

**LIGO-G1100039**

**Test of scalar-tensor gravity theory from  
observations of gravitational wave bursts  
with advanced detector network**

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# Search for scalar gravitational waves



- **Testing relativistic gravity theory** is important for fundamental physics and cosmology e.g. dark matter, dark energy, accelerating the Universe.
- One of plausible gravity theories is **scalar-tensor theory**. Significant difference from the general relativity is the existence of a scalar field which is connected with the gravity field with coupling parameters, and a resulting **scalar gravitational wave**. **Brans-Dicke theory** is famous scalar-tensor theory which has a coupling parameter  $\omega_{BD}$ .
- **Tensor GW** search might miss some type of sources, e.g. highly spherical core collapse if scalar-tensor theory is correct. In this sense, search for **SGW** is complementary to current **GW** search.
- This talk will focus on search for **SGW** from **Galactic spherical core collapses in Brans-Dicke theory**.

# Antenna pattern for scalar mode



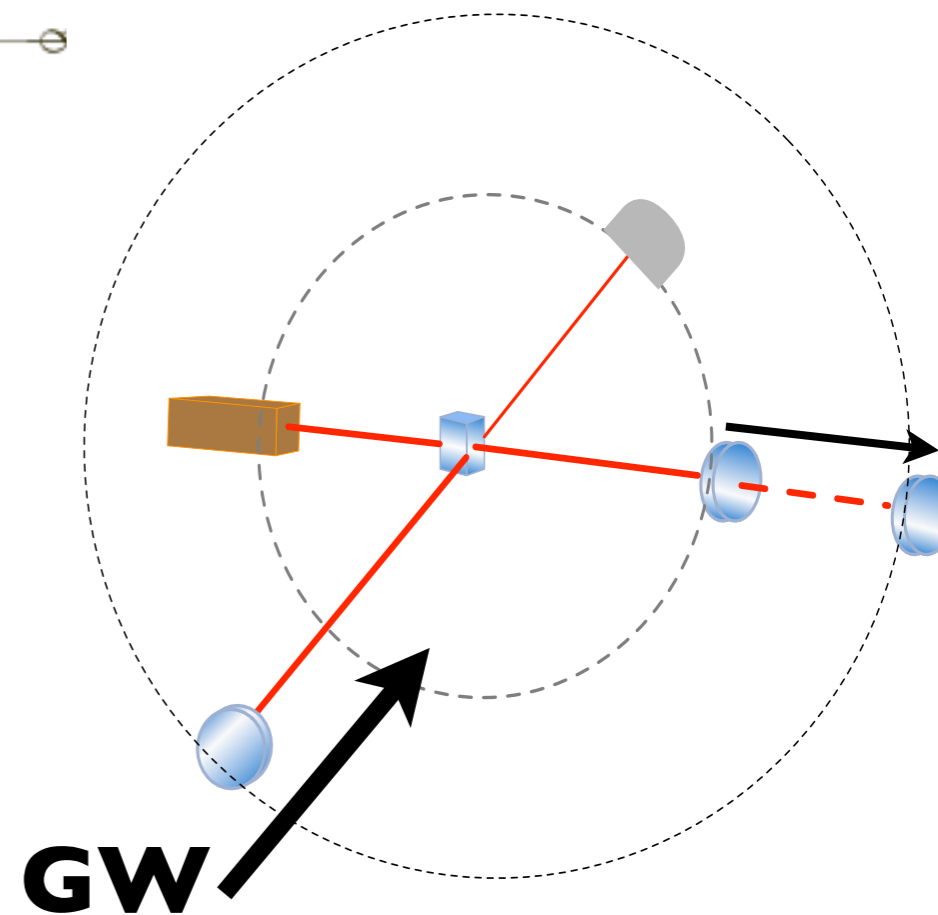
Antenna pattern function as a function of sky position  $(\theta, \Phi)$  is written as

$$F_+(\hat{\Omega}) = \frac{1}{2}(1 + \cos^2 \theta) \cos 2\phi$$

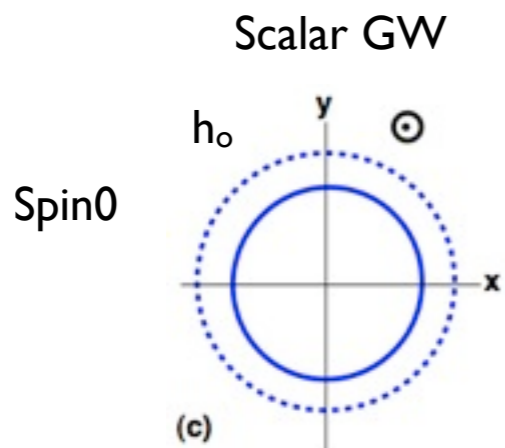
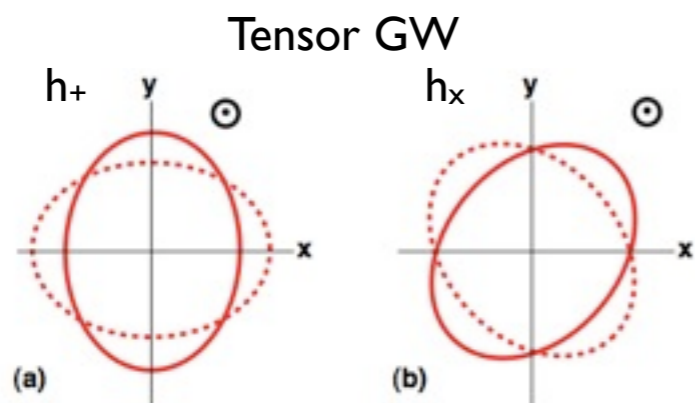
$$F_\times(\hat{\Omega}) = \cos \theta \sin 2\phi$$

$$F_o(\hat{\Omega}) = -\sin^2 \theta \cos 2\phi.$$

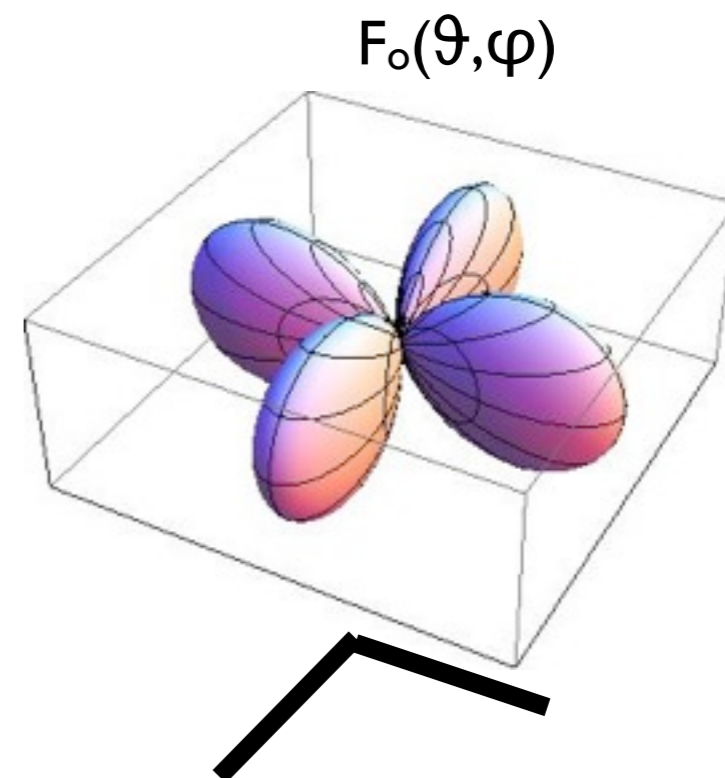
M.Tobar et al(1999), M. Maggiore et al(2000), K.Nakao et al(2001)



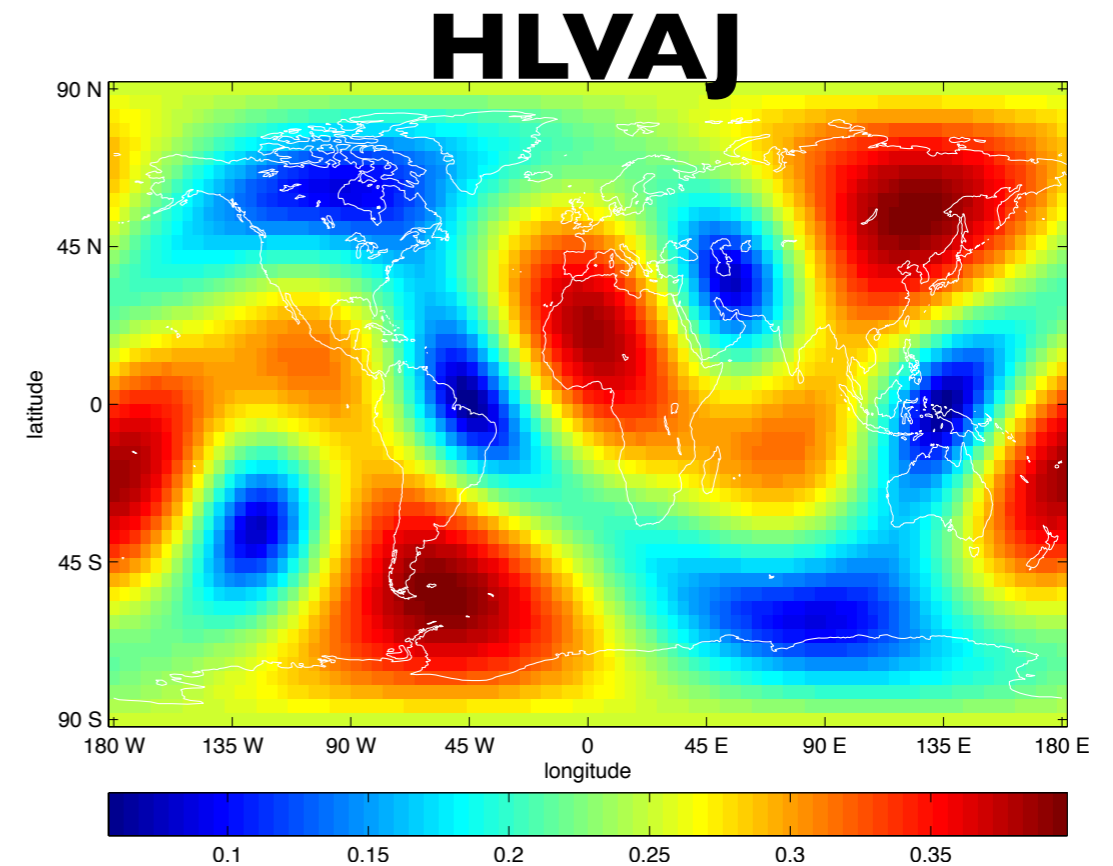
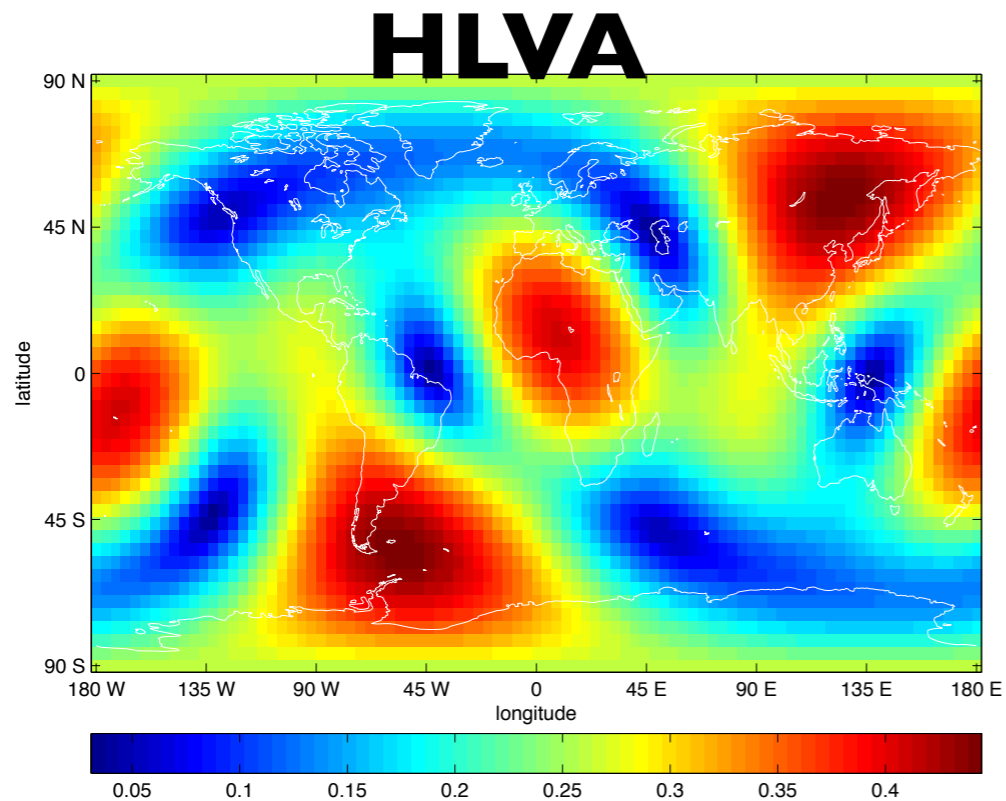
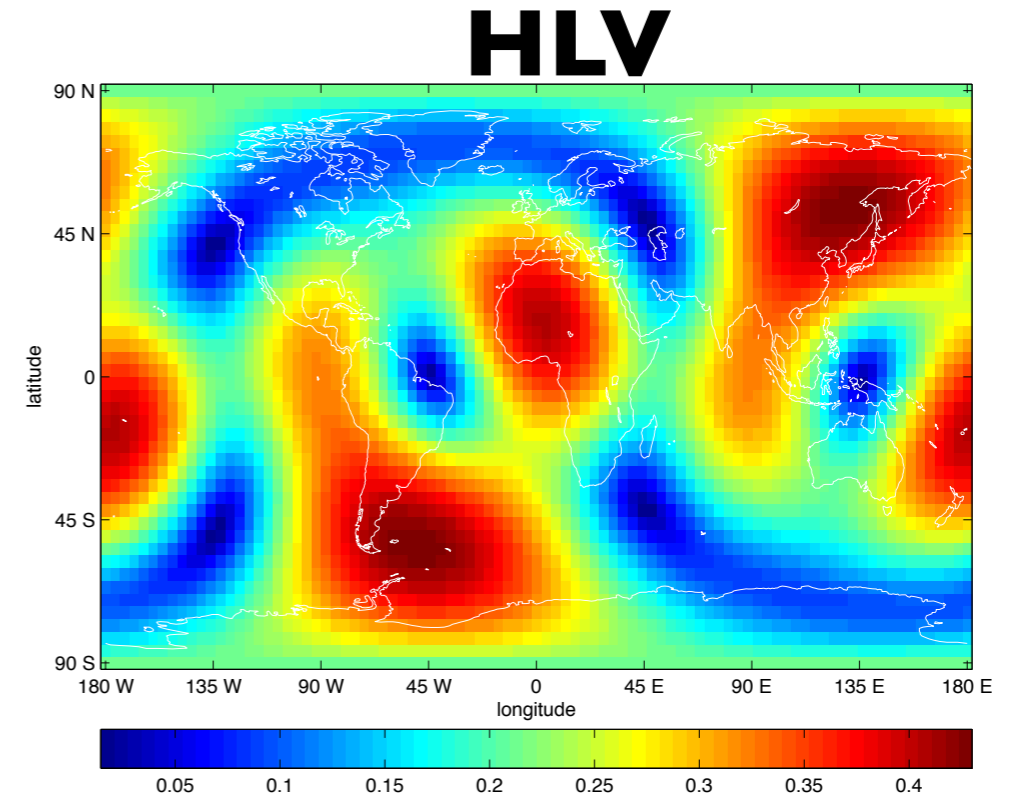
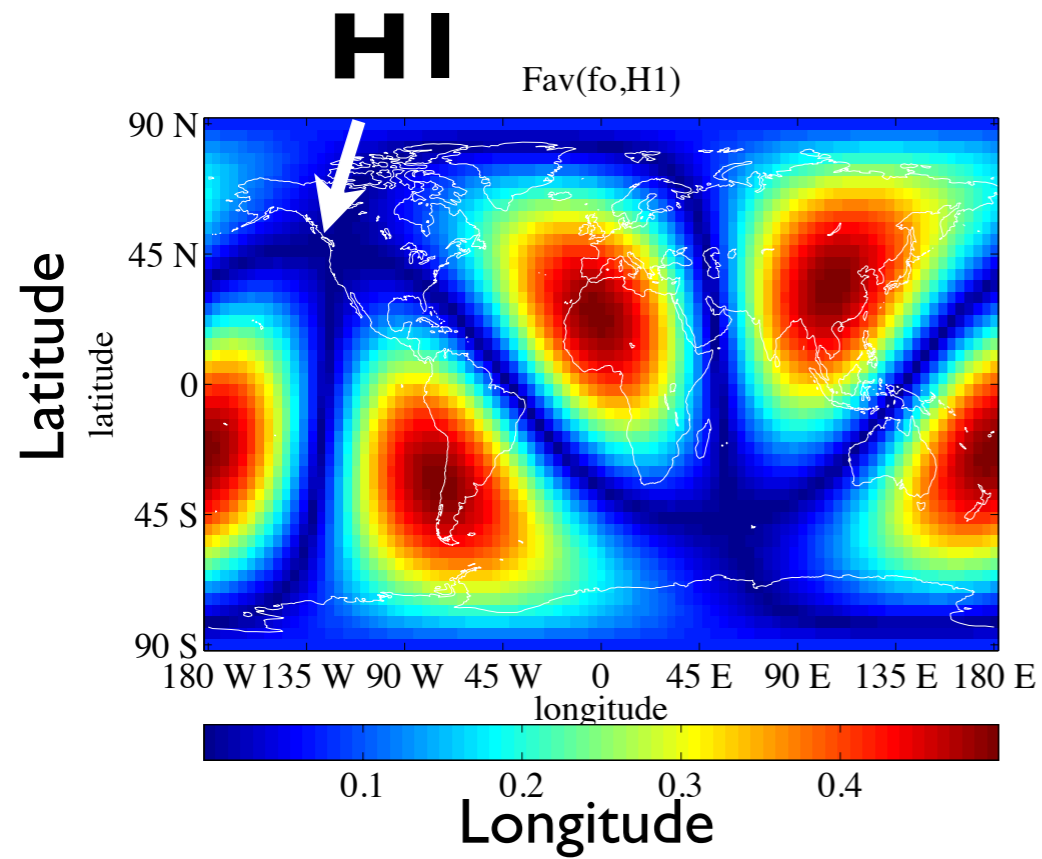
Polarization of tensor, scalar gravitational wave



C.Will, Living Review (2006)



# Antenna pattern sky-map of scalar mode



# Coherent network analysis



- Coherent network analysis can extract scalar gravitational wave with more than 3 world-wide detectors. This approach combines data taking account of the sky position  $(\vartheta, \varphi)$ , arrival time difference  $\tau(\vartheta, \varphi)$  coherently, and calculates all polarization components at a certain direction of the sky which is most likely.**

## Mathematical expression of the coherent network analysis

Expression of d-detectors can be taken as

$$\begin{bmatrix} x_1 \\ \vdots \\ x_d \end{bmatrix} = \begin{bmatrix} F_{1+} & F_{1\times} & F_{1\circ} \\ \vdots & \vdots & \vdots \\ F_{d+} & F_{d\times} & F_{d\circ} \end{bmatrix} \begin{bmatrix} h_+ \\ h_\times \\ h_\circ \end{bmatrix} + \begin{bmatrix} n_1 \\ \vdots \\ n_d \end{bmatrix}$$

The reconstruction of a gravitational wave is an inverse problem.

Maximum likelihood method to solve the inverse problem:

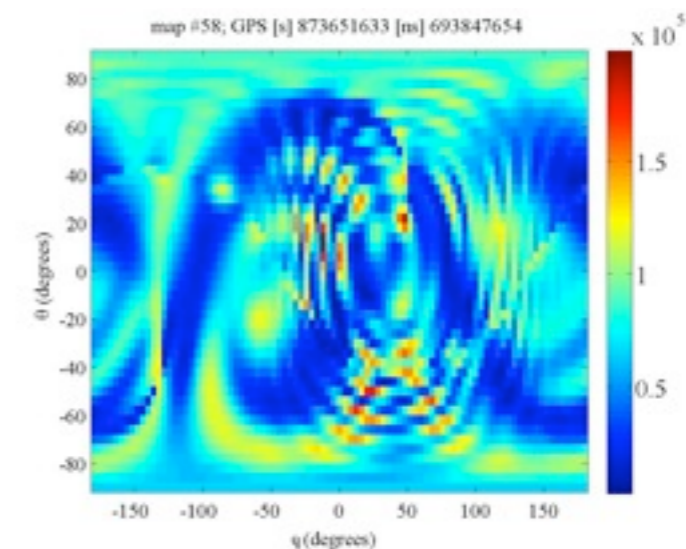
$$L[\mathbf{h}] := \|\mathbf{x} - \mathbf{F}\mathbf{h}\|^2$$

Changing sky position  $(\vartheta, \varphi)$ , time difference  $\tau(\vartheta, \varphi)$ .

The mathematical formula of the reconstructed scalar gravitational wave is

$$\begin{aligned} h_\circ &= \frac{1}{\det(\mathbf{M})} \left( ((F_+ \times F_\times) \cdot (F_\times \times F_\circ)) \cdot F_+ \right. \\ &\quad - ((F_+ \times F_\times) \cdot (F_+ \times F_\circ)) \cdot F_\times \\ &\quad \left. + ((F_+ \times F_\times) \cdot (F_+ \times F_\times)) \cdot F_\circ \right) \cdot \mathbf{x} \end{aligned}$$

Likelihood residual sky-map



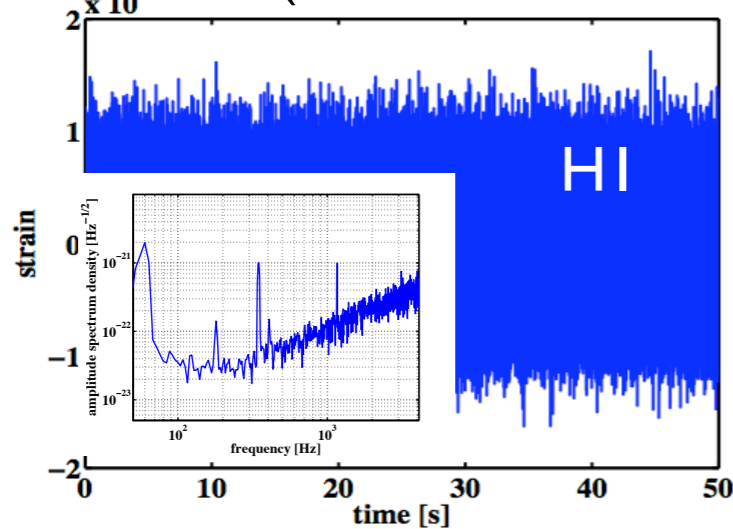


# Scalar pipeline

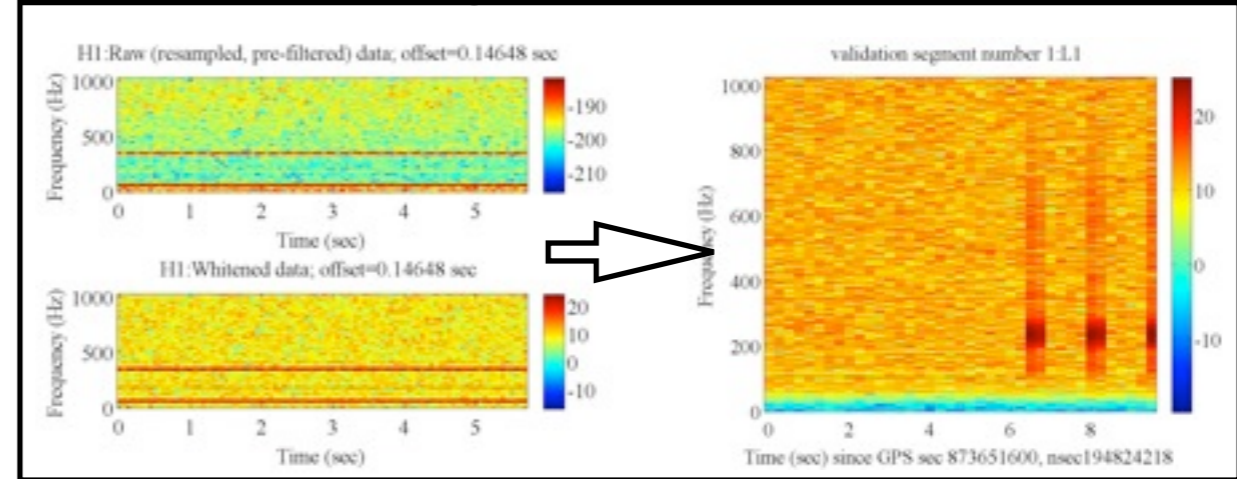


- **Full featured coherent network analysis pipeline(Data conditioning, detection stat., Veto analysis)**
- **One can apply the pipeline to HI,LI,VI,AI,LCGT**
- **Analysis result is output by a Web-based event display.**

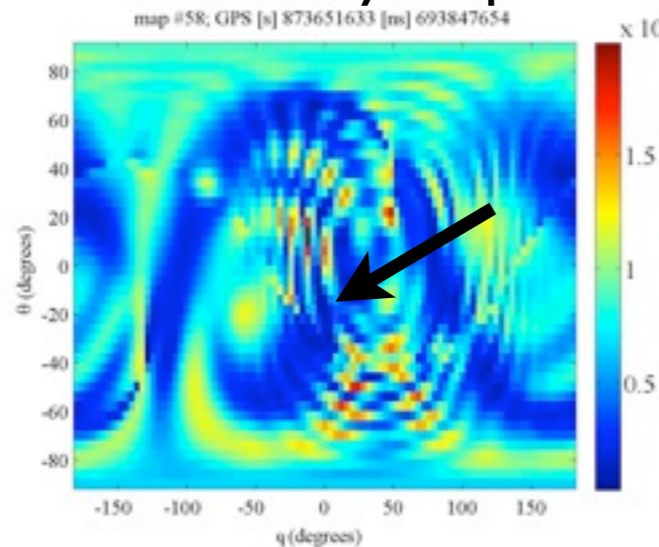
Data set (HI,LI,VI,AI,LCGT)



Data conditioning

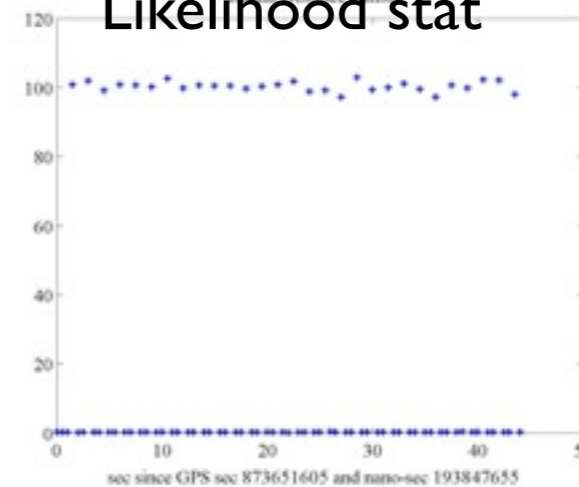


Residual sky-map



Coherent network analysis

Likelihood stat

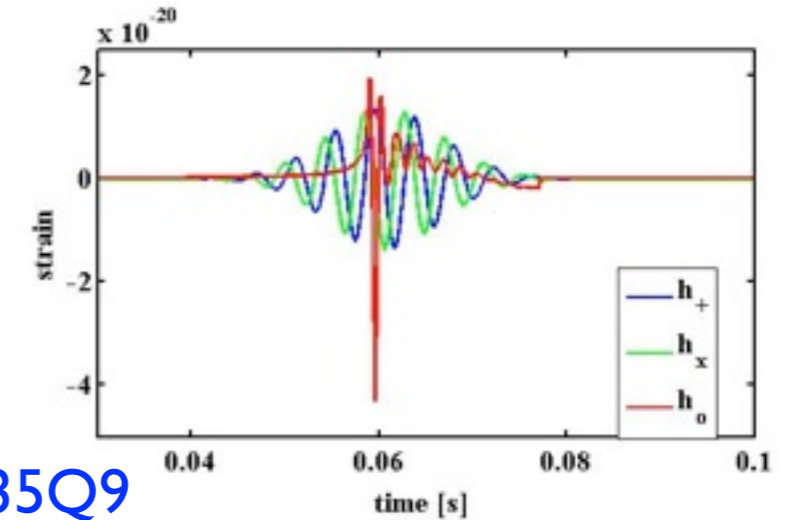


# Demonstration of pol. reconstruction



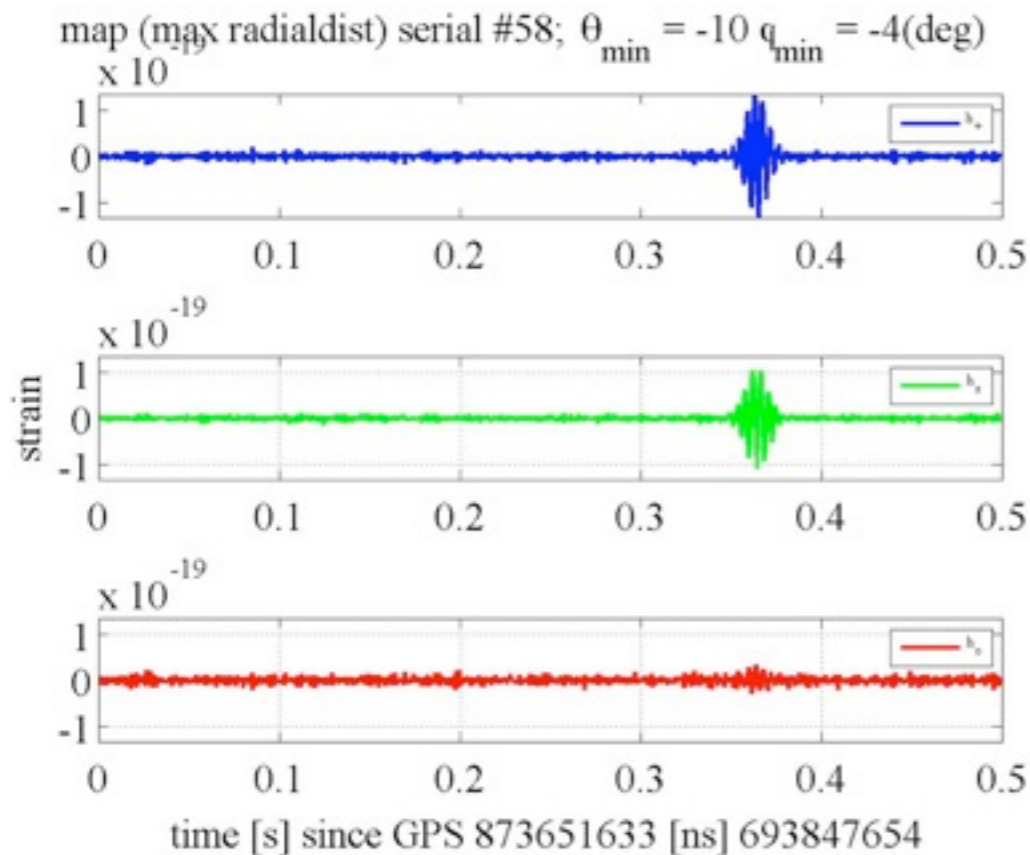
## Reconstruction of $h_+$ , $h_x$ , $h_o$

- As to injection signal, to see  $h_o$  clearly, I used spike-like burst as  $h_o$ .
- Although the grid of lat-lon map is coarse ( $4^\circ \times 4^\circ$ ) in the simulation,  $h_o$  is reconstructed clearly.



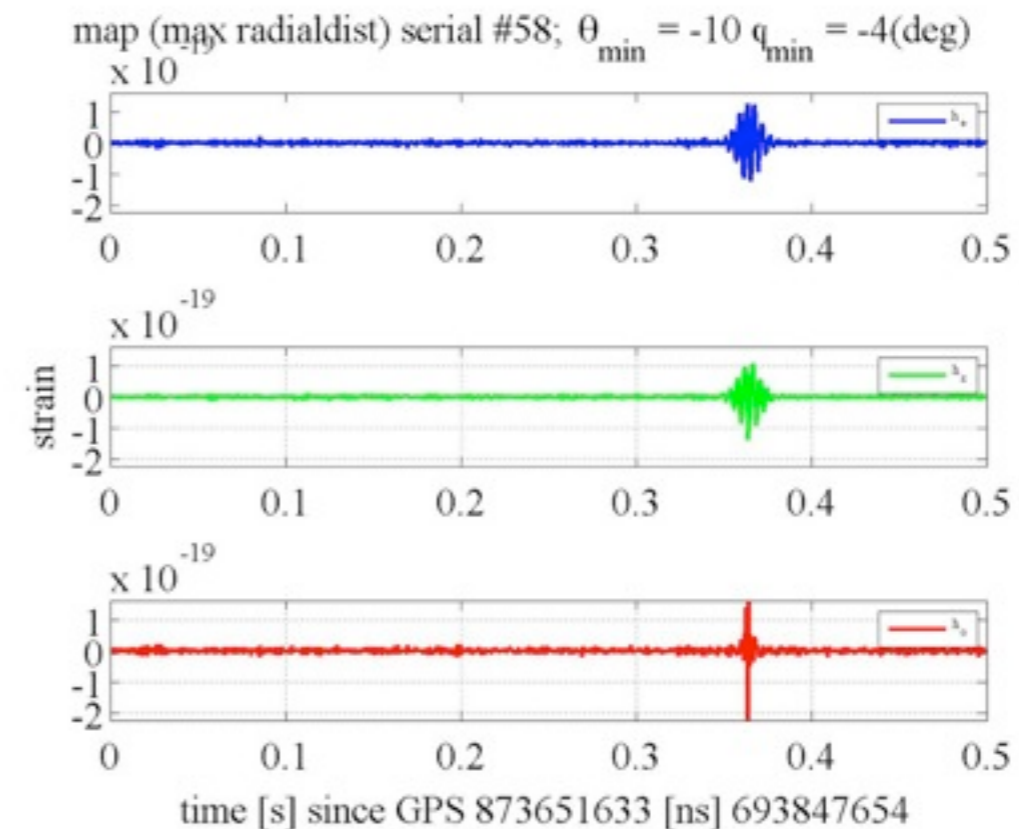
$h_+$ ,  $h_x$  : SG235Q9

$h_o$  : Not injected



$h_+$ ,  $h_x$  : SG235Q9

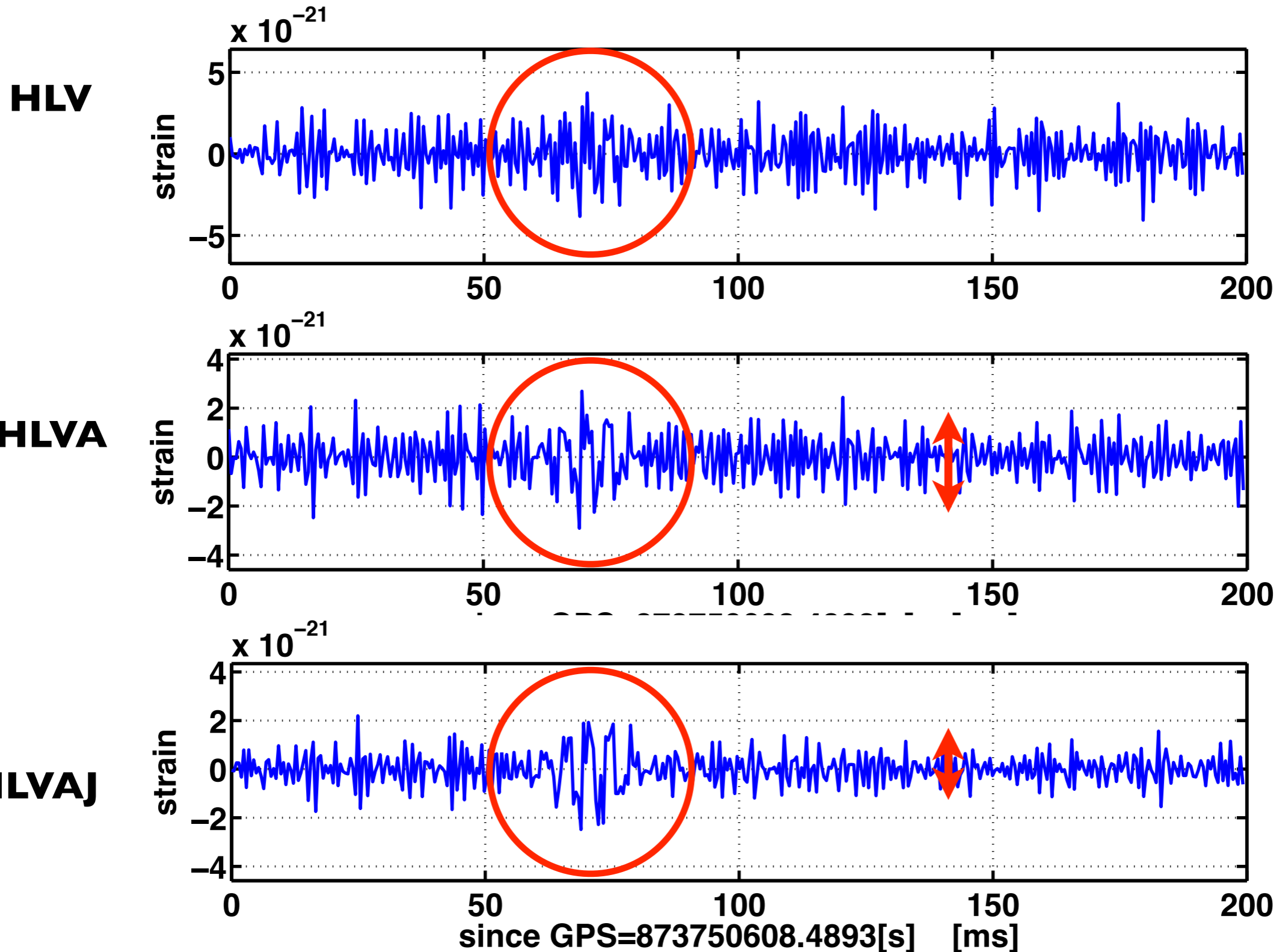
$h_o$  : Spike-like burst



# Reconstructed scalar GW



- Astrophysical model used is a spherically symmetric core collapse with 10Mo at the distance of 10kpc from the earth.(M.Sibata, 1994)

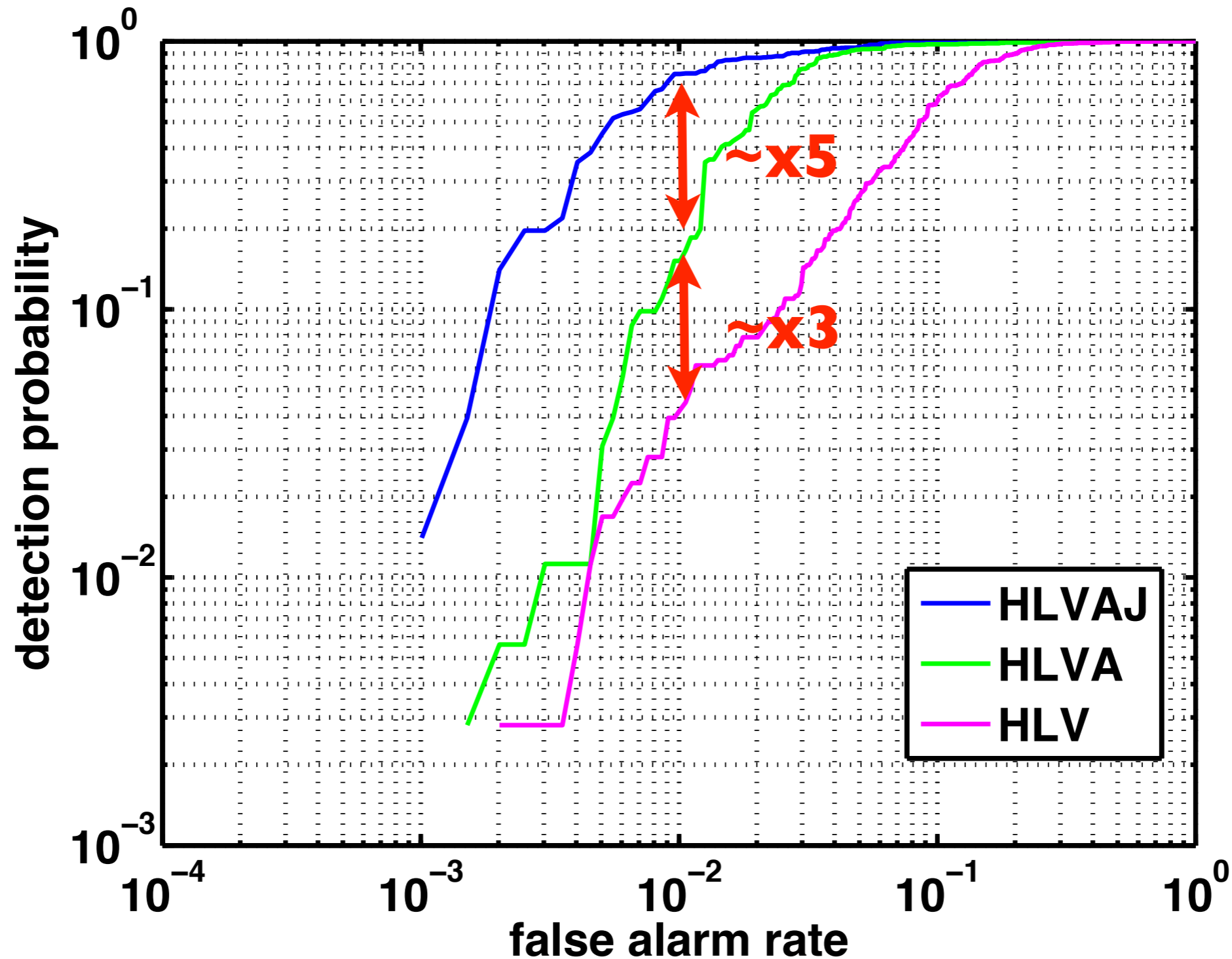




# ROC curve for adv. networks



- Simulated GWs is from spherical core collapse at 10kpc. Sky directions are uniformly distributed.



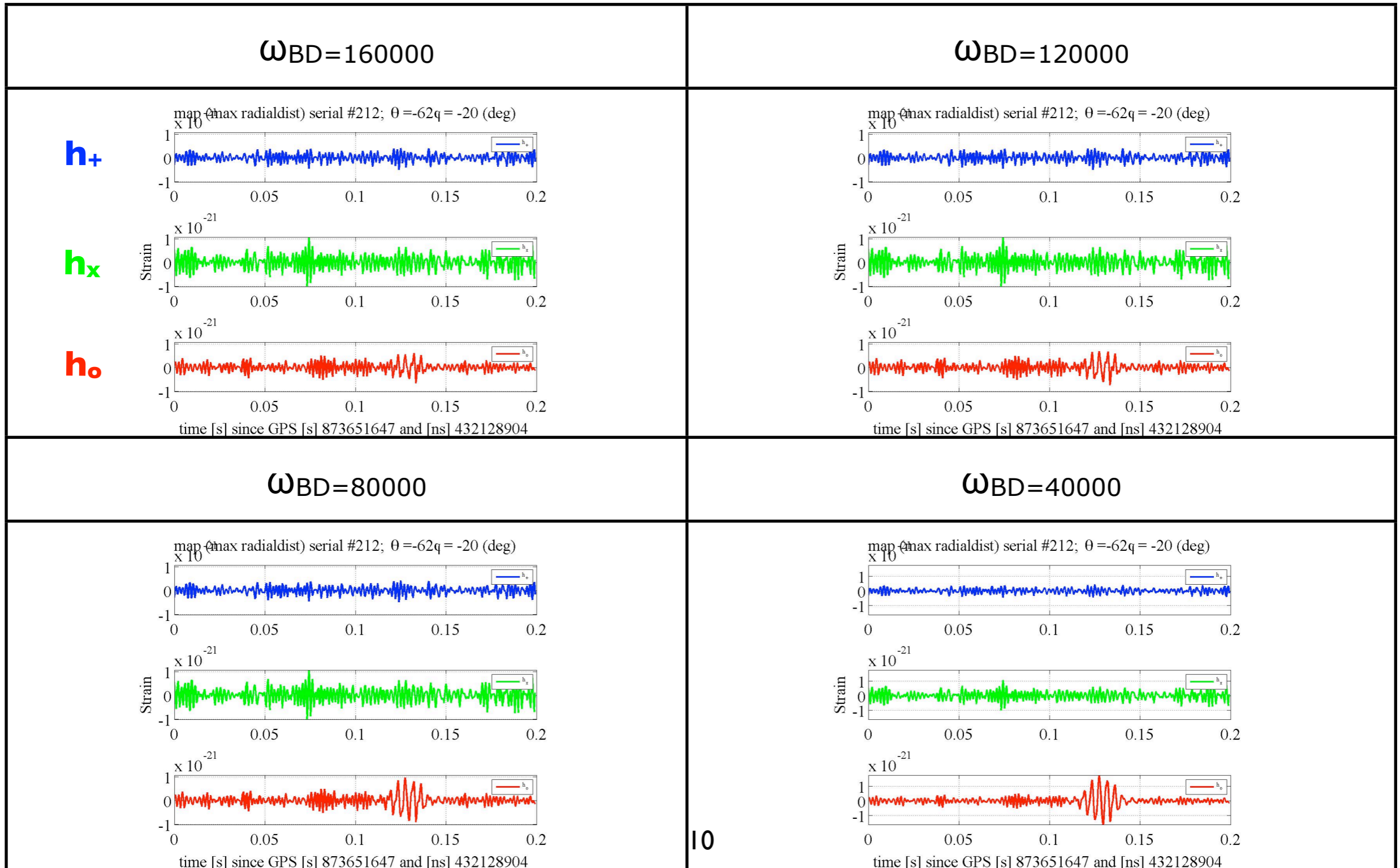
# Waveform reconstructions for $\omega_{BD}$ s



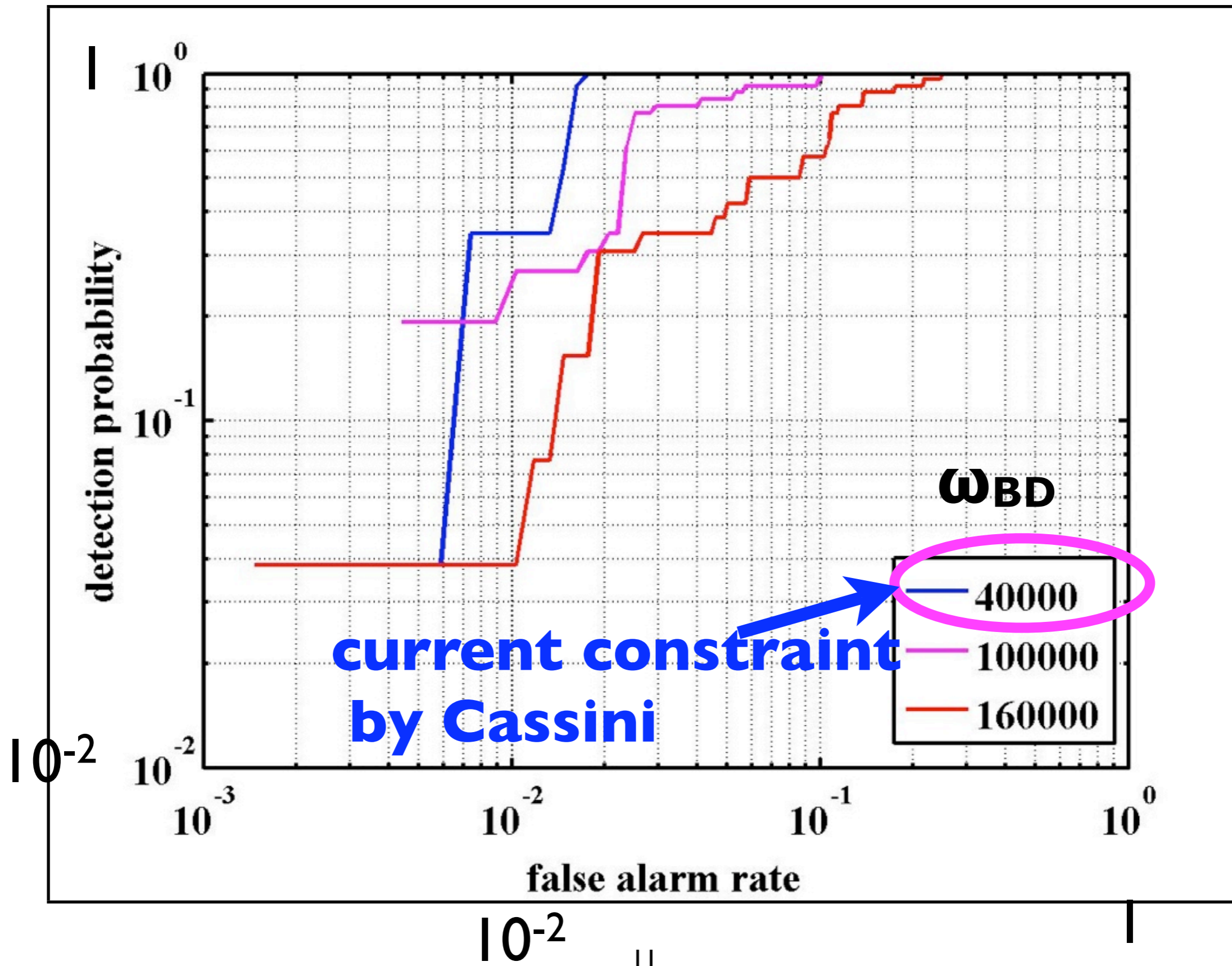
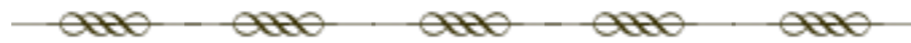
We performed simulations to reconstruct scalar gravitational waves with  $\omega_{BD} = 40000, 80000, 120000, 160000$ .

This simulation uses the design sensitivity of advLIGO for LIGO, VIRGO, and LCGT.

Astrophysical model used is the same as the previous simulation.



# ROC curve for $\omega_{BD}$

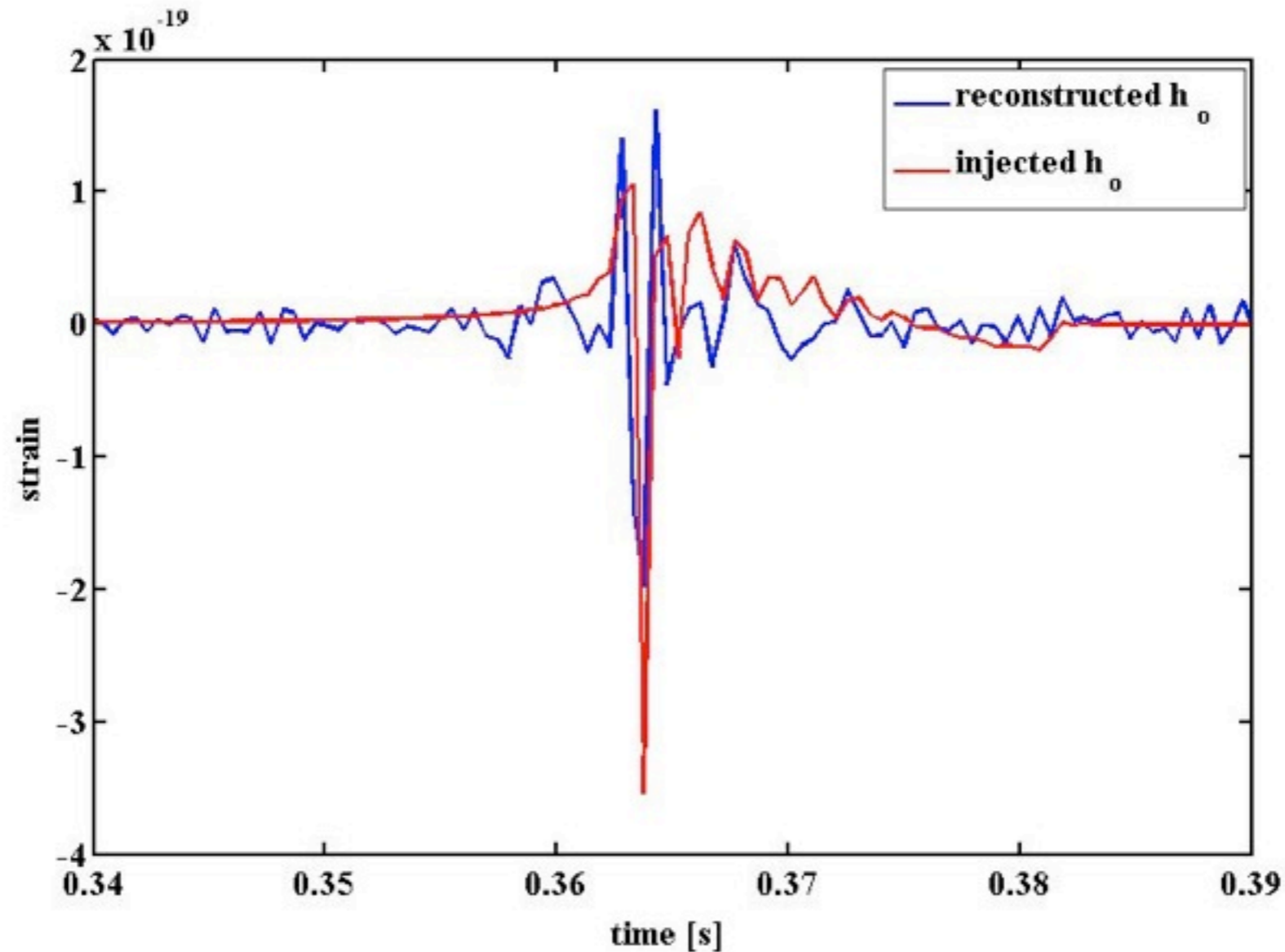


# Summary



- **We discuss search for scalar GW from Galactic spherical core collapse in Brans-Dicke theory with various adv det. network.**
- **Although depending sky location and models, it is possible to put stronger constraint on  $\omega_{BD}$ .**
- **LCGT and LIGO-Australia play an important role for search for scalar gravitational waves**
- **We need numerical simulations of scalar GW in S-T theory.**

# Wavrform comparison



**Red plot is injected  $h_0$  signal and blue plot is the reconstructed  $h_0$ .  
The difference at the low frequency region comes from the data conditioning step.  
Detector noise at low frequency is very high, such region is cut at the step.**