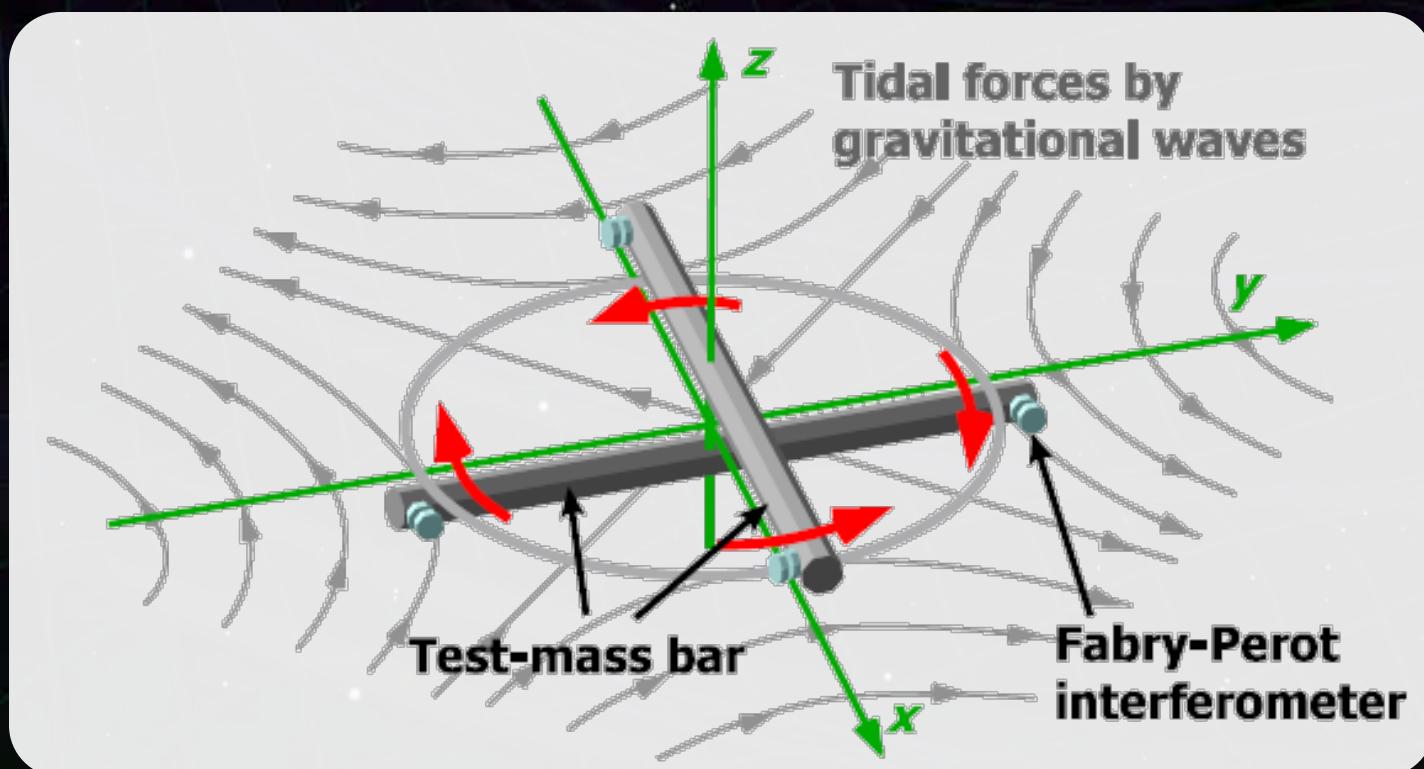
- M.Ando, et. al, Phys. Rev. Lett. 105, 161101 (2010)

## TOBA : Torsion-Bar Antenna

Monitors tidal-force fluctuation caused by GWs.

Two test-mass bars, placed orthogonal to each other.

Monitor differential angular fluctuation by interferometers.



M.Ando, et. al, Phys. Rev. Lett. 105, 161101 (2010)

# Detector response

## Equation of Motion of a test-mass bar

$$I \left( \ddot{\theta} + \frac{\omega_0}{Q} \dot{\theta} + \omega_0^2 \theta \right) = \frac{1}{4} q^{ij} \cdot \ddot{h}_{ij}(t)$$

$I$  : Moment of Inertia

$q^{ij}$  : Dynamic quadrupole moment

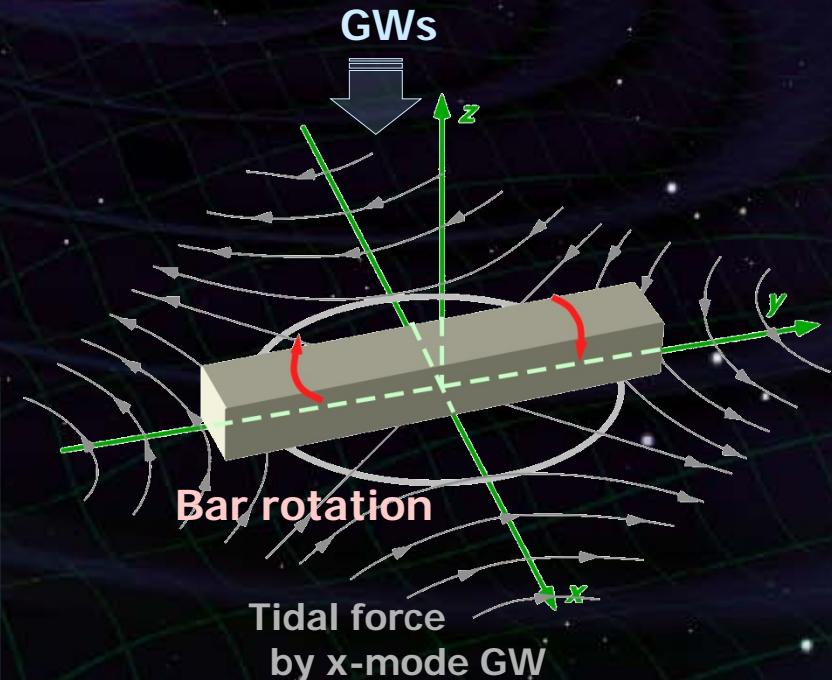


$$\tilde{\theta}(\omega) = \frac{1}{2} \alpha \tilde{h}_x(\omega) \quad (\omega \gg \omega_0)$$

$\alpha$  : shape factor, between 0 to 1

Dumbbell  $\rightarrow \alpha = 1$

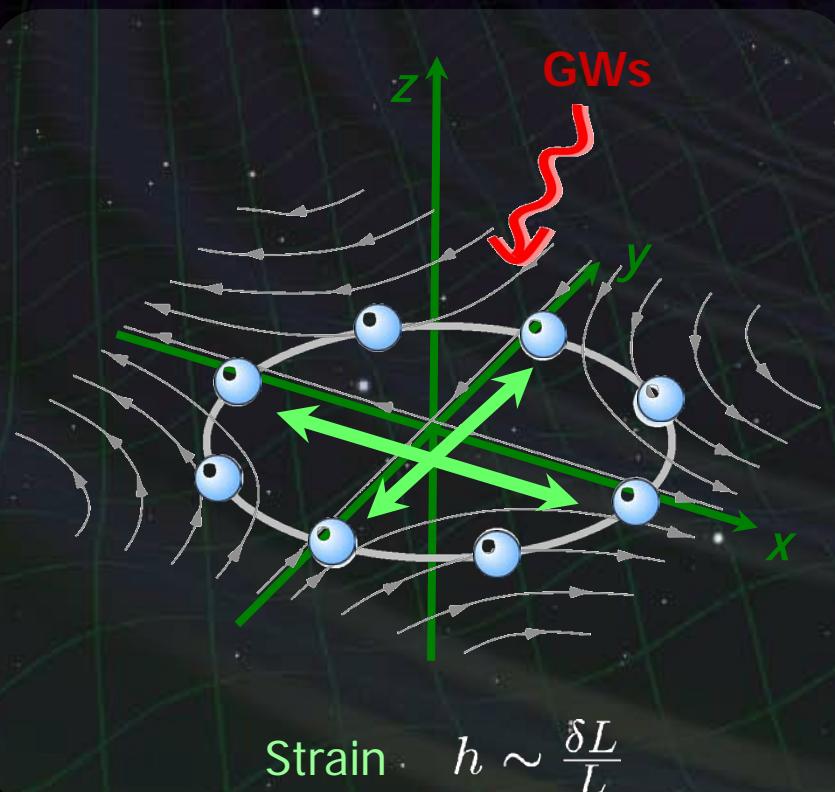
Dimension less,  
Independent of matter density



# Detection principle

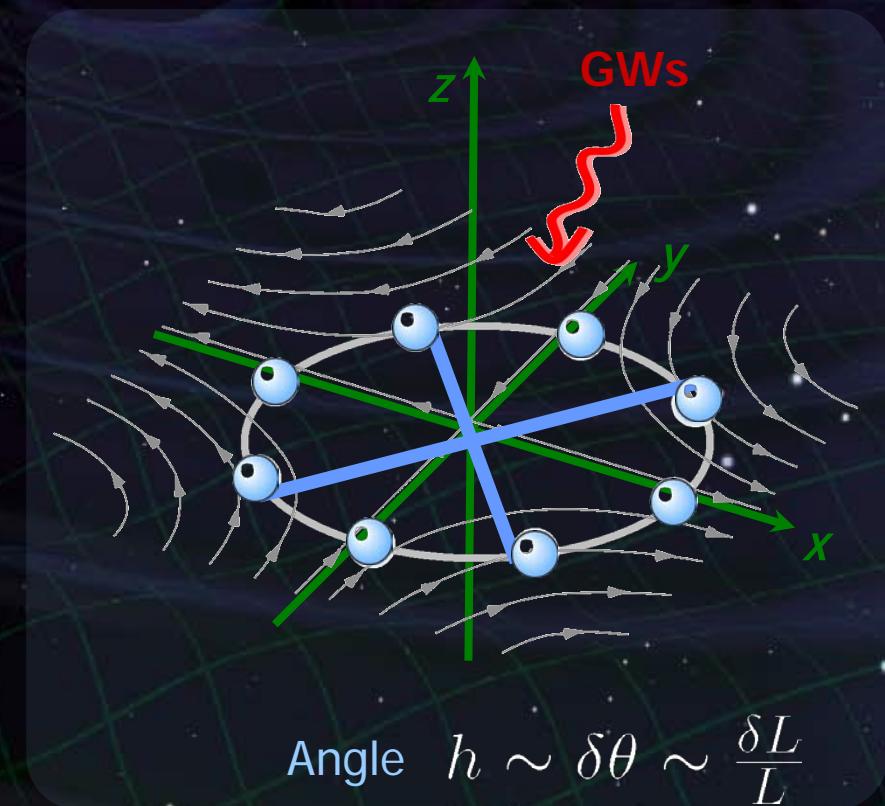
## Conventional IFO antenna

Detect differential length change



## Torsion-bar antenna

Detect differential rotation

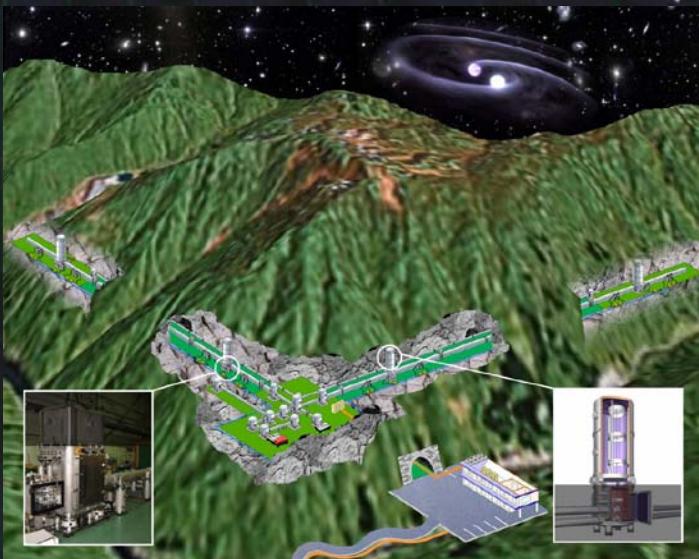


Observe change in tidal forces using free test masses

# Advantages

## Conventional IFO

Obs. band 10Hz-1kHz



Suspended as pendulum  
(Res. Freq. ~1Hz)

Long baseline  
→ High sensitivity

$$\text{SQL} \propto 1/(M \cdot L^2)^{1/2}$$

## TOBA

Obs. band 10mHz-1Hz

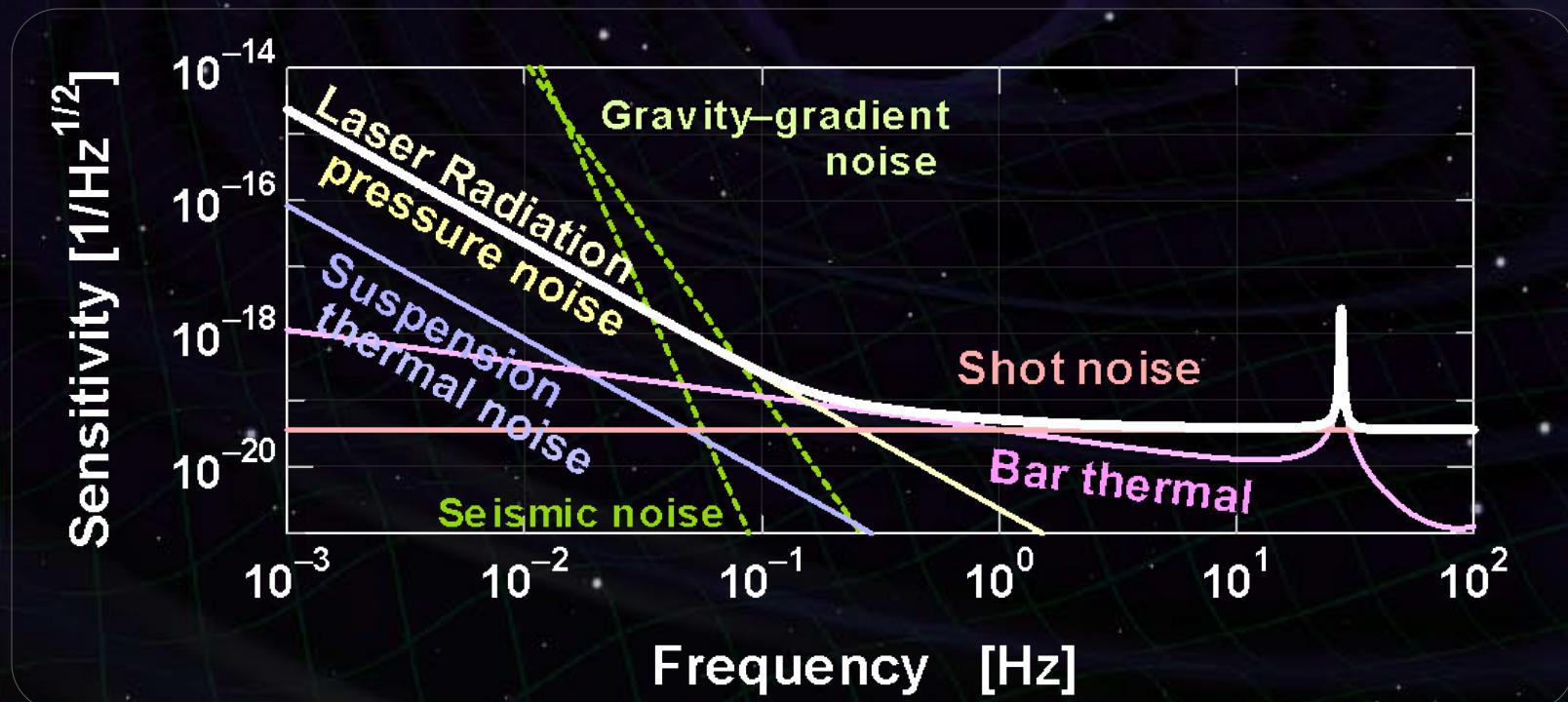


Torsion pendulum  
(Res. freq ~1mHz)

Shorter length  
→ Simple config.  
Common-mode rejection

# Fundamental noise level of TOBA

Practical parameters  $\Rightarrow \tilde{h} \simeq 3 \times 10^{-19} \text{ [Hz}^{-1/2}\text{]}$  (at 0.1 Hz)



Bar length : 10m, Mass : 7600kg

Laser source : 1064nm, 10W

Cavity length : 1cm, Finesse : 100

Bar Q-value : 10<sup>5</sup>, Temp: 4K

Support Loss : 10<sup>-10</sup>

Laser Freq. noise < 10Hz/Hz<sup>1/2</sup>,

Freq. Noise CMRR>100

Intensity noise < 10<sup>-7</sup>/Hz<sup>1/2</sup>,

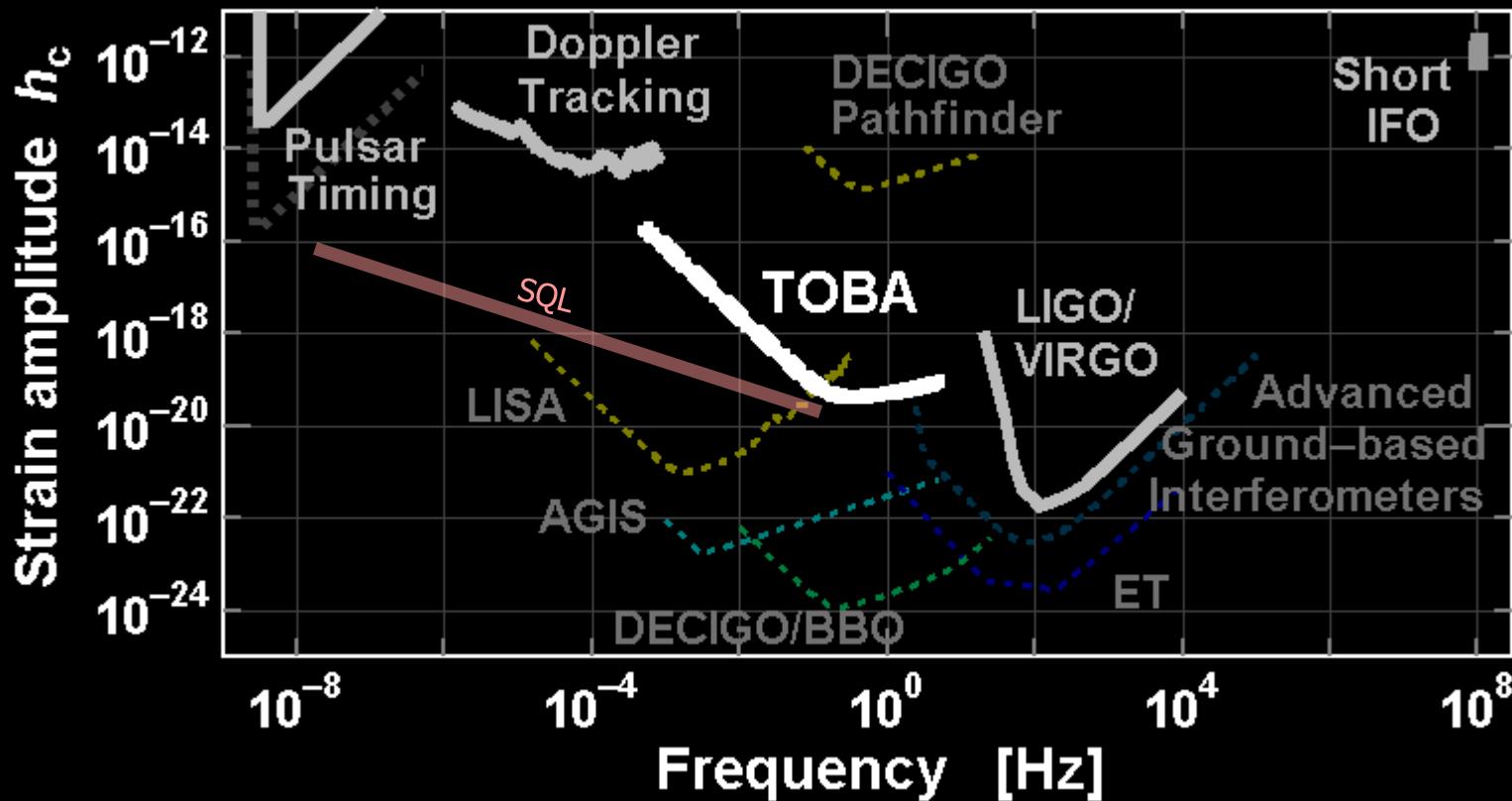
Bar residual RMS motion < 10<sup>-12</sup> m

# TOBA Sensitivity

## Comparison with the other detectors

DECIGO/BBO band:

Between ground-based detectors and LISA bands

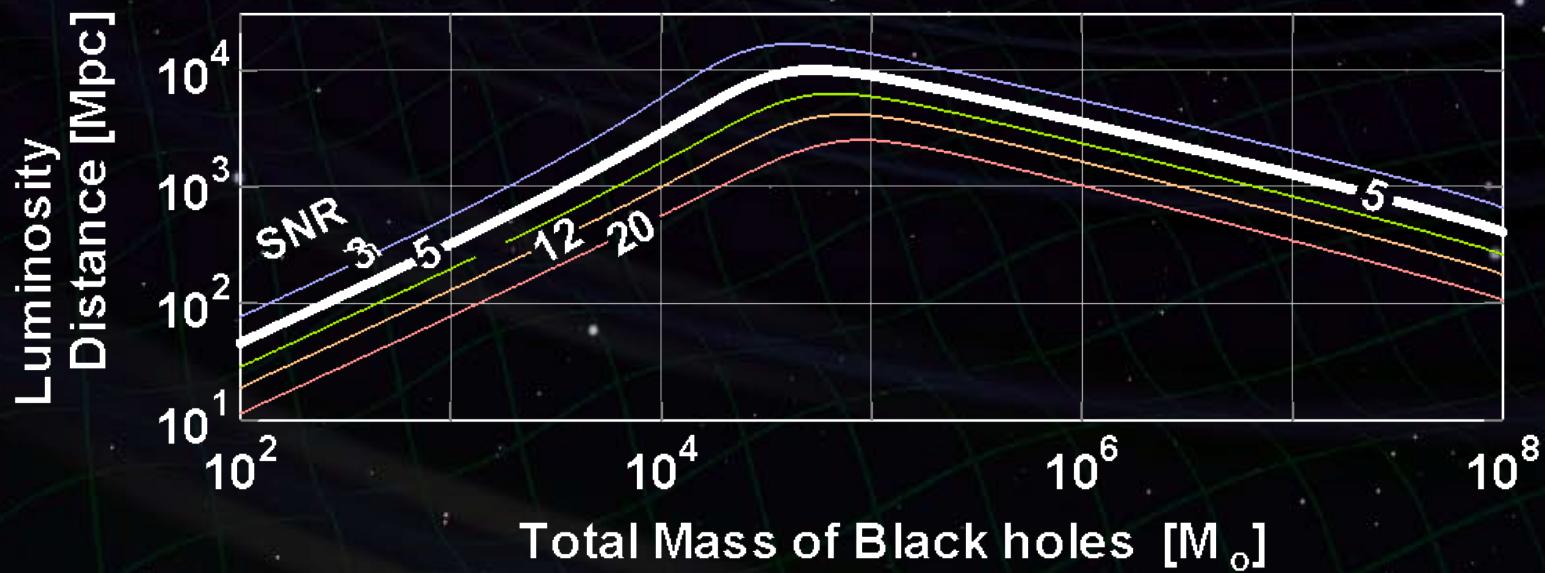


Characteristic amplitude :  $h_c = \tilde{h} \times \sqrt{f_{\text{center}}}$  (Dimensionless strain)

# Observable range

GWs from binary BH mergers

→ Obs. Range  $\sim 10\text{Gpc}$  ( $\sim 10^5 M_\odot$ , SNR = 5)



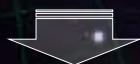
Calculation by K.Yagi

# Background GWs

Observable GW  
energy density ratio

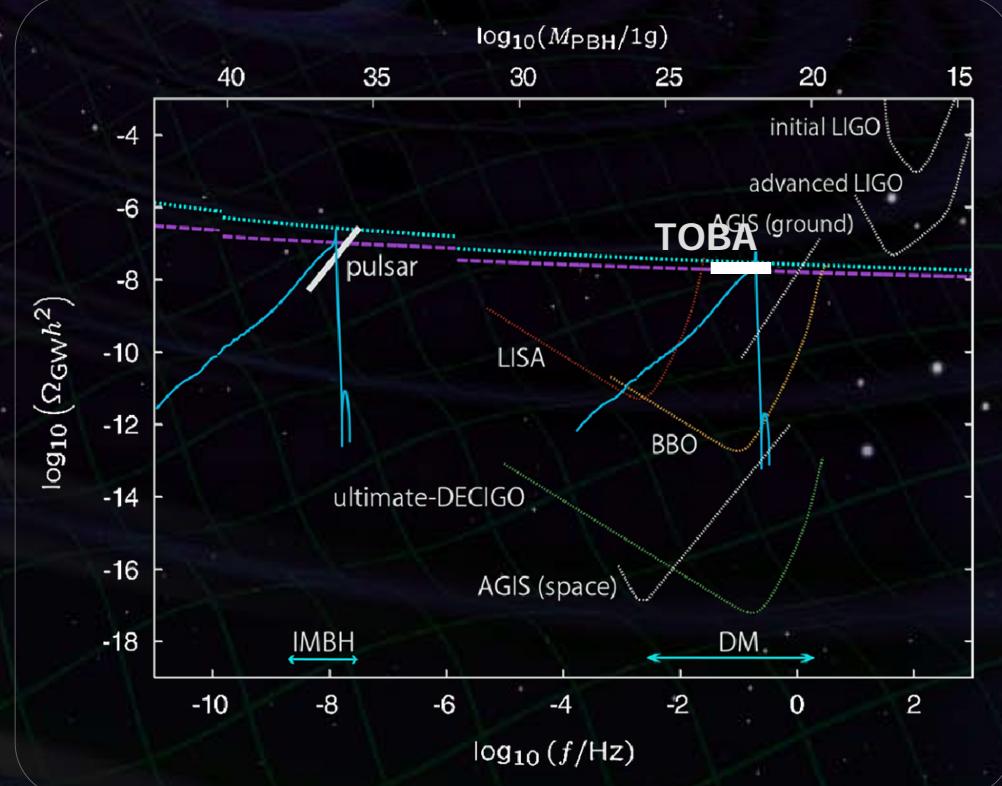
$$\Omega_{\text{gw}} \sim 10^{-7}$$

(1-yr obs. by 2 TOBAs)



Beat BBN upper limit  
GW by primordial  
tensor perturbation

R.Saito and J.Yokoyama,  
PRL 102, 161101 (2009)



# Prototype test

## Reference:

- K.Ishidoshiro, et. al, Phys. Rev. Lett. 106, 161101 (2011)
- A. Shoda, presentation at GWPAW2011

# Small-scale TOBA

- Optical readout

Mirrors at both edges of the test-mass bar  
→ Form Michelson interferometer  
Sensitive angular sensor

Nd:YAG laser source

Wavelength 1064nm  
Power 50mW

- Test-mass bar

Length ~200mm, Weight 160g  
Made of Aluminum  
Room temperature

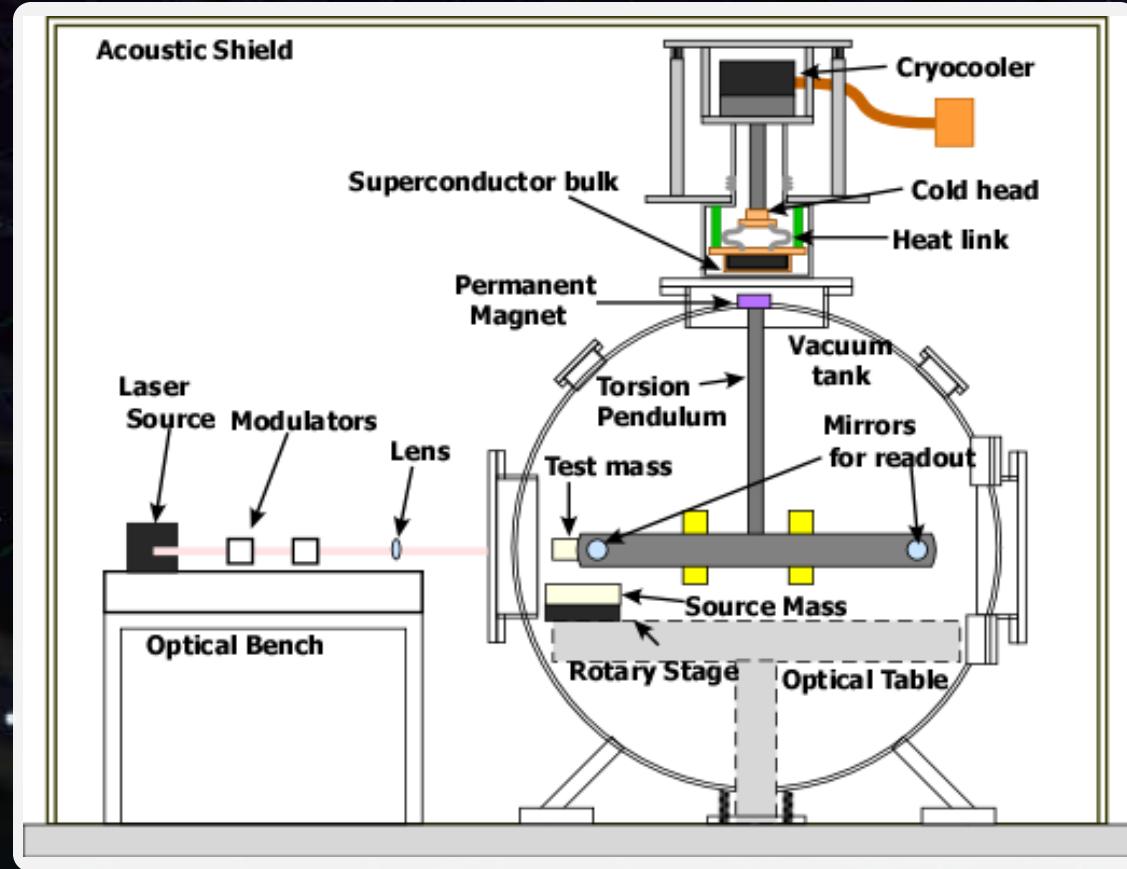
- Suspension

Magnetic levitation by pinning effect of type-II superconductor  
Superconductor bulk

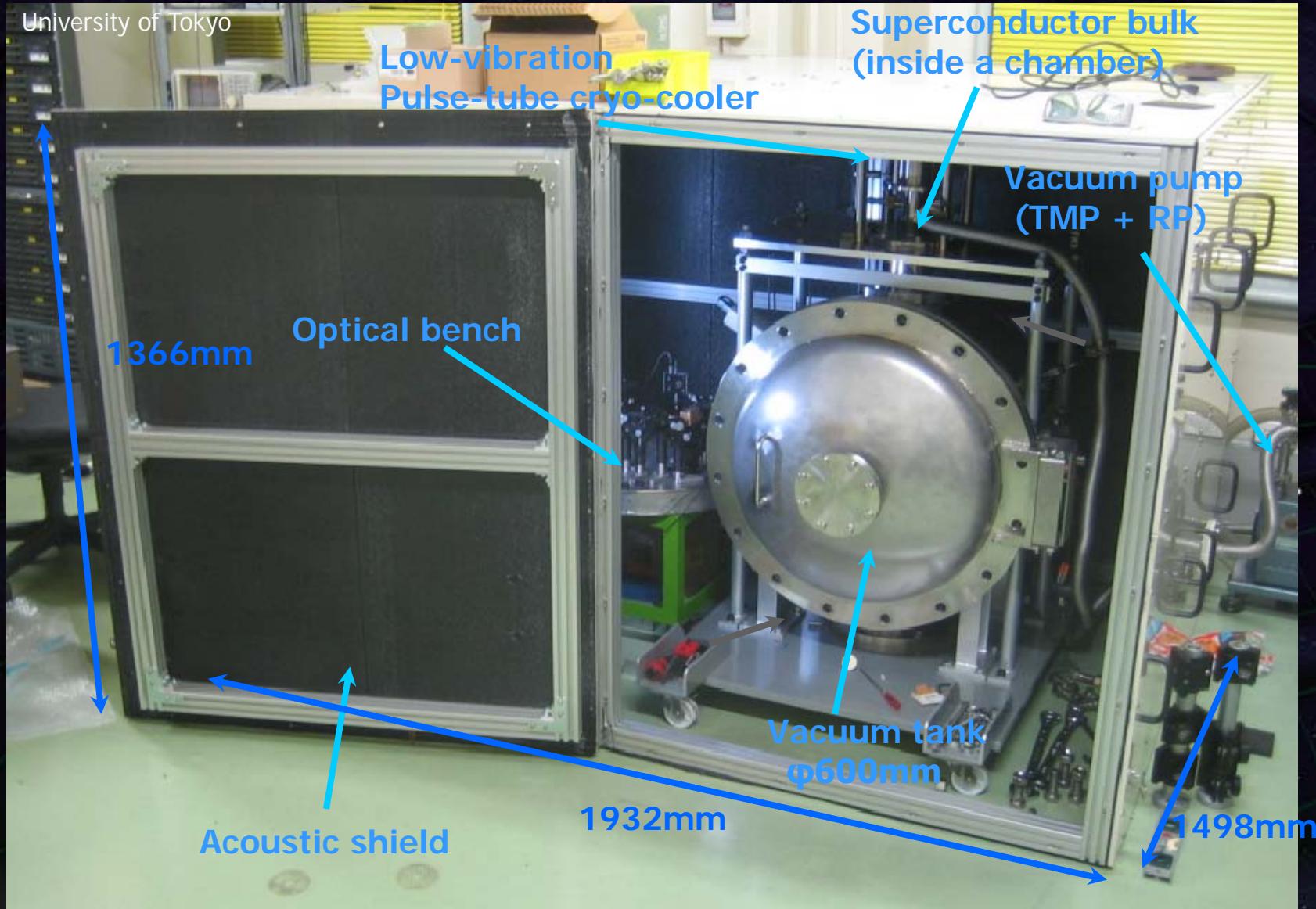
$\text{Gd}_1\text{Ba}_2\text{Cu}_3\text{O}_{6.9}$  : 70.9%  
 $\text{Gd}_2\text{Ba}_1\text{Cu}_1\text{O}_7$  : 19.2%  
 $\phi 600\text{mm}$ , t 20mm,  $T_c \sim 92\text{K}$   
Low-vibration cryo-cooler  
Operation temp. ~65K

- Vacuum system

Pressure  $10^{-5}\text{ Pa}$  by TMP+RP  
Acoustic shield enclosure



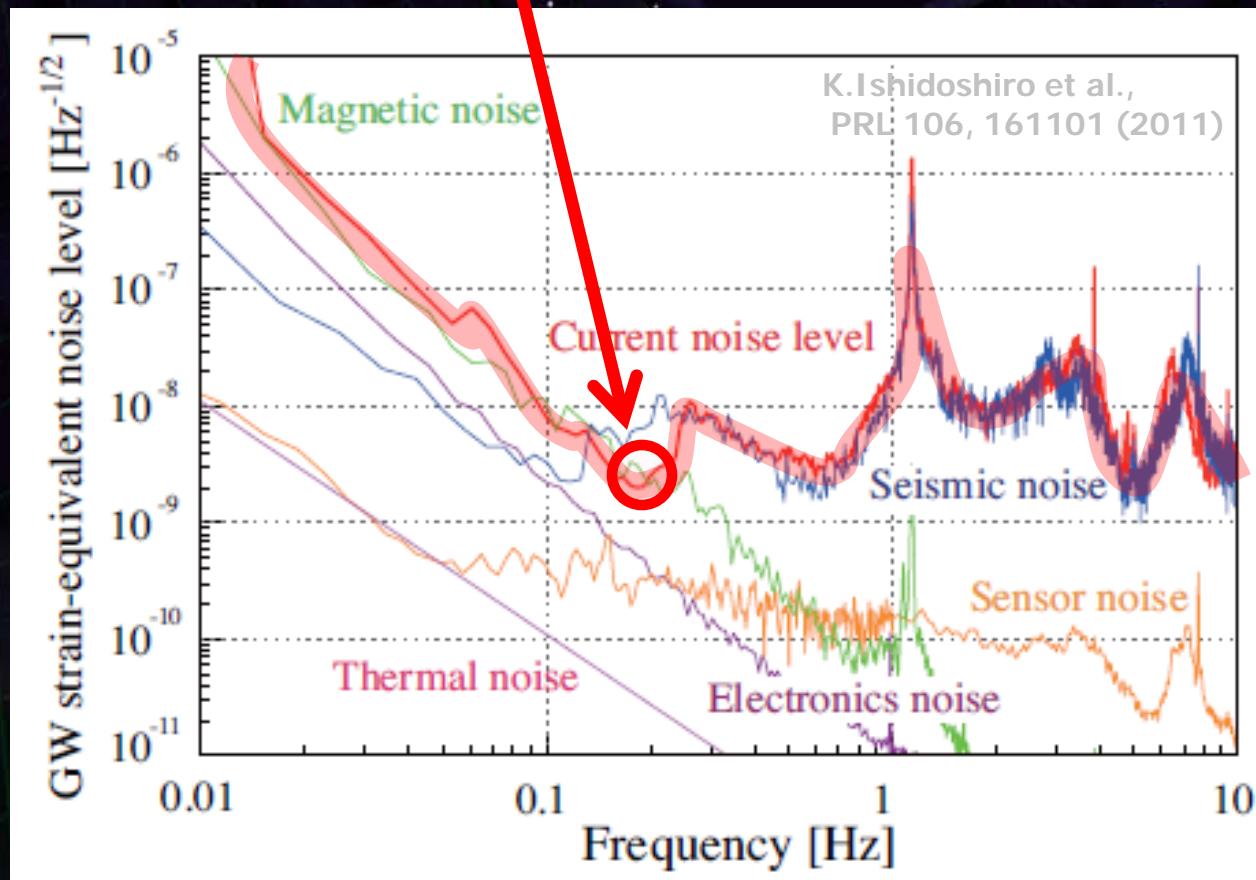
# Small-scale TOBA at Tokyo



# Sensitivity of small TOBA

## Small-scale TOBA at University of Tokyo

Sensitivity  $\tilde{h} \simeq 2 \times 10^{-9}$  [Hz $^{-1/2}$ ] at 0.2Hz



Limited by magnetic disturbances and seismic coupling

# GWB observation by small TOBA

- Observation run by small-scale TOBA at the University of Tokyo  
One-night observation → 7.5 hours' data  
Use stable 3.5 hours' data



- Data analysis for stochastic background GW  
Assume isotropic, unpolarized GWB

GWB energy density ratio

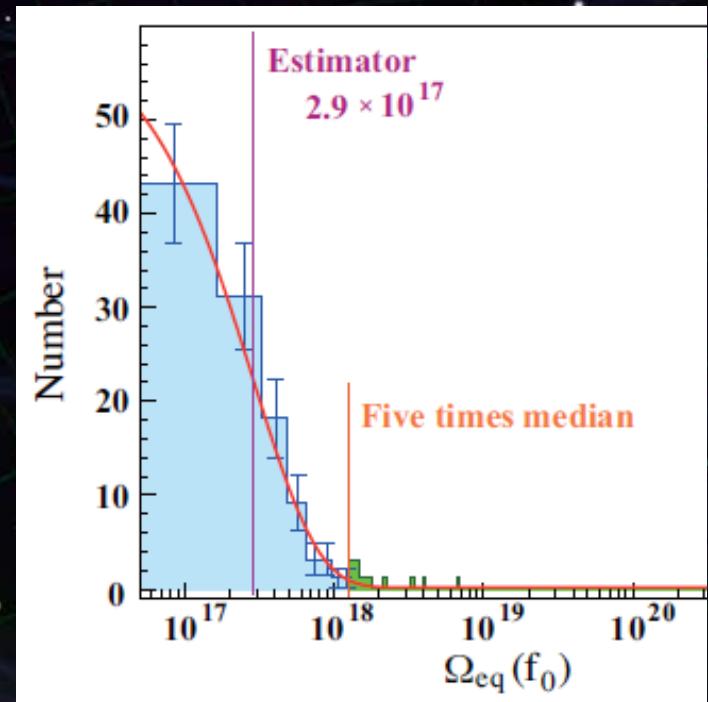
$$\Omega_{\text{eq}}(f_0) = \frac{10\pi^2}{3H_0^2} f_0^3 \tilde{h}^2(f_0)$$

Hubble constant  $H_0 = 70$  [km/s/Mpc]

Divide obs. data into 120 segments

→ Average and distribution

$$f_0 = 0.2 \text{ [Hz]}, \quad f_{\text{BW}} = 0.01 \text{ [Hz]}$$



# Upper limit on GWB

- Distribution → Averaged power at 0.2Hz

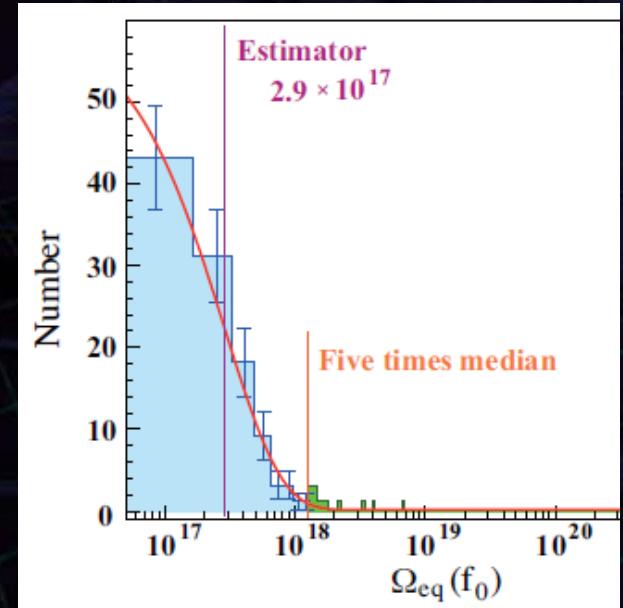
$$\overline{\Omega_{\text{eq}}} = 2.9 \times 10^{17}$$



Upper limit on  $\Omega_{\text{gw}}$

$$\Omega_{\text{gw}}^{\text{UL}} = 4.3 \times 10^{17} \quad (\text{C.L. 95\%})$$

Conservative upper limit including calibration error ( $\delta h/h \sim 10\%$ ) and the other systematic errors.



Some details...

Probability to have larger result than  $\overline{\Omega_{\text{eq}}}$

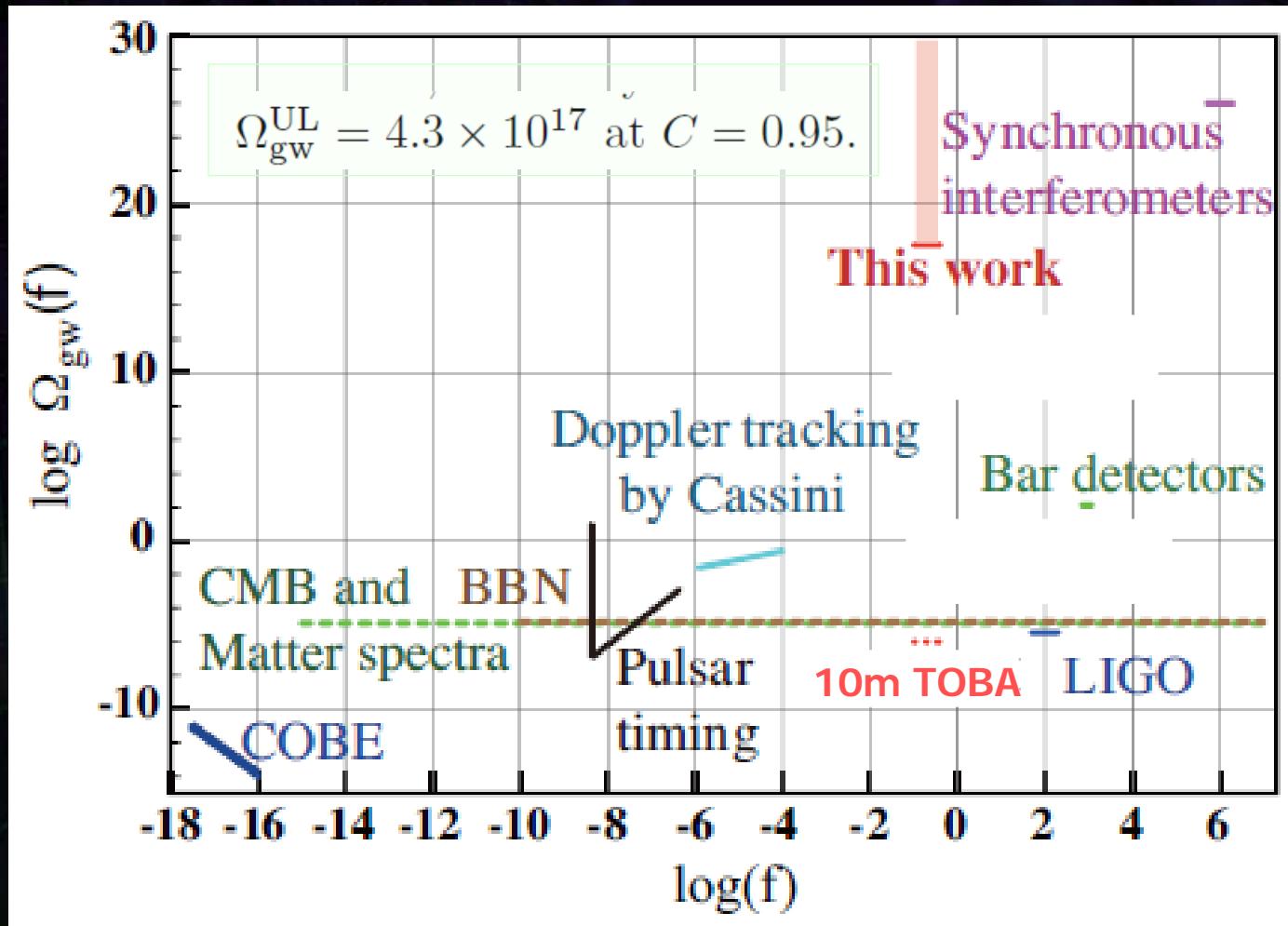
$$C = \int_{\overline{\Omega_{\text{eq}}}}^{\infty} P(\Omega_{\text{es}}|\Omega_{\text{gw}}) d\Omega_{\text{es}}$$

Distribution with  $\Omega_{\text{gw}}$  assuming Gaussian dist.

$$P(\Omega_{\text{es}}|\Omega_{\text{gw}}) \propto \exp \left[ -\frac{(\Omega_{\text{es}} - \Omega_{\text{gw}})^2}{2\Omega_{\text{gw}}^2/N} \right]$$

# Comparison with previous results

New upper limit at unexplored frequency band of 0.2Hz

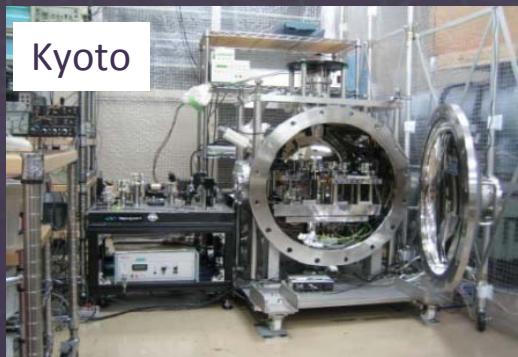


# Observation with two detectors

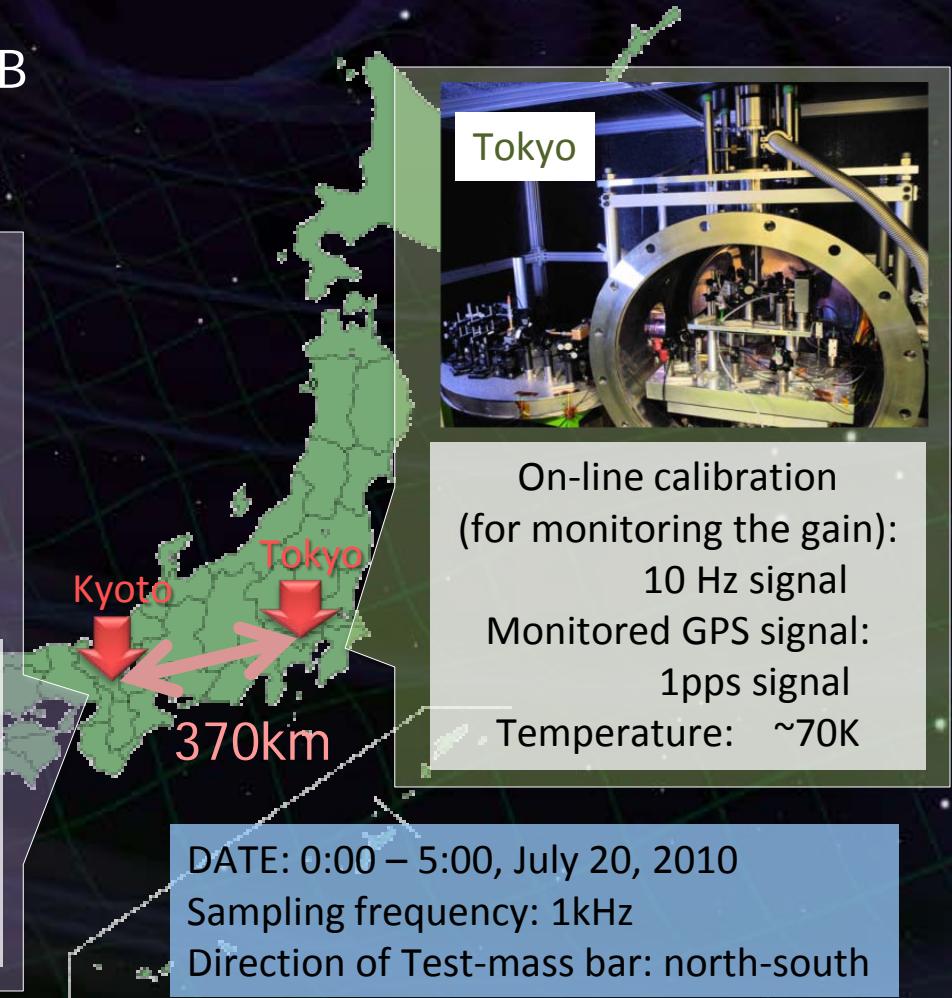
Observation with two detectors places at Tokyo and Kyoto, Japan.

Comparable sensitivity, Separation : 370km

→ Better upper limit on GWB  
Possible detection



On-line calibration  
(for monitoring the gain):  
8.7 Hz signal  
Monitored GPS signal:  
1pps and serial signal  
Temperature: ~40K



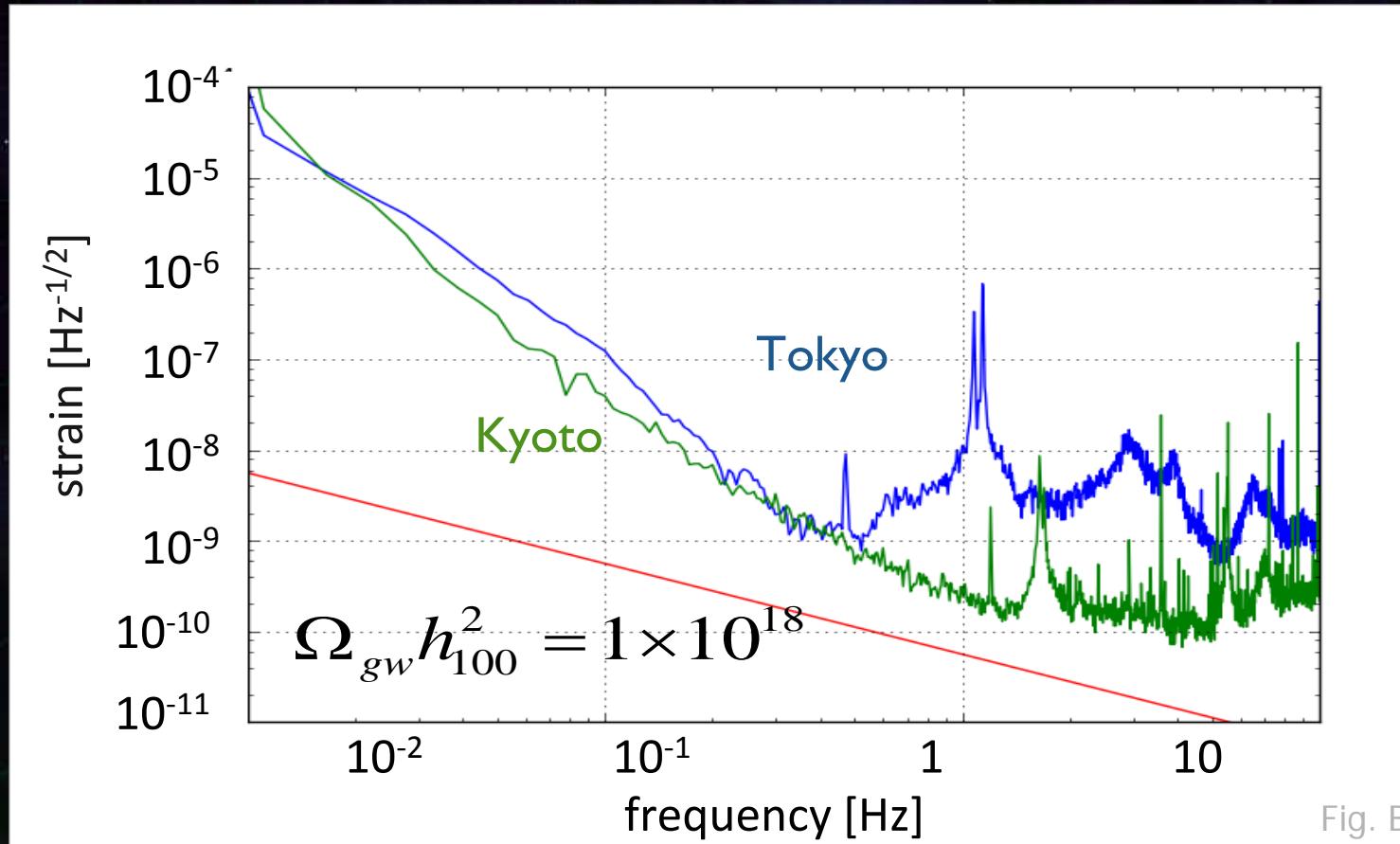
Original fig. by  
A.Shoda  
(GWPAW 2011)

# Sensitivities

One-night observation runs x three times

Data analysis underway  $\rightarrow \Omega_{gw}^{UL} < 9 \times 10^{15}$  is expected

(1/50 better upper limit than that by one detector)

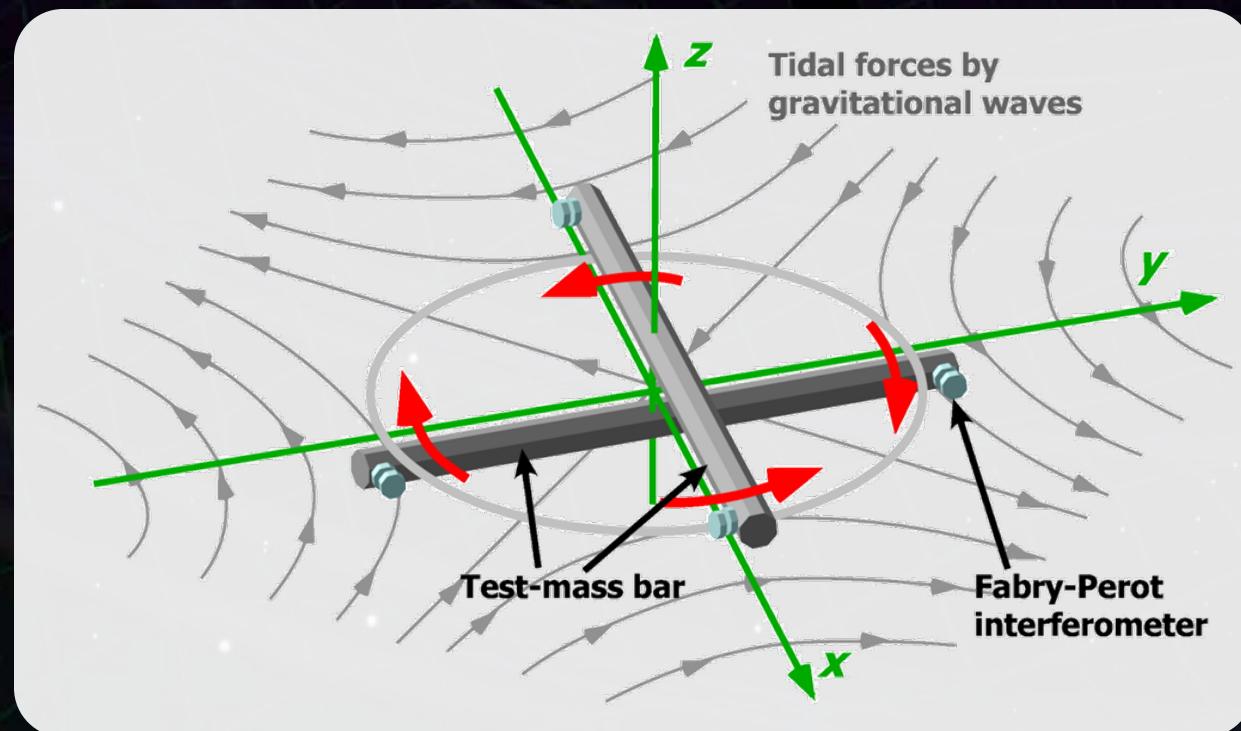


# Rotating TOBA

# Rotating TOBA

Rotate the detector along its axis

- Very low-freq. GW signal ( $\sim 10^{-8} - 10^{-4}$  Hz) is up-converted to 2 x (Rotation freq.)



# Rotating TOBA

Equation of Motion of a test-mass bar

$$I \left( \ddot{\theta} + \frac{\omega_0}{Q} \dot{\theta} + \omega_0^2 \theta \right) = \frac{1}{4} q^{ij} \cdot \ddot{h}_{ij}(t)$$

$I$  : Moment of Inertia  
 $q^{ij}$  : Dynamic quadrupole moment

Rotation  $\Rightarrow$

$$\theta_{\text{diff}} \simeq \alpha \left( \frac{\omega_g}{2\omega_{\text{rot}}} \right)^2 [h_x \cos(2\omega_{\text{rot}}t) + h_+ \sin(2\omega_{\text{rot}}t)],$$

GW with very-low freq. ( $\omega_g$ )  
appears as high freq. ( $2\omega_{\text{rot}}$ ) signal by up-conversion.

Advantage:

- Extract two independent polarization signals.
- Observable at high freq.  $\rightarrow$  easy to avoid low-freq. noises.
- Allow intermitted observation.

# Sensitivity by R-TOBA

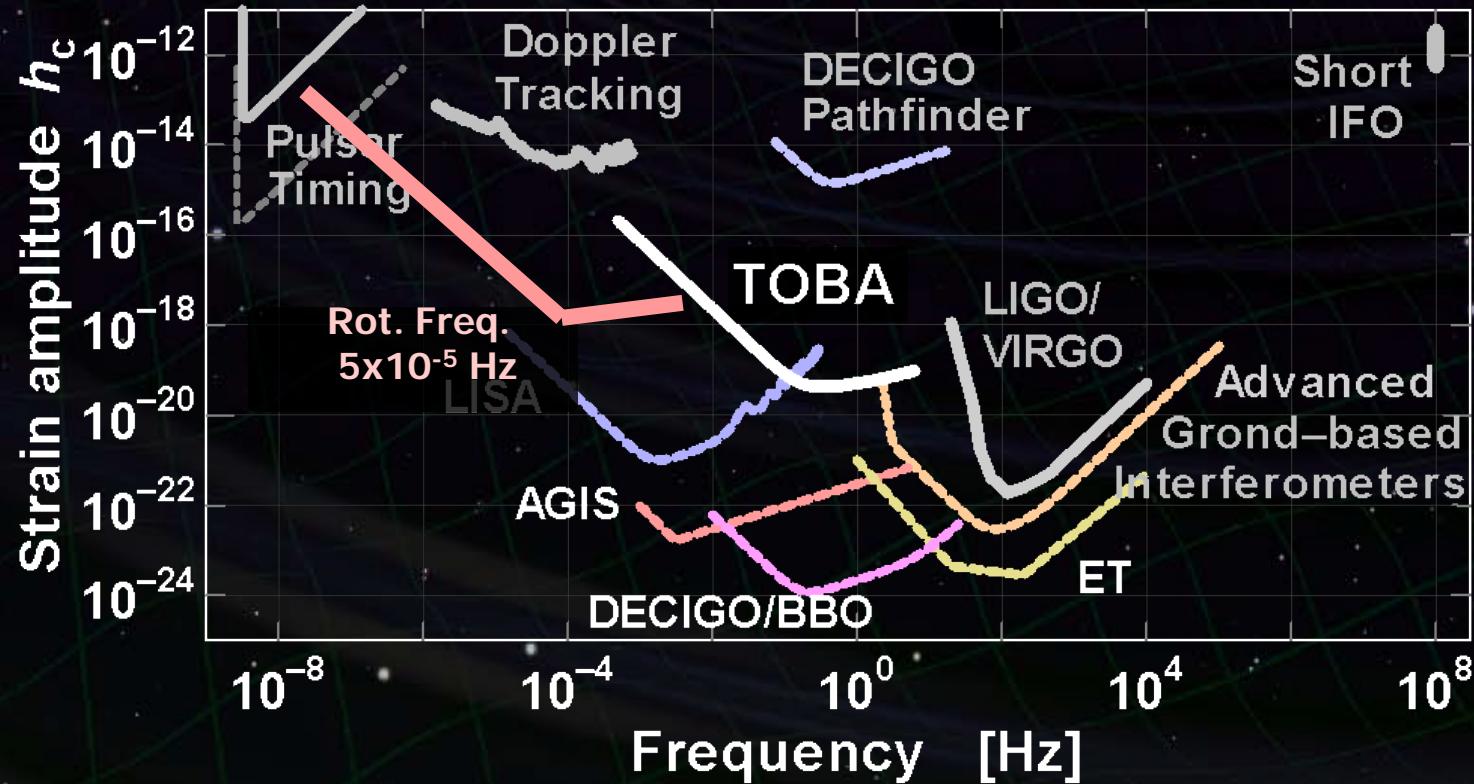
## Sensitivity example

Rotation freq.  $5 \times 10^{-5}$  Hz

Laser power 1mW

⇨ Bridge the Pulsar-timing and LISA bands

Bar length : 10m, Mass : 7600kg  
Laser source : 1064nm, 1mW  
Cavity length : 1cm, Finesse : 1  
Bar Q-value :  $10^5$ , Temp: 4K  
Support Loss :  $10^{-10}$



# Rotating TOBA prototype

( SWIM on SDS-1 satellite )

Reference:

- W. Kokuyama, presentation at GWADW2010

# SWIM $\mu$ v GW sensor

Tiny GW sensor : Test-mass length ~ 50mm

Launch in Jan. 2009, Decommission in Sept. 2010

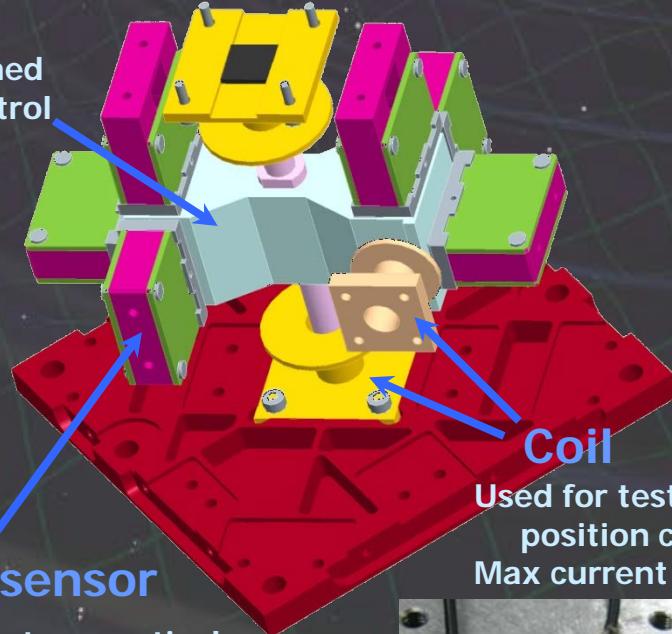
Successful operation and data-taking



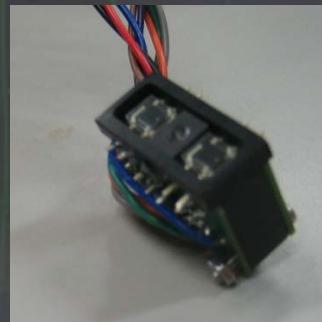
**TAM: Torsion Antenna Module with free-falling test mass**  
(Size : 80mm cube, Weight : ~500g)

## Test mass

~47g Aluminum, Surface polished  
Small magnets for position control



**Photo sensor**  
Used for test-mass position control  
Max current ~100mA



**Photo sensor**  
Reflective-type optical displacement sensor  
Separation to mass ~1mm  
Sensitivity ~  $10^{-9}$  m/Hz $^{1/2}$   
6 PSs to monitor mass motion



# Observation by SWIM

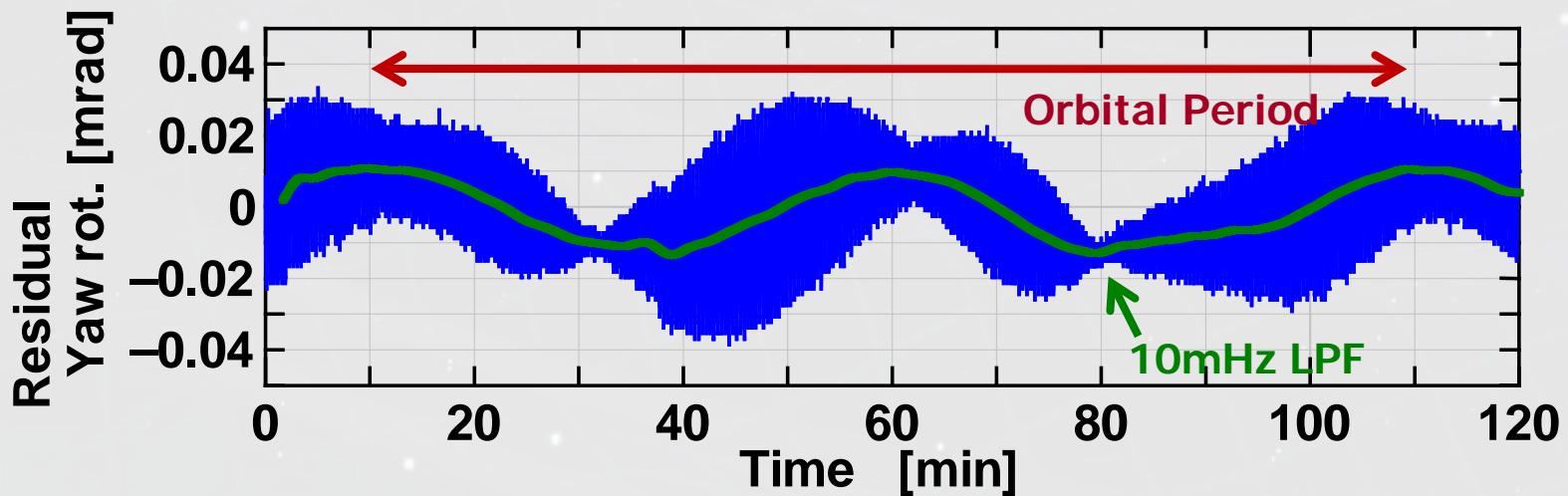
Continuous data taking

Jun 17, 2010 ~120 min.

July 15, 2010 ~240 min.

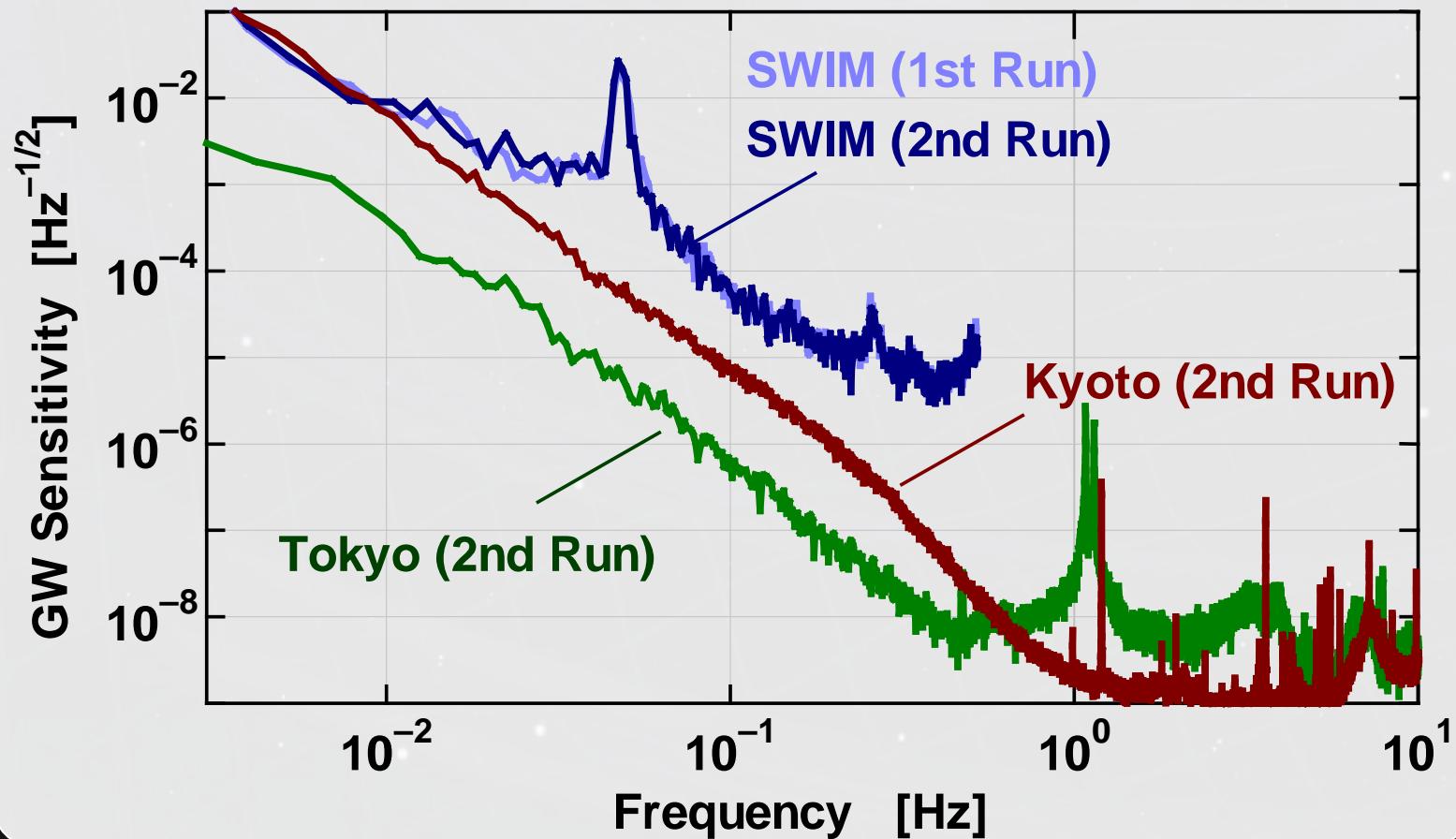
Simultaneous observation  
with ground-based detectors

⇒ Data analysis



# Sensitivity

Observation by SWIM and ground-based detectors  
1<sup>st</sup> run June 17 2010, 2<sup>nd</sup> run July 15 2010



# Summary

# Summary (1/2)

Propose a novel type GW detector : TOBA

→ Low-freq. observation ( $\sim 10^{-8} - 1 \text{ Hz}$ ) .

- Observable Range of 10Gpc for BH binary inspiral with realistic detector parameters.
- Having sensitivity to low-freq. (1mHz-0.1Hz) GWs even with ground-based configuration.
- Rotation operation enables us lower freq. (<1mHz) GWs.
- **Ground-based configuration**  
Simpler and lower-cost detector.  
Reduction of seismic and Newtonian noises is critical.
- **Space-borne mission**  
Free from seismic disturbances.  
Spin spacecraft naturally becomes a rotating TOBA.

# Summary (2/2)

## Ground-based prototype tests

- Single small-scale TOBA with length ~20cm
  - Set a new upper limit at 0.2Hz for GWB.
- Observation run with two separated small-scale TOBA
  - Data analysis in progress.
  - 1/50 better GWB upper limit is expected.

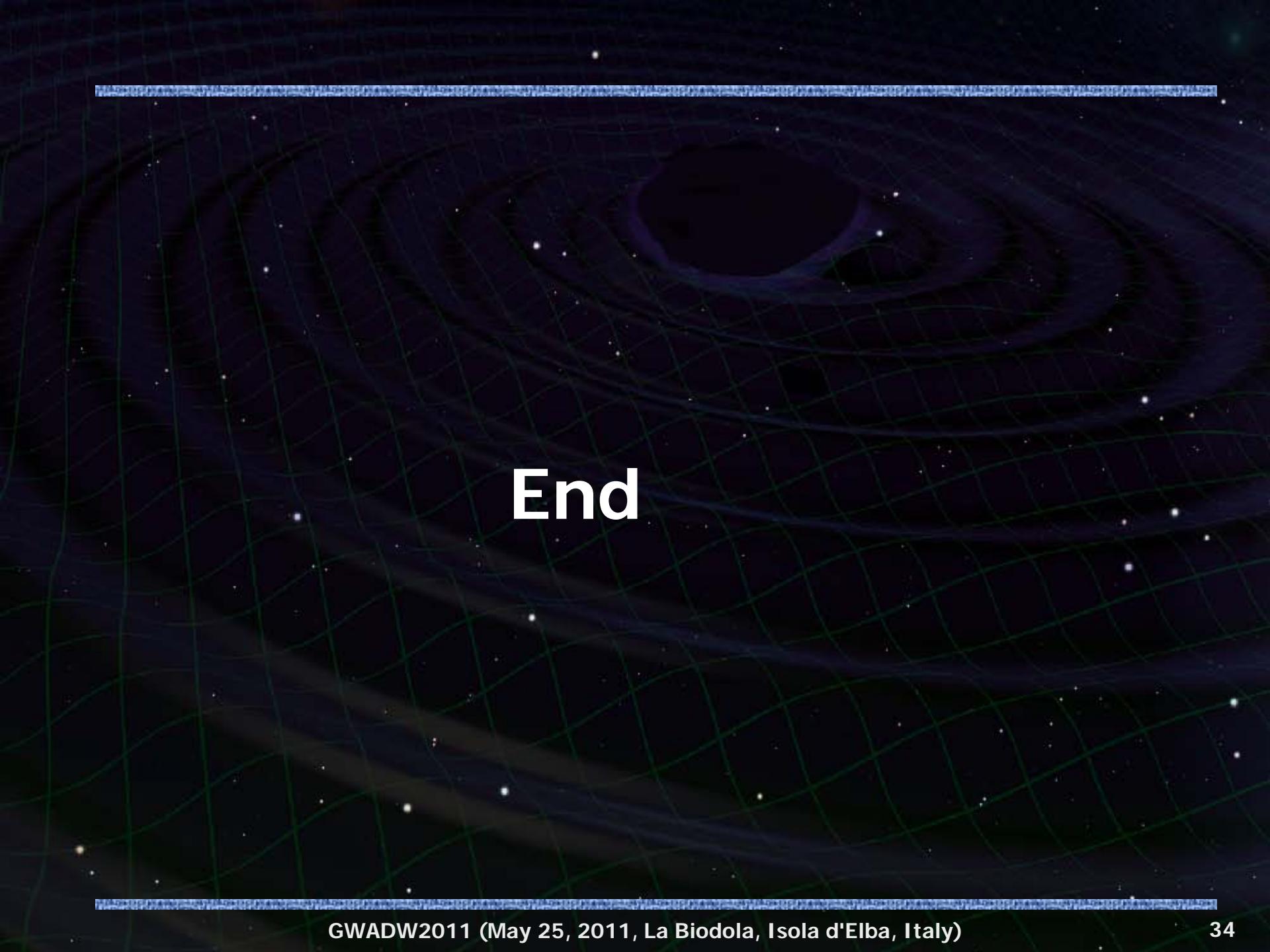
## Prototype in space

- Tiny module named SWIM $\mu$ v, length ~5cm
  - In orbit operation for ~1.5 years.
  - More than 6-hours' observation data.
  - Data analysis in progress.

# Discussions

New motivations for GW research field...

- Optical readout noise
- Low freq. seismic isolation and reduction of Newtonian noise.
- Material, bar shape, and thermal noise
- Cryogenic system
- New possibility as a space mission
- GW sources at different freq. band
  - Between pulsar timing and LISA
  - Between LISA and ground-based detectors
- Data analysis schemes
  - Rotating TOBA configuration
  - Distributed multiple detectors



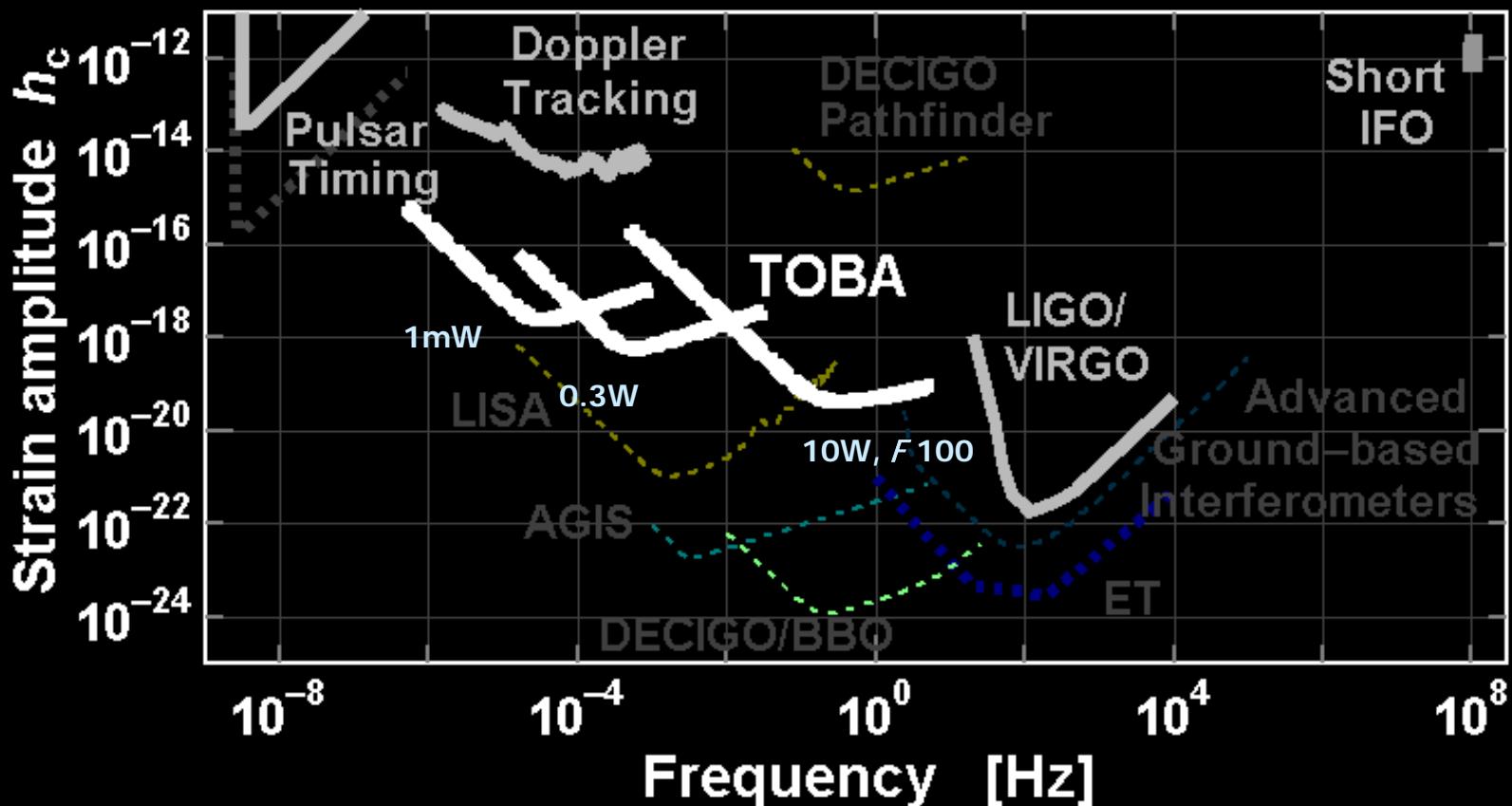
End

# Backups

# TOBA Sensitivity

## Sensitivity example

Bar length : 10m, Mass : 7600kg  
Laser source : 1064nm  
Bar Q-value :  $10^5$ , Temp: 4K  
Support Loss :  $10^{-10}$



# Topic

## Homodyne detection

Ideas of :

Bar rotation by tidal acceleration by GW

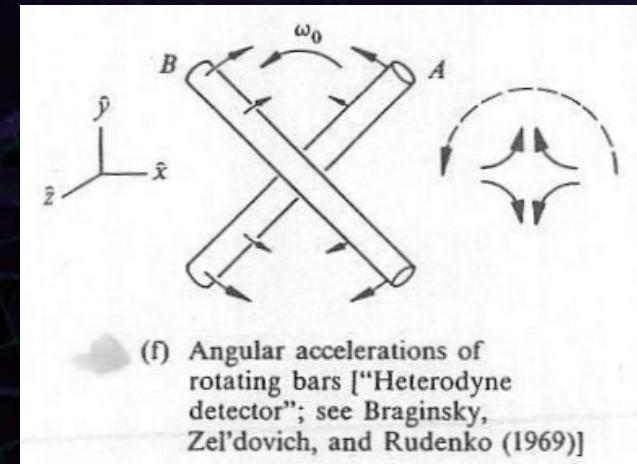
Detection of Circularly polarized GWs

Heterodyne detection method

V.B.Braginsky, Ya.B.Zel'dovich, and V.N.Rudenko  
Sov. Phys.- JETP Lett. 10 (1969) 280.

Being introduced in:

C.W.Misner, K.S.Thorne, J.A.Wheeler,  
'Gravitation' W.H.Freedman (1973) pp.1016.

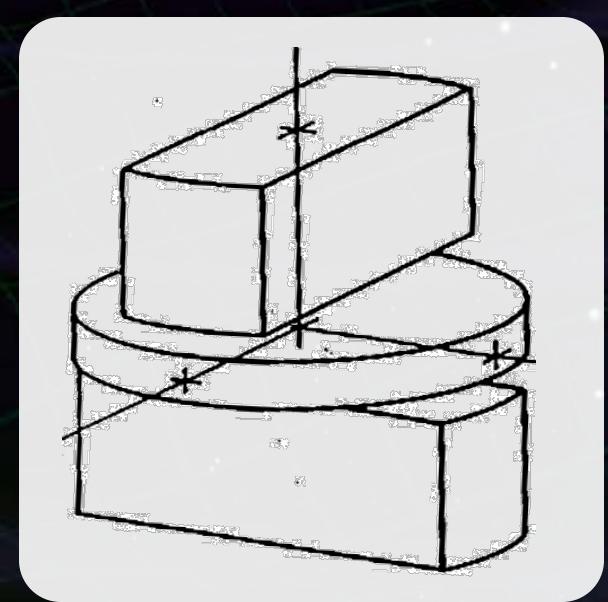


(f) Angular accelerations of rotating bars ["Heterodyne detector"; see Braginsky, Zel'dovich, and Rudenko (1969)]

Observation with torsion antenna :

Cryogenic torsion antenna to observe  
continuous GWs from Grab pulsar

S.Owa, et al.,  
'Cryogenic Detector for Gravitational  
Radiation from the Crab Pulsar'  
Proceedings of the fourth Mercel Grossmann  
Meeting on General Relativity (1986).



# SDS-1衛星での実証

SDS-1 (Small Demonstration Satellite - 1)

JAXA開発による100kg級の技術実証衛星

Size : 70x70x60cm, Weight : 100kg

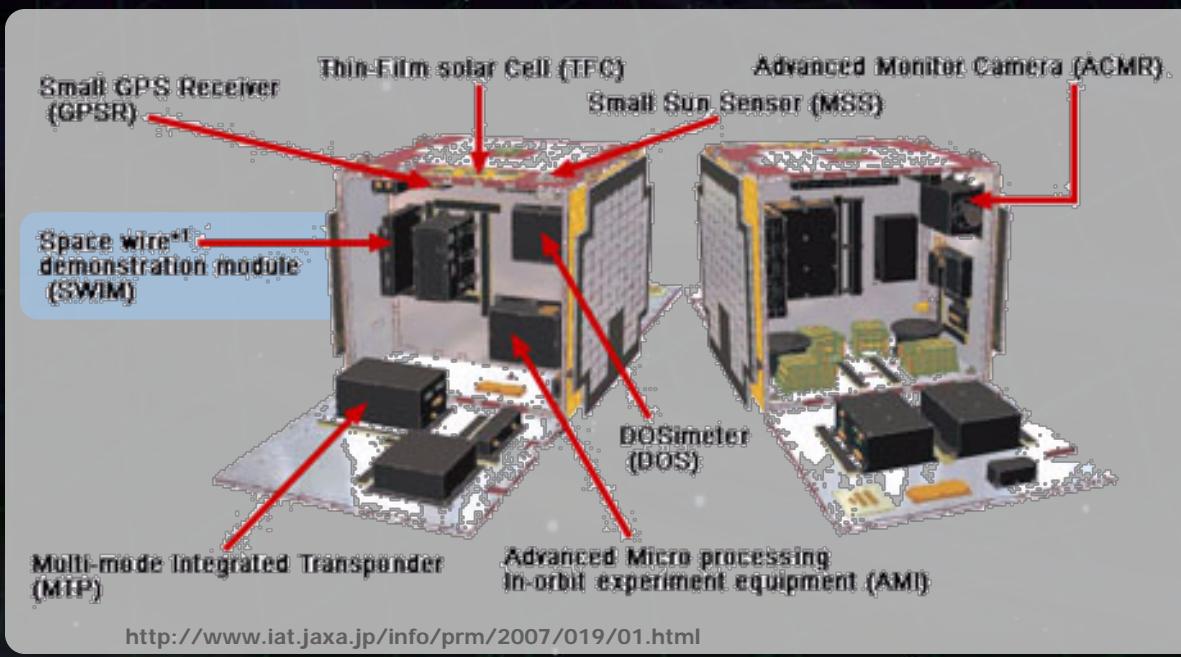
Power : >100W, Downlink : ~5kbps

Orbit : SSO (~660km)

Spin stabilization and 3-axis attitude control

Mission Lifetime : ~Half year (nominal)

SDS-1 and GOSAT  
(Press Release, November 4, 2008)  
Photo from Mainich Newspaper Web



# SDS-1/SWIM

SDS-1/SWIM

2005年 検討・開発開始.

2009年 1月23日打上げ.

2011年 9月 運用停止.

全ての機器で

full success以上を達成.

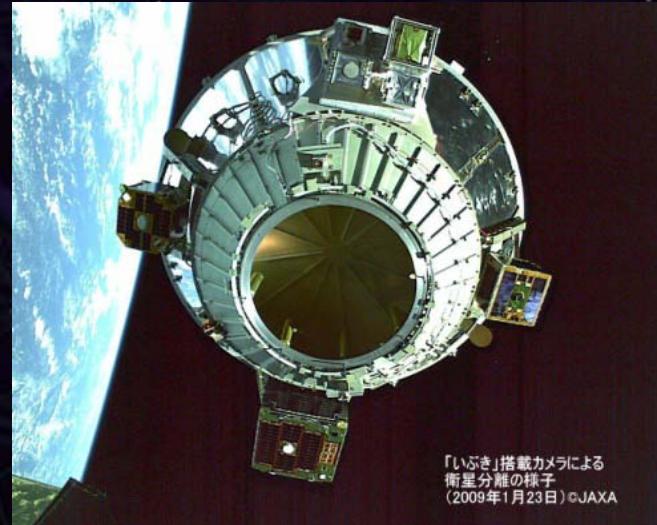


写真:  
JAXA

## SpaceCube2: Space-qualified Computer

CPU: HR5000  
(64bit, 33MHz)

System Memory:  
2MB Flash Memory  
4MB Burst SRAM  
4MB Asynch. SRAM

Data Recorder:  
1GB SDRAM  
1GB Flash Memory  
SpW: 3ch

Size: 71 x 221 x 171

Weight: 1.9 kg

Power: 7W



Photo by JAXA

## SWIM $\mu$ v : User Module

Processor test board.  
GW+Acc. sensor  
FPGA board  
DAC 16bit x 8 ch  
ADC 16bit x 4 ch

→ 32 ch by MPX

Torsion Antenna x2

~47g test mass

Data Rate : 380kbps  
Size: 124 x 224 x 174  
Weight: 3.5 kg  
Power: ~7W



Photo by JAXA

# SWIM $\mu$ v 軌道上実証

SWIM

In-orbit operation

Test mass controlled

Error signal → zero

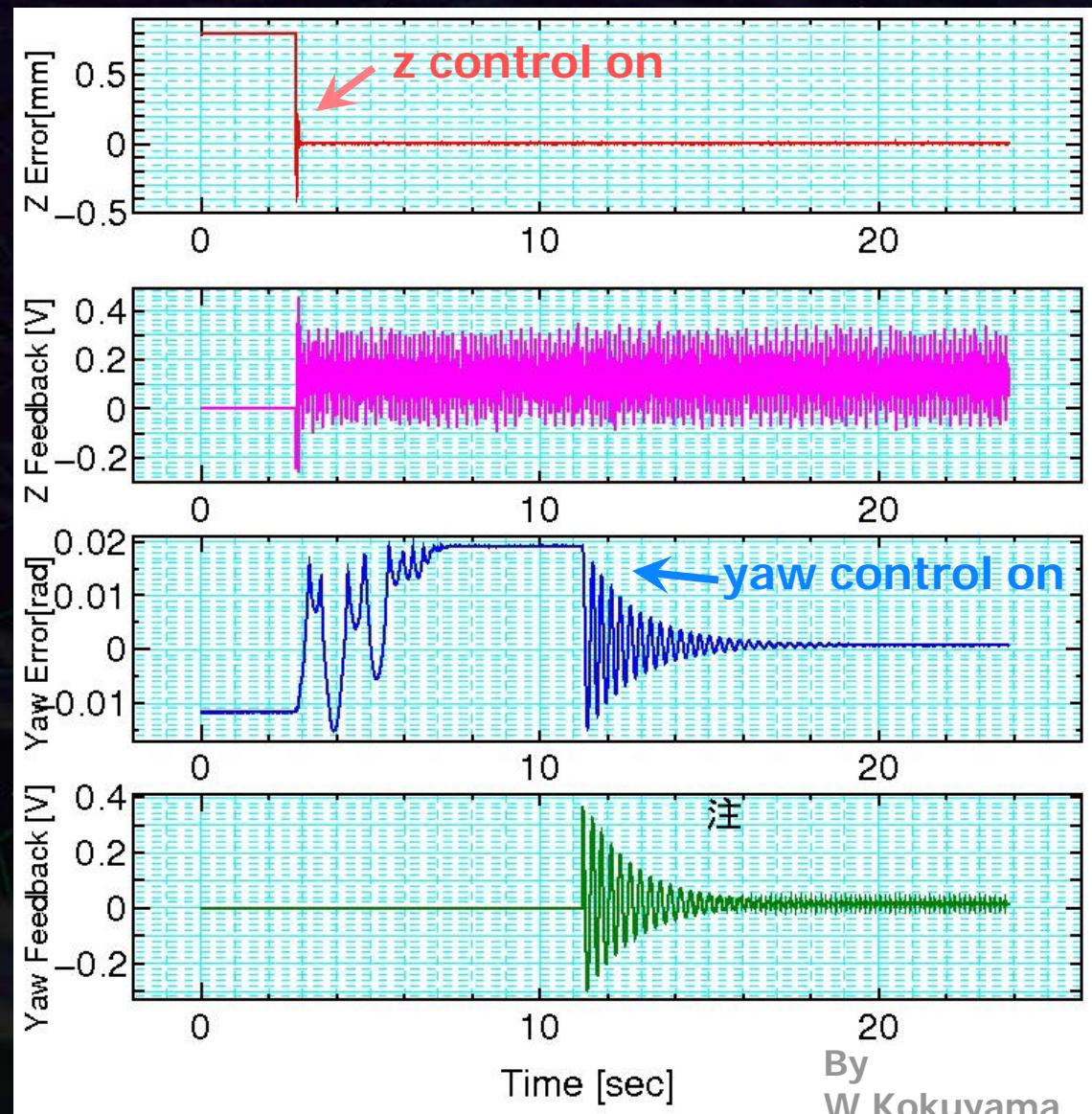
Damped oscillation  
(in pitch DoF)

Free oscillation  
in x and y DoF

Signal injection  
→ OL trans. Fn.

Operation: May 12, 2009

Downlink: ~ a week



By  
W.Kokuyama

# プロトタイプ

2つの地上装置, 1つの衛星搭載モジュール

## ねじれ型重力波検出器A

(地球周回軌道, 2009年-)



試験マス

変動検出

位置・姿勢

## ねじれ型重力波検出器B

(東京大学, 2008年-)



質量 50g, 長さ 5cm

無重力浮上 + 制御

反射型フォトセンサ

スピニ + 軌道運動

## ねじれ型重力波検出器C

(京都大学, 2010年-)



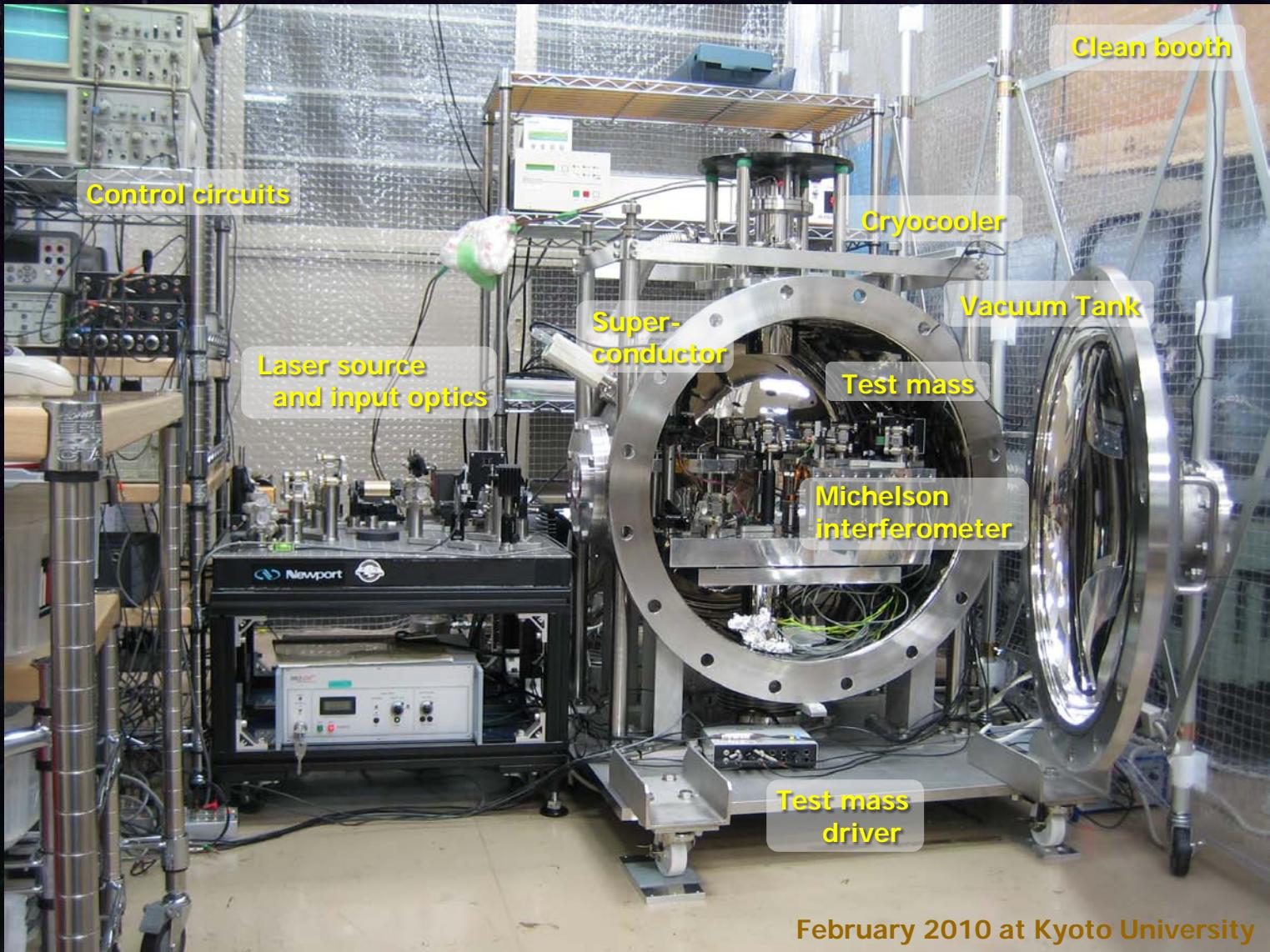
質量 340g, 長さ 25cm

超電導磁気浮上 + 制御

レーザー干渉計

地上静置観測

# Small-scale TOBA at Kyoto



# Observation with two detectors

1台の観測では、背景重力波の検出は極めて困難。

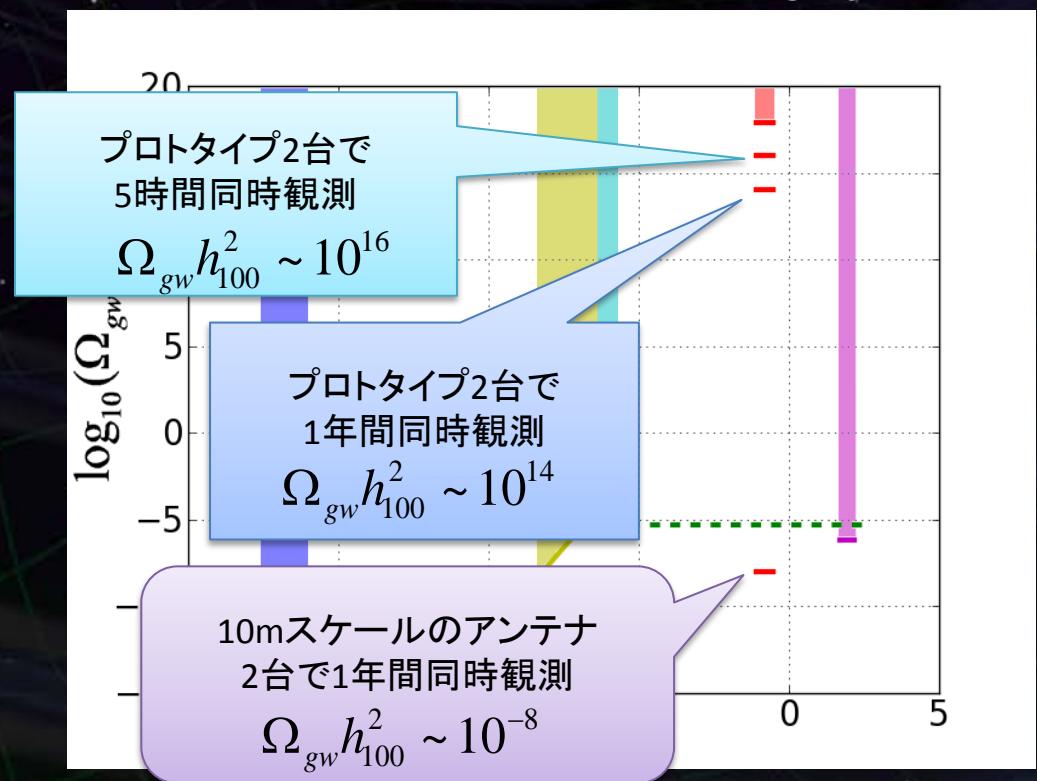
検出器の雑音と背景重力波を区別できない。

Fig. By A.Shoda

複数台での  
同時観測、相関解析を行う。  
信号と雑音を区別できる。  
感度を向上できる。

$$\sqrt{T_{\text{obs}} \Delta f_{\text{obs}}}$$

程度の向上。



# 結果の見通し

観測データ (2010年7月) 解析の暫定結果.

